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DOI:

[10.1109/TWC.2017.2697380](https://doi.org/10.1109/TWC.2017.2697380)

Document Version

Accepted author manuscript

[Link to publication record in Manchester Research Explorer](#)

Citation for published version (APA):

Yang, Z., Ding, Z., Fan, P., & Al-Dhahir, N. (2017). The Impact of Power Allocation on Cooperative Non-orthogonal Multiple Access Networks With SWIPT. *Wireless Communications, IEEE Transactions on*.
<https://doi.org/10.1109/TWC.2017.2697380>

Published in:

Wireless Communications, IEEE Transactions on

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The Impact of Power Allocation on Cooperative Non-orthogonal Multiple Access Networks with SWIPT

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Abstract—In this paper, a cooperative non-orthogonal multiple access (NOMA) network is considered, where a source communicates with two users through an energy harvesting relay. The impact of two types of NOMA power allocation policies, namely NOMA with fixed power allocation (F-NOMA) and cognitive radio inspired NOMA (CR-NOMA), on the considered cooperative simultaneous wireless information and power transfer (SWIPT) system is investigated. Particularly, closed-form expressions for the outage probability and their high SNR approximations are derived to characterize the performance of SWIPT-F-NOMA and SWIPT-CR-NOMA. These developed analytical results demonstrate that the two power allocation policies realize different tradeoffs between the reception reliability, user fairness and system complexity. Compared to conventional SWIPT relaying networks with orthogonal multiple access (OMA), the proposed NOMA schemes can effectively reduce the outage probability, although all of them realize the same diversity gain.

Index Terms—Non-orthogonal multiple access, simultaneous wireless information and power transfer, cognitive radio, outage probability, diversity gain.

I. INTRODUCTION

Non-orthogonal multiple access (NOMA) has recently attracted lots of attention, since it can provide high spectral efficiency and realize massive connectivity in the fifth generation (5G) mobile communication network [1] and [2]. In addition, a two-user special case of downlink NOMA has been adopted by Third Generation Partnership Project (3GPP) Long Term Evolution (LTE), termed multi-user superposition transmission (MUST) [3]. Unlike conventional orthogonal multiple access (OMA), multiple users in a NOMA network are allowed to share the same orthogonal resources in the time, frequency, and code domains. Meanwhile, successive interference cancellation (SIC) is applied at the receiver side,

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The work of Zheng Yang and Pingzhi Fan was supported by the National Science and Technology Major Project under Grant 2016ZX03001018-002, the Huawei HIRP Project under Grant YB201504, and the 111 Project under Grant 111-2-14. The work of Zheng Yang was also supported by the National Natural Science Foundation of China (No. 61571128). The work of Z. Ding was supported by the UK EPSRC under grant number EP/L025272/1 and by H2020-MSCA-RISE-2015 under grant number 690750. The work of N. Al-Dhahir was made possible by NPRP grant # NPRP 8-627-2-260 from the Qatar National Research Fund.

in order to remove the co-channel interference due to the implementation of NOMA [4] and [5].

The impact of partial channel state information on the performance of NOMA has been studied in [6], by assuming that users are uniformly distributed in a disk. The performance of NOMA in large-scale underlay cognitive radio (CR) networks with randomly deployed users was studied in [7]. The impact of user pairing on NOMA was investigated in [8], where two types of power allocation schemes were proposed. One is termed NOMA based on fixed power allocation (F-NOMA), and the other is termed CR inspired NOMA (CR-NOMA). The power allocation problem for realizing user fairness in NOMA systems has been investigated in [9], and the work in [10] considered the power allocation problem for NOMA with practical modulation based on finite constellation sizes. In [11], an amplify-and-forward (AF) relay equipped with a single antenna was used to help the base station for serving users equipped with multiple antennas in cooperative NOMA networks.

Simultaneous wireless information and power transfer (SWIPT) is a new paradigm, which can prolong the lifetime of energy constrained networks. Therefore, SWIPT is an important enabling technology to 5G communications, in order to support its Internet of Things (IoT) functionality. The key idea of SWIPT is to encourage nodes to harvest energy from their received radio frequency information-bearing signals, which was firstly proposed in [12]. However, it is not practical for a receiver to decode information and harvest energy at the same time, due to the practical limitation. Motivated by this issue, the authors in [13] have proposed two practical receiver architectures, i.e., power splitting (PS) and time switching (TS). The PS and TS protocol have been applied to cooperative networks with AF relaying, and their outage probability and throughputs have been analysed in [14]. In [15] and [16], game theoretic approaches for PS have been proposed in a multi-user cooperative decode-and-forward (DF) and AF relaying network, respectively. In [17], the author has studied the outage performance and the average harvested energy for SWIPT in large-scale cooperative networks. The work in [18]–[20] investigates the outage probability for the multiple relays with energy storage devices, where the Markov chain model is used to describe the states of the batteries.

Since NOMA improves the spectral efficiency of cooperative networks, and SWIPT provides more incentives for user cooperation, it is natural to consider the combination of NOMA and SWIPT in cooperative networks. An example for such a combination can be found in [21], where users with strong channel conditions were used as energy harvesting

relays to improve the reception reliability for those users with poor channel conditions. In this paper, a different cooperative DF relaying scenario is considered, where one source communicates with two users via a dedicated relay which harvests energy from the source, and the NOMA principle is used for cooperative transmission. The main contribution of this paper is three-fold, as listed in the following:

- We first consider the application of SWIPT to cooperative NOMA with fixed power allocation, where the outage probability and diversity gain are considered as criteria to analyse the system performance. The developed closed-form analytical results show that SWIPT-F-NOMA can achieve better outage performance than SWIPT-OMA under the condition that the power allocation coefficients and the users' targeted rates are chosen correctly.
- With the application of the cognitive radio concept, we consider two types of CR-NOMA with different constraints as explained in the following. One is to meet a fixed quality of service (QoS) requirement, such as a targeted data rate, at the user with worse channel condition (CR-NOMA(F)), and the other is to meet a dynamic QoS requirement at the user with strong channel conditions (CR-NOMA(D)), i.e., this user will experience a larger rate in NOMA than that in OMA. Furthermore, the SWIPT concept is applied into the two CR-NOMA cooperative networks. The exact expressions for the outage probability and their high signal-to-noise ratio (SNR) asymptotic results are derived. The analytical results show that SWIPT-CR-NOMA(F) achieves better outage performance for the user with poor channel conditions, but results in a loss of the outage probability for the user with strong channel conditions, compared to those of SWIPT-OMA. With SWIPT-CR-NOMA(D), the user with the strong channel conditions experiences the same outage probability as the case with SWIPT-OMA, but the user with the poor channel conditions experiences better outage performance compared to the case with SWIPT-OMA.
- Furthermore, the analytical results developed in this paper demonstrate that the use of SWIPT-F-NOMA, SWIPT-CR-NOMA(F), or SWIPT-CR-NOMA(D) will not cause any diversity gain loss, compared to the case that the relay uses its own battery for relay transmission power, but these SWIPT-NOMA schemes will lead to a loss of the outage probability. In addition, SWIPT-CR-NOMA(F) achieves the best outage performance for the user with the poor channel conditions, but the worst outage probability for the user with the strong channel conditions, among the three SWIPT-NOMA schemes.

II. SYSTEM MODEL

Consider a cooperative network with one source (S), one energy harvesting relay (R), and two users (U_1 , U_2). Assume that all the nodes are equipped with a single antenna, and there is no direct link between the source and the users, i.e., the source communicates with the users via the energy harvesting relay. All the wireless channels are assumed to

Fig. 1. System model of NOMA based cooperative network with SWIPT.

undergo quasi-static independent and non-identically Rayleigh fading, as shown in Fig. 1.

The cooperative transmission consists of two time slots. In the first time slot, the source S uses superposition coding to combine two independent signals, x_1 and x_2 , as $x = \sqrt{\gamma_1 P}x_1 + \sqrt{\gamma_2 P}x_2$, where x_k , $k = 1, 2$, is message for U_k , P is the transmission power at source S , and γ_k is the power allocation factor for x_k , with the constraint $\gamma_1 + \gamma_2 = 1$. Therefore, during the first time slot, the receive signal at relay R is given by

$$y_R = \sqrt{(1 - \rho)}(\sqrt{\gamma_1 P}x_1 + \sqrt{\gamma_2 P}x_2)h + w, \quad (1)$$

where ρ is the power splitting coefficient, $w \sim \mathcal{CN}(0, \sigma^2)$ is the additive white Gaussian noise (AWGN), $h = gd^{-\frac{\alpha}{2}}$ is the channel coefficient between S and R , g denotes Rayleigh fading from S to R with $g \sim \mathcal{CN}(0, 1)$, d is the distance between S and R , and α is the path loss exponent.

Without loss of generality, assume that the relay detects the signal, x_1 , first. Therefore, the achievable rates for the relay to detect signal x_1 is given by

$$R_1 = \frac{1}{2} \log_2 \left(1 + \frac{(1 - \rho)\gamma_1 \rho |h|^2}{(1 - \rho)\gamma_2 \rho |h|^2 + 1} \right), \quad (2)$$

where $\rho = \frac{P}{\sigma^2}$ denotes the transmit SNR.

If the relay can successfully decode the message x_1 , i.e., $R_1 \geq R_1^*$, then it can remove the signal x_1 before detecting x_2 , where R_1^* denotes the targeted rate for U_1 . This means that under the condition $R_1 \geq R_1^*$, SIC is successfully carried out at the relay, and the message x_2 will be detected at the relay with the following instantaneous rate

$$R_2 = \frac{1}{2} \log_2 \left(1 + (1 - \rho)\gamma_2 \rho |h|^2 \right). \quad (3)$$

It is noted that the power splitting protocol is applied at the relay to harvest energy from the source. In addition, the relay uses the DF protocol to decode the signals from the source. Because of these reasons, the relay has to firstly ensure the detection of the messages from the source, then it can carry out energy harvesting. In other words, only when the relay can successfully decode the signals from the source, it can use the harvested energy to forward the signals to the users. Therefore, it is much more important for the relay to decode the information than performing energy harvesting.

In order to ensure that the relay can harvest the sufficient energy to power the relay transmission, we impose the following constraints, $R_1 = R_1^*$ and $R_2 = R_2^*$, which imply that relay R can correctly decode both the signals x_1 and x_2 , simultaneously, where R_2^* denote the targeted data rates for U_2 . With these imposed conditions, $R_1 = R_1^*$ and $R_2 = R_2^*$, i.e.,

$$\begin{cases} \frac{1}{2} \log_2 \left(1 + \frac{(1-\varrho)\gamma_1 \rho |h|^2}{(1-\varrho)\gamma_2 \rho |h|^2 + 1} \right) = R_1^* \\ \frac{1}{2} \log_2 (1 + (1-\varrho)\gamma_2 \rho |h|^2) = R_2^* \end{cases} \quad (4)$$

After some algebraic manipulations, (4) can be rewritten as follows:

$$\begin{cases} (1-\varrho)\rho |h|^2 (1 - 2^{2R_1^*} \gamma_2) = 2^{2R_1^*} - 1 \\ (1-\varrho)\rho |h|^2 \gamma_2 = 2^{2R_2^*} - 1 \end{cases} \quad (5)$$

According to (5), it is easy to obtain the power allocation factor γ_2 and the power splitting factor ϱ which are given by

$$\gamma_2 = \frac{2^{2R_2^*} - 1}{2^{2R_1^* + 2R_2^*} - 1}, \quad (6)$$

and

$$\varrho = \max \left\{ 0, 1 - \frac{2^{2R_1^* + 2R_2^*} - 1}{\rho |h|^2} \right\}, \quad (7)$$

respectively, note that $0 < \gamma_2 < 1$, and $\varrho < 1$. Hence $\varrho = 0$ means the received signals from the source are fully used for information decoding, and the relay cannot harvest any energy.

Based on (1), the energy harvested at relay R is given by [14], [15]

$$P_R = \eta \varrho P |h|^2, \quad (8)$$

where η is the energy harvesting coefficient. Note that the energy harvested from AWGN has been omitted.

Based on (6) and (7), the maximal transmission power at relay R can be obtained as follows:

$$P_R = \max \{0, \eta(P|h|^2 - \varepsilon\sigma^2)\}, \quad (9)$$

where $\varepsilon = 2^{2R_1^* + 2R_2^*} - 1$.

The reason for the simplified energy harvesting model in (9) is given as follows. On one hand, the contribution of this paper is to show that the use of NOMA can yield some significant outage performance gains, compared to OMA, when both of them use the same SWIPT protocol. On the other hand, the simplified SWIPT model can provide some insights to understand the advantage of combining SWIPT with NOMA, which can offer some technical guidances to implement SWIPT in practice. It is worth pointing out that it is a promising future direction to study the impact of the energy for maintaining the user circuits on the performance of SWIPT, which is beyond the scope of this paper.

Since both x_1 and x_2 are decoded correctly at the relay, the NOMA scheme can be used to serve the two users in the second time slot. Firstly, denote $h_k = g_k d_k^{-\frac{\alpha}{2}}$, $k = 1, 2$, is the channel coefficient between the relay and U_k , where $g_k \sim \mathcal{CN}(0, 1)$ and d_k are Rayleigh fading and the distance from the relay to U_k , respectively. Without loss of generality, assume that the channel fading gains $|h_k|^2$ are ordered as $|h_1|^2 \leq |h_2|^2$. According to NOMA scheme, the relay retransmits a

superimposed mixture of x_1 and x_2 as $x_R = \sqrt{\alpha_1 P_R} x_1 + \sqrt{\alpha_2 P_R} x_2$, where $\alpha_k, k = 1, 2$, is power allocation factor for U_k , with $\alpha_1 > \alpha_2$ and $\alpha_1 + \alpha_2 = 1$. The received signal at the k -th user, $k = 1, 2$, is given by

$$y_k = (\sqrt{\alpha_1 P_R} x_1 + \sqrt{\alpha_2 P_R} x_2) h_k + w_k, \quad (10)$$

where w_k is AWGN with mean zero and variance σ^2 .

Based on the NOMA principle, both users will decode x_1 first, since $|h_1|^2 \leq |h_2|^2$. Therefore, the achievable rate for U_1 to detect x_1 is given by

$$R_1^N = \frac{1}{2} \log_2 \left(1 + \frac{\alpha_1 \rho_R |h_1|^2}{\alpha_2 \rho_R |h_1|^2 + 1} \right), \quad (11)$$

where $\rho_R = \frac{P_R}{\sigma^2}$.

The achievable rate for U_2 to detect x_1 is given by

$$R_{1 \rightarrow 2}^N = \frac{1}{2} \log_2 \left(1 + \frac{\alpha_1 \rho_R |h_2|^2}{\alpha_2 \rho_R |h_2|^2 + 1} \right). \quad (12)$$

Note that if $R_{1 \rightarrow 2}^N \geq R_1^*$, i.e., U_2 can correctly decode the signal, x_1 , which means that under the condition $R_{1 \rightarrow 2}^N \geq R_1^*$, the SIC can be successfully carried out at U_2 to remove the signal, x_1 . Therefore, the achievable rate for U_2 to decode x_2 is given by

$$R_2^N = \frac{1}{2} \log_2 (1 + \alpha_2 \rho_R |h_2|^2). \quad (13)$$

We will investigate the outage performance of SWIPT-NOMA with two types of power allocation schemes in the following two sections. The motivation for considering the outage as the performance evaluation criterion is explained in the following.

Recall that the bit error ratio (BER) is an important performance criterion which can be used to evaluate the errors that occur in a transmission system. However, it is difficult to obtain the BER in closed-form expressions, since it depends on which coding and modulation schemes are used. Fortunately, the outage probability can be evaluated in a simpler way and provides a tight bound on the BER, when optimal coding with an infinite length is used [22].

Furthermore, the outage probability is defined as the event that when the instantaneous rate at the receiver falls below a targeted data rate, which can be used to measure a predefined QoS requirement for delay-sensitive networks. This is because the throughput is a function of the channel fading quality, and evaluating the satisfied QoS requirement is quite challenging. Therefore, it is important to investigate the outage performance in wireless communication system, especially in delay-sensitive networks.

III. NOMA BASED ON FIXED POWER ALLOCATION

With F-NOMA, the power allocation factors for the users are constants and the strong user is allocated less power than the weak user, as long as the order of the users' channels is still the same. In this case, the power allocation coefficients are not functions of the users' channel fading gains, i.e., the transmitter only needs to know the order of the users' channel fading gains to perform NOMA.

Recall that the relay harvests energy from the source and the SIC is carried out at U_2 to remove the signal x_1 , before detecting its own message. Therefore the coverage probability for U_2 can be defined as follows:

$$\bar{P}_2^F = \Pr\{R_{1 \rightarrow 2}^N \geq R_1^*, R_2^N \geq R_2^*, P_R > 0\}. \quad (14)$$

The following theorem provides a closed-form expression for the outage probability experienced by U_2 and its approximation in the high SNR region, when F-NOMA relaying is used.

Theorem 1: The use of F-NOMA SWIPT relaying ensures that the following outage probability is achieved at U_2

$$P_2^F = 1 - e^{-\frac{d^\alpha \varepsilon}{\rho}} (\phi_1 K_1(\phi_1) - \phi_2 K_1(\phi_2) + \phi_3 K_1(\phi_3)), \quad (15)$$

where $\Psi_{\max} = \max\left\{\frac{\varepsilon_1}{\eta(\alpha_1 - \alpha_2 \varepsilon_1)}, \frac{\varepsilon_2}{\eta \alpha_2}\right\}$, $\alpha_1 > \alpha_2 \varepsilon_1$, $\varepsilon_1 = 2^{2R_1^*} - 1$, $\varepsilon_2 = 2^{2R_2^*} - 1$, $\phi_1 = \sqrt{\frac{4\Psi_{\max} d^\alpha d_1^\alpha}{\rho}}$, $\phi_2 = \sqrt{\frac{4\Psi_{\max} d^\alpha (d_1^\alpha + d_2^\alpha)}{\rho}}$, $\phi_3 = \sqrt{\frac{4\Psi_{\max} d^\alpha d_2^\alpha}{\rho}}$, and $K_v(\cdot)$ denotes the modified Bessel function of the second kind with order v [23]. The high SNR approximation for P_2^F is given by

$$P_2^F \approx \frac{d^\alpha}{\rho} \left(\varepsilon - \Psi_{\max} d_1^\alpha \ln \frac{d_1^\alpha}{d_1^\alpha + d_2^\alpha} - \Psi_{\max} d_2^\alpha \ln \frac{d_2^\alpha}{d_1^\alpha + d_2^\alpha} \right). \quad (16)$$

Proof: See Appendix A. ■

Due to the fact that line-of-sight path of the S-R link may exist, we use Nakagami- m fading for the S-R link to which SWIPT is applied, and investigate the outage performance for U_2 in SWIPT-F-NOMA systems. Particularly, assume that the S-R link, denoted by h , follows a Nakagami- m distribution with a sharp parameter m and a variance λ , whereas the links from the relay to the users follow Rayleigh fading.

Most results in this paper can be extended to the case with Nakagami- m fading. For example, the outage probability for U_2 in SWIPT-F-NOMA is given in the following Lemma.

Lemma 1: The closed-form expression for the outage probability at U_2 in SWIPT-F-NOMA is given by

$$\tilde{P}_2^F = 1 - \frac{e^{-\frac{m\varepsilon}{\lambda\rho}}}{\Gamma(m)} \sum_{i=0}^{m-1} 2^{-i} \binom{m-1}{i} \left(\frac{m\varepsilon}{\lambda\rho}\right)^{m-1-i} \times (\Phi_1^{i+1} K_{i+1}(\Phi_1) - \Phi_2^{i+1} K_{i+1}(\Phi_2) + \Phi_3^{i+1} K_{i+1}(\Phi_3)), \quad (17)$$

where m is an integer, $\Phi_1 = \sqrt{\frac{4m\Psi_{\max} d^\alpha}{\lambda\rho}}$, $\Phi_2 = \sqrt{\frac{4m\Psi_{\max} (d_1^\alpha + d_2^\alpha)}{\lambda\rho}}$, $\Phi_3 = \sqrt{\frac{4m\Psi_{\max} d_2^\alpha}{\lambda\rho}}$.

Proof: By using steps similar to those used to prove Theorem 1, and also using the fact that the PDF of $|h|^2$ is given by

$$f_{|h|^2}(x) = \frac{m^m}{\Gamma(m)\lambda^m} x^{m-1} e^{-\frac{mx}{\lambda}}, \quad (18)$$

the Lemma is proved. ■

It can be observed from (17) that the closed-form expression can be found under the condition that m is an integer, and it is difficult if m is not an integer. It is important to point out that Rayleigh fading is a special case of Nakagami- m fading with $m = 1$, as such, we adopt Rayleigh fading to model the link

with SWIPT in the remaining of this paper, in order to evaluate the outage performance with mathematical tractability.

Similar to (14), the coverage probability at U_1 in F-NOMA SWIPT relaying transmission is defined as follows:

$$\bar{P}_1^F = \Pr\{R_1^N \geq R_1^*, P_R > 0\}. \quad (19)$$

Recall that the cumulative density function (CDF) of $|h_1|^2$ is given by

$$F_{|h_1|^2}(x) = 1 - e^{-(d_1^\alpha + d_2^\alpha)x}. \quad (20)$$

By using this CDF and also following the steps similar to those in the proof of Theorem 1, a closed-form expression for the outage probability experienced by U_1 in F-NOMA SWIPT relaying transmission and its high SNR approximation can be obtained as follows:

$$P_1^F = 1 - e^{-\frac{d^\alpha \varepsilon}{\rho}} \phi_4 K_1(\phi_4) \approx \frac{\Psi_1 d^\alpha (d_1^\alpha + d_2^\alpha)}{\rho} \ln \frac{\rho}{\Psi_1 d^\alpha (d_1^\alpha + d_2^\alpha)}, \quad (21)$$

where $\Psi_1 = \frac{\varepsilon_1}{\eta(\alpha_1 - \alpha_2 \varepsilon_1)}$, $\alpha_1 > \alpha_2 \varepsilon_1$, and $\phi_4 = \sqrt{\frac{4\Psi_1 d^\alpha (d_1^\alpha + d_2^\alpha)}{\rho}}$.

The outage probability of OMA: OMA is a good benchmarking scheme for the NOMA transmission protocol. In cooperative SWIPT networks, if source communicates with U_i , $i = 1, 2$, via an energy harvesting relay in an OMA mode, such as time division multiple access (TDMA), four time slots are needed in total to serve U_1 and U_2 . Similar to (9), the maximal transmission power for the i -th user is given by

$$P_{R,i} = \max\{0, \eta(P|h|^2 - \varepsilon_i' \sigma^2)\}, \quad (22)$$

where $\varepsilon_i' = 2^{4R_i^*} - 1$, $i = 1, 2$.

The achievable rate for the energy harvesting relay communicating with U_i in OMA is given by

$$R_i^T = \frac{1}{4} \log_2(1 + \rho_{R,i} |h_i|^2), \quad (23)$$

where $\rho_{R,i} = \frac{P_{R,i}}{\sigma^2}$.

The use of the OMA strategy means that the outage probability at U_i can be defined as follows:

$$P_i^O = 1 - \Pr\left\{\frac{1}{4} \log_2(1 + \rho_{R,i} |h_i|^2) > R_i^*, P|h|^2 > \varepsilon_i' \sigma^2\right\} = 1 - \Pr\left\{|h_i|^2 > \frac{\varepsilon_i'}{\eta(\rho|h|^2 - \varepsilon_i')}, |h|^2 > \frac{\varepsilon_i'}{\rho}\right\}. \quad (24)$$

Based on (24) and following the steps similar to those in the proof for Theorem 1, the outage probability of U_1 in OMA and its high SNR approximation are given by

$$P_1^O = 1 - e^{-\frac{d^\alpha \varepsilon_1'}{\rho}} \phi_5 K_1(\phi_5) \approx \frac{\varepsilon_1' d^\alpha (d_1^\alpha + d_2^\alpha)}{\eta \rho} \ln \frac{\eta \rho}{\varepsilon_1' d^\alpha (d_1^\alpha + d_2^\alpha)}, \quad (25)$$

where $\phi_5 = \sqrt{\frac{4\varepsilon_1' d^\alpha (d_1^\alpha + d_2^\alpha)}{\eta \rho}}$

Similarly, the outage probability of U_2 in OMA and its high SNR approximation are given by

$$P_2^O = 1 - e^{-\frac{d^\alpha \varepsilon_2'}{\rho}} \left(\phi_6 K_1(\phi_6) - \phi_7 K_1(\phi_7) + \phi_8 K_1(\phi_8) \right) \\ \approx \frac{d^\alpha}{\rho} \left(\varepsilon - \varepsilon_2' d_1^\alpha \ln \frac{d_1^\alpha}{d_1^\alpha + d_2^\alpha} - \varepsilon_2' d_2^\alpha \ln \frac{d_2^\alpha}{d_1^\alpha + d_2^\alpha} \right), \quad (26)$$

where $\phi_6 = \sqrt{\frac{4\varepsilon_2' d^\alpha d_1^\alpha}{\eta\rho}}$, $\phi_7 = \sqrt{\frac{4\varepsilon_2' d^\alpha (d_1^\alpha + d_2^\alpha)}{\eta\rho}}$, and $\phi_8 = \sqrt{\frac{4\varepsilon_2' d^\alpha d_2^\alpha}{\eta\rho}}$.

One can observe from (16) and (26), (21) and (25) that F-NOMA based SWIPT can achieve the same diversity gain as OMA based SWIPT. However, in Section V, both simulations and analytical results demonstrate that F-NOMA based SWIPT can realize a better outage performance compared to the OMA scheme. This is because the use of NOMA allows all the users to share the bandwidth resources, which yields higher spectral efficiency, compared to OMA.

IV. COGNITIVE RADIO INSPIRED NOMA

In this Section, we focus on two types of CR inspired NOMA. The first one is to treat the user with poor connections to the relay as a primary user, and the other one is to treat the user with strong connections to the relay as a primary user.

A. CR-NOMA with a fixed QoS requirement at the weak user

Theorem 1 shows that SWIPT-F-NOMA can achieve better performance than SWIPT-OMA under the condition $\alpha_1 > \alpha_2 \varepsilon_1$, i.e., the power allocation factors and the users' targeted rates need to be carefully chosen. In order to overcome this disadvantage, we can consider NOMA as a special case of CR systems [8], where a user with poor channel conditions is considered as a primary user sharing the same spectrum with a secondary user, which has strong channel conditions. The advantage of this CR-NOMA is that the QoS requirement of the weak user can be strictly guaranteed.

Recall that the channel fading gains have been ordered as $|h_1|^2 \leq |h_2|^2$, which means U_1 can be considered as a primary user and should be served with high priority based on the concept of CR networks [24]. Therefore, the rate at U_1 , R_1^N , in (11) needs to satisfy the following constraint:

$$\frac{1}{2} \log_2 \left(1 + \frac{\alpha_1 \rho_R |h_1|^2}{\alpha_2 \rho_R |h_1|^2 + 1} \right) \geq R_1^*, \quad (27)$$

which means that the maximal transmit power factor α_2 can be used for U_2 is given by

$$\alpha_2 = \max \left\{ 0, \frac{\rho_R |h_1|^2 - \varepsilon_1}{\rho_R |h_1|^2 (1 + \varepsilon_1)} \right\}. \quad (28)$$

Based on the relay transmission power P_R in (9) and the power allocation factor α_2 in (28), a closed-form expression for the outage probability at U_1 in CR-NOMA can be obtained as follows:

$$P_1^{C,I} = 1 - \Pr \left\{ |h|^2 > \frac{\varepsilon}{\rho}, |h_1|^2 > \frac{\varepsilon_1}{\eta(\rho|h|^2 - \varepsilon)} \right\} \\ = 1 - \int_{\frac{\varepsilon}{\rho}}^{\infty} e^{-\frac{(d_1^\alpha + d_2^\alpha) \varepsilon_1}{\eta(\rho x - \varepsilon)}} d^\alpha e^{-d^\alpha x} dx \\ = 1 - e^{-\frac{d^\alpha \varepsilon}{\rho}} \phi_9 K_1(\phi_9), \quad (29)$$

where $\phi_9 = \sqrt{\frac{4\varepsilon_1 d^\alpha (d_1^\alpha + d_2^\alpha)}{\eta\rho}}$.

At high SNR, $P_1^{C,I}$ can be approximated as follows:

$$P_1^{C,I} \approx \frac{\varepsilon_1 d^\alpha (d_1^\alpha + d_2^\alpha)}{\eta\rho} \ln \frac{\eta\rho}{\varepsilon_1 d^\alpha (d_1^\alpha + d_2^\alpha)}. \quad (30)$$

Based on (9), (13), and (28), the coverage probability of U_2 in CR-NOMA(F) relaying SWIPT transmission is defined as follows:

$$\bar{P}_2^{C,I} = \left\{ R_2^N \geq R_2^*, \rho_R > 0, |h_1|^2 > \frac{\varepsilon_1}{\rho_R} \right\}. \quad (31)$$

The following theorem provides an exact expression for the outage probability experienced by U_2 and its approximation at high SNR.

Theorem 2: The use of CR-NOMA with a fixed QoS constraint at U_1 yields an outage probability at U_2 as follows:

$$P_2^{C,I} = 1 - e^{-\frac{d^\alpha \varepsilon}{\rho}} \sqrt{\frac{\tau}{\rho}} K_1 \left(\sqrt{\frac{\tau}{\rho}} \right) - \sum_{i_1, i_2 \in \{1, 2\}} \frac{2d^\alpha d_{i_1}^\alpha e^{-\frac{d^\alpha \varepsilon}{\rho}}}{\eta\rho} \\ \times \int_0^{\varepsilon_2(1+\varepsilon_1)} K_0 \left(2\sqrt{\frac{g_{i_1, i_2}(s)}{\rho}} \right) ds, \quad (32)$$

where $g_{i_1, i_2}(s) = \frac{d^\alpha d_{i_2}^\alpha \varepsilon_2(1+\varepsilon_1)(s+\varepsilon_1) + d^\alpha d_{i_1}^\alpha s(s+\varepsilon_1)}{\eta s}$, $\tau = \frac{4d^\alpha (d_1^\alpha + d_2^\alpha)(\varepsilon_1 + \varepsilon_2(1+\varepsilon_1))}{\eta}$. When $\rho \rightarrow \infty$, the high SNR approximation of the outage probability is given by

$$P_2^{C,I} \approx \frac{\ln \rho}{\rho}. \quad (33)$$

Proof: See Appendix B. ■

Comparing (33) to (26), we can see that the diversity gain at U_2 in SWIPT-CR-NOMA(F) is identical to that in SWIPT-OMA, but the use of CR-NOMA results in a higher outage probability, compares to the OMA case. The main reason is that U_2 is regarded as a secondary user in SWIPT-CR-NOMA(F), and it is served only after the QoS requirement of U_1 is satisfied.

B. CR-NOMA with a dynamic QoS requirement at the strong user

Recall that by using this CR-NOMA inspired power allocation policy, the strong user can be served by the transmitter only when the weak user's QoS is met. Especially, when the weak user's targeted rate is very high, the transmitter has to allocate all the power to support this user, and the strong user cannot be served. In order to ensure that the strong user in NOMA systems can be also served, we impose a constraint that this user achieves at least the same throughput as that in OMA, then allocate all the remaining power to the weak user. In other words, the user with strong channel conditions is regarded as a primary user, and consider a dynamic QoS requirement of this user which is to achieve a rate larger than that of OMA, i.e.,

$$\frac{1}{2} \log_2 (1 + \alpha_2 \rho_R |h_2|^2) \geq \frac{1}{4} \log_2 (1 + \rho_{R,2} |h_2|^2), \quad (34)$$

which means the maximal power allocation factor α_1 is given by

$$\alpha_1 = 1 - \frac{\sqrt{1 + \rho_{R,2}|h_2|^2} - 1}{\rho_R|h_2|^2}. \quad (35)$$

Based on (35), the coverage probability of U_2 in CR-NOMA with a dynamic QoS requirement at the strong user (SWIPT-CR-NOMA(D)) can be expressed as follows:

$$\begin{aligned} \bar{P}_2^{C,II} &= \Pr\left\{\frac{1}{2} \log_2 \left(1 + \frac{\alpha_1 \rho_R |h_2|^2}{\alpha_2 \rho_R |h_2|^2 + 1}\right) \geq R_1^*, \right. \\ &\quad \left. \frac{1}{2} \log_2 (1 + \alpha_2 \rho_R |h_2|^2) \geq R_2^* \right\} \\ &= \Pr\left\{\frac{1}{4} \log_2 (1 + \rho_{R,2} |h_2|^2) \geq R_1^*, \right. \\ &\quad \left. \frac{1}{4} \log_2 (1 + \rho_{R,2} |h_2|^2) \geq R_2^* \right\} \\ &= \Pr\left\{\frac{1}{4} \log_2 (1 + \rho_{R,2} |h_2|^2) \geq R_2^* \right\}. \end{aligned} \quad (36)$$

From (36), it is interesting to observe that U_2 in SWIPT-CR-NOMA(D) can experience the same coverage probability as that of SWIPT-OMA. The reason for this is that the maximal power allocation factor α_1 in (35) is based on the condition in (34), i.e., U_2 should get a rate no less than that in OMA.

Theorem 3: The use of CR-NOMA with a dynamic QoS requirement at the strong user yields an outage probability at U_1 as expressed in (37) at the top of the next page, where $\rho_{R,2} = \eta(\rho_Z - \varepsilon_2')$, $\rho_R = \eta(\rho_Z - \varepsilon)$, $H(x) = \frac{\rho_{R,2} - 2g(x)}{g^2(x)}$, $g(x) = \frac{\rho_R x - \varepsilon_1}{(\varepsilon_1 + 1)x}$, $K(\rho_{R,2}, \rho_R) = \frac{\rho_{R,2}(\varepsilon_1 + 1)^2 - 2\rho_R + \sqrt{\Delta(\rho_{R,2}, \rho_R)}}{2\rho_R^2}$, $\Delta(\rho_{R,2}, \rho_R) = (\rho_{R,2}(\varepsilon_1 + 1)^2 - 2\rho_R)^2 + 4\rho_R^2(\varepsilon_1^2 + 2\varepsilon_1)$. At high SNR, $P_1^{C,II}$ can be approximated as follows:

$$P_1^{C,II} \approx \frac{\ln \rho}{\rho}. \quad (38)$$

Proof: See Appendix C. ■

Note that the SWIPT-CR-NOMA(D) achieves similar outage performance compared to SWIPT-OMA at high SNR, as the approximated expression in (38) is quite similar to that in (25) at high SNR. However, the simulation results in Section V show that the outage probability of U_1 in SWIPT-CR-NOMA(D) is always better than that in SWIPT-OMA. The main reason is that the power allocation factor, α_1 , in (35) is a function of the strong user's channel gain, and the rate for U_1 , R_1^N , in (11) is an increasing function of α_1 , which can further improve the weak user's performance.

V. NUMERICAL RESULTS

In this section, computer simulations are used to verify the accuracy of the developed analytical results about the outage probability of NOMA based cooperative SWIPT networks. In the considerable network, we choose the energy harvesting efficiency $\eta = 0.4$, the path loss factor $\alpha = 4$. The carrier frequency, transmitter antenna gain, and receiver antenna gain are set to be 915 MHz, 1 dBm, and 1 dBm, respectively. Fig. 2-Fig. 4 are obtained with the following distances, where the distance between the source and the relay is given by $d =$

Fig. 2. SWIPT-F-NOMA with $\alpha_1 = 0.75$ and $\alpha_2 = 0.25$.

10 m, the distances from relay to U_1 and U_2 are given by $d_1 = 25$ m and $d_2 = 10$ m, respectively, and the noise power is set to be -114 dBm. Fig. 5 is obtained with the following distances, where the distance between the source and the relay is given by $d = 5$ m, the distances from the relay to the U_1 and the U_2 are given by $d_1 = 16$ m and $d_2 = 5$ m, respectively, and the noise power is set to be -84 dBm.

Fig. 2 shows the outage performance of F-NOMA with SWIPT in cooperative networks as a function of the transmitter power P . It can be seen from Fig. 2 that SWIPT-F-NOMA achieves the same diversity gain as SWIPT-OMA, but the NOMA scheme offers a constant performance gain in the outage probability, compared to the OMA scheme. This is because NOMA allows multiple users to share the same resources at the time, frequency and code domains via power domain multiplexing. Furthermore, if the users' targeted rates and power allocation factors cannot satisfy $\alpha_1 > \alpha_2 \varepsilon_1$, the outage will always occur, as stated in Theorem 1. In addition, it is important to point out that the curves for the closed-form expressions in (15), (21), (25) and (26) match Monte Carlo simulation results perfectly.

Fig. 3. SWIPT-CR-NOMA with a fixed QoS requirement at the weak user.

$$\begin{aligned}
P_1^{C,II} = & 1 - d^\alpha \int_{\frac{\varepsilon_2}{\rho}}^{\infty} \left(e^{-(d_1^\alpha + d_2^\alpha)K(\rho_R, 2, \rho_R)} - e^{-\frac{(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta(\rho z - \varepsilon)}} \right) e^{-d^\alpha z} dz - e^{-\frac{d^\alpha \varepsilon}{\rho}} \sqrt{\frac{4d^\alpha(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta\rho}} K_1 \left(\sqrt{\frac{4d^\alpha(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta\rho}} \right) \\
& - \sum_{i_1, i_2 \in \{1, 2\}} d_{i_1}^\alpha \int_{\frac{\varepsilon_2}{\rho}}^{\infty} \int_{\frac{\varepsilon_1}{\rho_R}}^{K(\rho_R, 2, \rho_R)} e^{-d_{i_2}^\alpha H(x) - d_{i_1}^\alpha x} dx d^\alpha z e^{-d^\alpha z} dz.
\end{aligned} \quad (37)$$

In Fig. 3, the outage probability of SWIPT-CR-NOMA with a fixed QoS constraint at the weak user is investigated. Fig. 3 demonstrates that all the curves are parallel, which means the achievable diversity order is the same for SWIPT-CR-NOMA(F) and SWIPT-OMA. Compared to SWIPT-OMA, it is interesting to find that the weak user in SWIPT-CR-NOMA(F) can significantly improve its outage performance, while the strong user's outage probability is deteriorated severely. This is because the power allocation factor, α_2 in (28) is a function of the weak user's channel gain, and the strong user cannot get sufficient power, especially when the weak user's targeted rate is high. Again, Fig. 3 confirms that the analytical results developed in (29) and (32) perfectly match computer simulations.

Fig. 4. The outage probability of weak user in SWIPT-CR-NOMA(D) with a dynamic QoS requirement at the strong user.

In Fig. 4, we focus on the outage performance of the user with weak channel conditions when the CR-NOMA power allocation policy is designed to meet the dynamic QoS constraint at the strong user. Note that there is no need to show the performance of U_2 , since this strong user experiences the same outage performance as in SWIPT-OMA. As can be observed from Fig. 4, SWIPT-CR-NOMA(D) can achieve better outage performance than SWIPT-OMA, although the same diversity gain is realized by both schemes. Furthermore, Fig. 4 also demonstrates that the users' targeted rates significantly affect the performance gap between NOMA and OMA. Particularly, as the difference between R_1^* and R_2^* increases, the outage performance gap between SWIPT-CR-NOMA(D) and SWIPT-OMA enlarges accordingly. In addition, computer simulations also confirm the accuracy of the analytical results developed in (37).

In Fig. 5, the outage probability difference between the

(a) The weak user.

(b) The strong user.

Fig. 5. Outage probability comparison with/without SWIPT for CR-NOMA and F-NOMA, where $\gamma_1 = \alpha_1 = 0.7$, $\gamma_2 = \alpha_2 = 0.3$, $R_1^* = 0.5 \text{ bits/s/Hz}$, $R_2^* = 1.5 \text{ bits/s/Hz}$.

NOMA schemes with SWIPT and without SWIPT is studied. Fig. 5 demonstrates that the diversity gain achieved by NOMA with SWIPT is the same as that achieved by NOMA without energy harvesting, but the use of SWIPT results in a outage probability loss. This phenomenon is expected since the use of SWIPT means that the relay transmission power which is harvested from the signals sent by the source is much smaller than that in the case without SWIPT. In addition, it can be seen from Fig. 5 that SWIPT-CR-NOMA(F) achieves the best outage performance for the weak user, but the worst outage probability for the strong user.

VI. CONCLUSIONS

We have investigated the application of SWIPT to cooperative F-NOMA and CR-NOMA networks, and their outage probabilities have been analyzed in this paper. Compared to SWIPT-OMA, SWIPT-F-NOMA can achieve better outage performance if the users' targeted rates and power allocation coefficients are correctly chosen. For SWIPT-CR-NOMA(F), the outage performance of the user with strong channel conditions is degraded compared to the OMA case, but the outage performance of the weak user can be significantly improved. Furthermore, for CR-NOMA-SWIPT(D), the weak user' outage performance improves evidently and there is no loss in the outage performance at the user with strong channel conditions, compared to SWIPT-OMA.

In this paper, the effect of power allocation on cooperative NOMA with SWIPT has been investigated, where all the nodes are equipped with a single antenna, and an important future direction is to consider the application of multiple-input multiple-output technologies to the addressed cooperative SWIPT-NOMA networks. In addition, another promising future direction is that the addressed system model in this paper can be extended to the case with multiple relays to improve the reception reliability of NOMA transmission. The key step is to consider how many relays can correctly decode the source signals and harvest energy from the source simultaneously, then choose one relay from the qualified relays to serve two users with different power allocation schemes.

APPENDIX A

PROOF OF THEOREM 1

Based on (14), the coverage probability of U_2 can be rewritten as follows:

$$\begin{aligned}\bar{P}_2^F &= \Pr\left\{\frac{1}{2}\log_2\left(1 + \frac{\alpha_1\rho_R|h_2|^2}{\alpha_2\rho_R|h_2|^2 + 1}\right) \geq R_1^*, \right. \\ &\quad \left. \frac{1}{2}\log_2(1 + \alpha_2\rho_R|h_2|^2) \geq R_2^*, P_R > 0\right\} \\ &= \Pr\left\{(\rho|h|^2 - \varepsilon)|h_2|^2 > \Psi_{\max}, |h|^2 > \frac{\varepsilon}{\rho}\right\}. \quad (39)\end{aligned}$$

Since the unordered channel fading gains $|\tilde{h}_k|^2, k = 1, 2$ are exponentially distributed with different expectations, the CDF of $|h_2|^2$ is given by

$$F_{|h_2|^2}(y) = (1 - e^{-d_1^\alpha y})(1 - e^{-d_2^\alpha y}). \quad (40)$$

Based on (40), the coverage probability $\bar{P}_2^F$ in (39) can be calculated as follows:

$$\begin{aligned}\bar{P}_2^F &= \int_{\frac{\varepsilon}{\rho}}^{\infty} \left(e^{-\frac{d_1^\alpha \Psi_{\max}}{\rho x - \varepsilon}} + e^{-\frac{d_2^\alpha \Psi_{\max}}{\rho x - \varepsilon}} - e^{-\frac{(d_1^\alpha + d_2^\alpha) \Psi_{\max}}{\rho x - \varepsilon}} \right) \\ &\quad \times d^\alpha e^{-d^\alpha x} dx. \quad (41)\end{aligned}$$

Let $t = \rho x - \varepsilon$, the above $\bar{P}_2^F$ can be further evaluated as follows:

$$\begin{aligned}\bar{P}_2^F &= \frac{e^{-\frac{d^\alpha \varepsilon}{\rho}}}{\rho} \int_0^\infty \left(e^{-\frac{d_1^\alpha \Psi_{\max}}{t}} + e^{-\frac{d_2^\alpha \Psi_{\max}}{t}} - e^{-\frac{(d_1^\alpha + d_2^\alpha) \Psi_{\max}}{t}} \right) d^\alpha e^{-\frac{d^\alpha t}{\rho}} dt \\ &= e^{-\frac{d^\alpha \varepsilon}{\rho}} \left[\sqrt{\frac{4\Psi_{\max} d^\alpha d_1^\alpha}{\rho}} K_1 \left(\sqrt{\frac{4\Psi_{\max} d^\alpha d_1^\alpha}{\rho}} \right) \right. \\ &\quad - \sqrt{\frac{4\Psi_{\max} d^\alpha (d_1^\alpha + d_2^\alpha)}{\rho}} K_1 \left(\sqrt{\frac{4\Psi_{\max} d^\alpha (d_1^\alpha + d_2^\alpha)}{\rho}} \right) \\ &\quad \left. + \sqrt{\frac{4\Psi_{\max} d^\alpha d_2^\alpha}{\rho}} K_1 \left(\sqrt{\frac{4\Psi_{\max} d^\alpha d_2^\alpha}{\rho}} \right) \right]. \quad (42)\end{aligned}$$

Substituting (42) into the outage probability $P_2^F = 1 - \bar{P}_2^F$, the first part of the theorem is proved.

When $z \rightarrow 0$, the Bessel function $zK_1(z)$ can be approximated by using series representation as follows [23, eq. (8.446)]:

$$\begin{aligned}zK_1(z) &= 1 + \sum_{k=0}^{\infty} \frac{(\frac{z}{2})^{2k+1}}{k! \Gamma(k+2)} \left(\ln \frac{z}{2} + C \right) \\ &\quad - \frac{1}{2} \sum_{l=0}^{\infty} \frac{(\frac{z}{2})^{2l+1}}{l!(n+l)!} \left(\sum_{k=1}^l \frac{1}{k} + \sum_{k=1}^{l+1} \frac{1}{k} \right) \\ &\approx 1 + \frac{z^2}{2} \ln \frac{z}{2}. \quad (43)\end{aligned}$$

When $z \rightarrow 0$, the exponential function e^{-z} can be approximated as follows:

$$e^{-z} \approx 1 - z. \quad (44)$$

By applying (43) and (44) into (15), P_2^F can be approximated at high SNR as follows:

$$\begin{aligned}P_2^F &\approx 1 - \left(1 - \frac{\varepsilon d^\alpha}{\rho}\right) \left[\left(1 + \frac{2\Psi_{\max} d^\alpha d_1^\alpha}{\rho} \ln \sqrt{\frac{\Psi_{\max} d^\alpha d_1^\alpha}{\rho}}\right) \right. \\ &\quad - \left(1 + \frac{2\Psi_{\max} d^\alpha (d_1^\alpha + d_2^\alpha)}{\rho} \ln \sqrt{\frac{\Psi_{\max} d^\alpha (d_1^\alpha + d_2^\alpha)}{\rho}}\right) \\ &\quad \left. + \left(1 + \frac{2\Psi_{\max} d^\alpha d_2^\alpha}{\rho} \ln \sqrt{\frac{\Psi_{\max} d^\alpha d_2^\alpha}{\rho}}\right) \right] \\ &\approx \frac{d^\alpha}{\rho} \left(\varepsilon - \Psi_{\max} d_1^\alpha \ln \frac{d_1^\alpha}{d_1^\alpha + d_2^\alpha} - \Psi_{\max} d_2^\alpha \ln \frac{d_2^\alpha}{d_1^\alpha + d_2^\alpha} \right). \quad (45)\end{aligned}$$

Therefore, the second part of the theorem is also proved. The proof for the theorem is complete.

APPENDIX B

PROOF OF THEOREM 2

Based on (9) and (13), the coverage probability of U_2 in (31) can be further expressed as follows:

$$\begin{aligned}\bar{P}_2^{C,I} &= \Pr\left\{\frac{1}{2}\log_2(1 + \alpha_2\rho_R|h_2|^2) \geq R_2^*, \rho_R > 0, |h_1|^2 > \frac{\varepsilon_1}{\rho_R}\right\} \\ &= \Pr\left\{\frac{\eta(\rho|h|^2 - \varepsilon)|h_1|^2 - \varepsilon_1}{|h_1|^2(1 + \varepsilon_1)}|h_2|^2 \geq \varepsilon_2, |h|^2 > \frac{\varepsilon}{\rho}, \right. \\ &\quad \left. |h_1|^2 > \frac{\varepsilon_1}{\eta(\rho|h|^2 - \varepsilon)}\right\}.\end{aligned}\quad (46)$$

Recall that the users' channel gains are ordered as $|h_1|^2 \leq |h_2|^2$, the above coverage probability $\bar{P}_2^{C,I}$ can be further rewritten as follows:

$$\begin{aligned}\bar{P}_2^{C,I} &= \Pr\left\{|h_2|^2 \geq |h_1|^2, |h|^2 > \frac{\varepsilon}{\rho}, |h_1|^2 > \frac{\varepsilon_1 + \varepsilon_2(1 + \varepsilon_1)}{\eta(\rho|h|^2 - \varepsilon)}\right\} \\ &\quad + \Pr\left\{|h_2|^2 \geq \frac{\varepsilon_2(1 + \varepsilon_1)|h_1|^2}{\eta(\rho|h|^2 - \varepsilon)|h_1|^2 - \varepsilon_1}, |h|^2 > \frac{\varepsilon}{\rho}, \right. \\ &\quad \left. \frac{\varepsilon_1}{\eta(\rho|h|^2 - \varepsilon)} < |h_1|^2 < \frac{\varepsilon_1 + \varepsilon_2(1 + \varepsilon_1)}{\eta(\rho|h|^2 - \varepsilon)}\right\}.\end{aligned}\quad (47)$$

Note that the joint probability density function (PDF) of $|h_1|^2$ and $|h_2|^2$ is given by [25]

$$f_{|h_1|^2, |h_2|^2}(x, y) = \sum_{i_1, i_2 \in \{1, 2\}} d_{i_1}^\alpha e^{-d_{i_1}^\alpha x} d_{i_2}^\alpha e^{-d_{i_2}^\alpha y}, \quad (48)$$

where $0 < x < y$.

Denote the first factor in $\bar{P}_2^{C,I}$ in (47) as Q_1 , which can be evaluated by applying (48) as follows:

$$\begin{aligned}Q_1 &= \sum_{i_1, i_2 \in \{1, 2\}} d_{i_1}^\alpha d_{i_2}^\alpha \int_{\frac{\varepsilon}{\rho}}^\infty \int_{\frac{\varepsilon_1 + \varepsilon_2(1 + \varepsilon_1)}{\eta(\rho z - \varepsilon)}}^\infty \int_x^\infty e^{-d_{i_2}^\alpha y} dy \\ &\quad \times e^{-d_{i_1}^\alpha x} dx e^{-d_{i_2}^\alpha z} dz \\ &= \sum_{i_1, i_2 \in \{1, 2\}} \frac{d_{i_1}^\alpha d_{i_2}^\alpha}{d_{i_1}^\alpha + d_{i_2}^\alpha} \int_{\frac{\varepsilon}{\rho}}^\infty e^{-(d_{i_1}^\alpha + d_{i_2}^\alpha) \frac{\varepsilon_1 + \varepsilon_2(1 + \varepsilon_1)}{\eta(\rho z - \varepsilon)}} e^{-d_{i_2}^\alpha z} dz \\ &= \sum_{i_1, i_2 \in \{1, 2\}} \frac{d_{i_1}^\alpha e^{-\frac{d_{i_1}^\alpha \varepsilon}{\rho}}}{d_{i_1}^\alpha + d_{i_2}^\alpha} \sqrt{\frac{4d_{i_1}^\alpha(d_{i_1}^\alpha + d_{i_2}^\alpha)(\varepsilon_1 + \varepsilon_2(1 + \varepsilon_1))}{\eta\rho}} \\ &\quad \times K_1\left(\sqrt{\frac{4d_{i_1}^\alpha(d_{i_1}^\alpha + d_{i_2}^\alpha)(\varepsilon_1 + \varepsilon_2(1 + \varepsilon_1))}{\eta\rho}}\right) \\ &= e^{-\frac{d_{i_1}^\alpha \varepsilon}{\rho}} \sqrt{\frac{4d_{i_1}^\alpha(d_{i_1}^\alpha + d_{i_2}^\alpha)(\varepsilon_1 + \varepsilon_2(1 + \varepsilon_1))}{\eta\rho}} \\ &\quad \times K_1\left(\sqrt{\frac{4d_{i_1}^\alpha(d_{i_1}^\alpha + d_{i_2}^\alpha)(\varepsilon_1 + \varepsilon_2(1 + \varepsilon_1))}{\eta\rho}}\right).\end{aligned}\quad (49)$$

Denote the second factor in $\bar{P}_2^{C,I}$ in (47) as Q_2 , which can be evaluated by applying (48) as follows:

$$\begin{aligned}Q_2 &= \sum_{i_1, i_2 \in \{1, 2\}} \int_{\frac{\varepsilon}{\rho}}^\infty \int_{\frac{\varepsilon_1}{\eta(\rho z - \varepsilon)}}^\infty \int_{\frac{\varepsilon_2(1 + \varepsilon_1)x}{\eta(\rho z - \varepsilon)x - \varepsilon_1}}^\infty d_{i_2}^\alpha e^{-d_{i_2}^\alpha y} dy \\ &\quad \times d_{i_1}^\alpha e^{-d_{i_1}^\alpha x} dx d_{i_2}^\alpha e^{-d_{i_2}^\alpha z} dz.\end{aligned}\quad (50)$$

Let $t = \rho z - \varepsilon$ and $s = \eta(\rho z - \varepsilon)x - \varepsilon_1$, Q_2 in (50) can be rewritten as follows:

$$\begin{aligned}Q_2 &= \sum_{i_1, i_2 \in \{1, 2\}} d_{i_1}^\alpha \int_{\frac{\varepsilon}{\rho}}^\infty \int_{\frac{\varepsilon_1}{\eta(\rho z - \varepsilon)}}^\infty e^{-\frac{d_{i_2}^\alpha \varepsilon_2(1 + \varepsilon_1)x}{\eta(\rho z - \varepsilon)x - \varepsilon_1} - d_{i_1}^\alpha x} dx \\ &\quad \times d_{i_1}^\alpha e^{-d_{i_1}^\alpha z} dz \\ &= \sum_{i_1, i_2 \in \{1, 2\}} \frac{d_{i_1}^\alpha d_{i_2}^\alpha e^{-\frac{d_{i_1}^\alpha \varepsilon}{\rho}}}{\eta\rho} \int_0^{\varepsilon_2(1 + \varepsilon_1)} \\ &\quad \times \underbrace{\int_0^\infty \frac{\exp\left(-\frac{d_{i_2}^\alpha \varepsilon_2(1 + \varepsilon_1)(s + \varepsilon_1) + d_{i_1}^\alpha s(s + \varepsilon_1)}{\eta s t} - \frac{d_{i_1}^\alpha t}{\rho}\right) dt}{t}}_{Q_3} ds.\end{aligned}\quad (51)$$

By applying $K_v(z) = \frac{1}{2}\left(\frac{z}{2}\right)^v \int_0^\infty \frac{\exp(-t - z^2/(4t))}{t^{v+1}} dt$ in [23, eq. (8.447)], the above integral Q_3 can be evaluated as follows:

$$Q_3 = 2K_0\left(2\sqrt{\frac{d_{i_2}^\alpha \varepsilon_2(1 + \varepsilon_1)(s + \varepsilon_1) + d_{i_1}^\alpha s(s + \varepsilon_1)}{\eta\rho s}}\right).\quad (52)$$

Substituting (49), (51) and (52) into (47), and using the fact that $P_2^{C,I} = 1 - \bar{P}_2^{C,I}$, the first part of the theorem is proved.

The Gaussian-Chebyshev quadrature [26] is applied to approximate the integral $\int_0^{\varepsilon_2(1 + \varepsilon_1)} K_0\left(2\sqrt{\frac{g_{i_1, i_2}(s)}{\rho}}\right) ds$ in (32) as follows:

$$\begin{aligned}&\int_0^{\varepsilon_2(1 + \varepsilon_1)} K_0\left(2\sqrt{\frac{g_{i_1, i_2}(s)}{\rho}}\right) ds \\ &\approx \frac{\pi \varepsilon_2(1 + \varepsilon_1)}{2n} \sum_{i=1}^n \left|\sin \frac{2i-1}{2n}\pi\right| K_0\left(2\sqrt{\frac{g_{i_1, i_2}(s_i)}{\rho}}\right),\end{aligned}\quad (53)$$

where $s_i = \frac{\varepsilon_2(1 + \varepsilon_1)}{2}(1 + \cos \frac{2i-1}{2n}\pi)$, and n is a complexity-accuracy tradeoff parameter.

Recall that the series representation of Bessel function $K_0(z)$ can be expressed as follows [23, eq. (8.447)]:

$$\begin{aligned}K_0(z) &= -\ln\left(\frac{z}{2}\right) \sum_{k=0}^\infty \frac{\left(\frac{z}{2}\right)^{2k}}{(k!)^2} + \sum_{k=0}^\infty \frac{z^{2k} \Psi(k+1)}{2^{2k} (k!)^2} \\ &\approx -\ln\left(\frac{z}{2}\right).\end{aligned}\quad (54)$$

Based on (44), (53) and (54), Q_2 in (51) can be approximated as follows:

$$\begin{aligned}Q_2 &= \sum_{i_1, i_2 \in \{1, 2\}} \frac{2d_{i_1}^\alpha e^{-\frac{d_{i_1}^\alpha \varepsilon}{\rho}}}{\eta\rho} \int_0^{\varepsilon_2(1 + \varepsilon_1)} K_0\left(2\sqrt{\frac{g_{i_1, i_2}(s)}{\rho}}\right) ds \\ &\approx - \sum_{i_1, i_2 \in \{1, 2\}} \frac{d_{i_1}^\alpha (1 - \frac{d_{i_1}^\alpha \varepsilon}{\rho})}{\eta\rho} \frac{\pi \varepsilon_2(1 + \varepsilon_1)}{2n} \\ &\quad \times \sum_{i=1}^n \left|\sin \frac{2i-1}{2n}\pi\right| \ln \frac{g_{i_1, i_2}(s_i)}{\rho} \\ &\approx \sum_{i_1, i_2 \in \{1, 2\}} \frac{\pi d_{i_1}^\alpha \varepsilon_2(1 + \varepsilon_1)}{2\eta n} \sum_{i=1}^n \left|\sin \frac{2i-1}{2n}\pi\right| \frac{\ln \rho}{\rho}.\end{aligned}\quad (55)$$

When $\rho \rightarrow \infty$, Q_1 in (49) can be approximated as follows:

$$Q_1 \approx 1 - \frac{\tau}{4\rho} \ln \frac{4\rho}{\tau}. \quad (56)$$

According to (55) and (56), the outage probability of U_2 at high SNR can be approximated as follows:

$$\begin{aligned} P_2^{C,I} &= 1 - Q_1 - Q_2 \\ &\approx \frac{\tau}{4\rho} \ln \frac{4\rho}{\tau} - \sum_{i_1, i_2 \in \{1,2\}} \frac{\pi d_{i_1}^\alpha \varepsilon_2 (1 + \varepsilon_1)}{2\eta n} \\ &\quad \times \sum_{i=1}^n \left| \sin \frac{2i-1}{2n} \pi \right| \frac{\ln \rho}{\rho} \\ &\approx \frac{\ln \rho}{\rho}. \end{aligned} \quad (57)$$

Therefore, the second part of the theorem is proved, and the proof is complete.

APPENDIX C

PROOF OF THEOREM 3

Based on (9), (22) and (35), the coverage probability of U_1 can be expressed as follows:

$$\begin{aligned} \bar{P}_1^{C,II} &= \Pr \left\{ \underbrace{\frac{1}{2} \log_2 \left(1 + \frac{\alpha_1 \rho_R |h_1|^2}{\alpha_2 \rho_R |h_1|^2 + 1} \right) \geq R_1^*, \rho_R > \rho_{R,2} > 0}_{Q_4} \right\} \\ &\quad + \Pr \left\{ \underbrace{\frac{1}{2} \log_2 (1 + \rho_R |h_1|^2) \geq R_1^*, \rho_R > 0, \rho_{R,2} = 0}_{Q_5} \right\}. \end{aligned} \quad (58)$$

The first factor in (58), Q_4 , can be expressed as follows:

$$\begin{aligned} Q_4 &= \Pr \left\{ 1 + \rho_R |h_1|^2 > (\varepsilon_1 + 1)(1 + \alpha_2 \rho_R |h_1|^2), \right. \\ &\quad \left. \rho_R > \rho_{R,2} > 0 \right\} \\ &= \Pr \left\{ \frac{\sqrt{1 + \rho_{R,2} |h_2|^2} - 1}{|h_2|^2} < \frac{\rho_R |h_1|^2 - \varepsilon_1}{(\varepsilon_1 + 1) |h_1|^2}, \right. \\ &\quad \left. \rho_R > \rho_{R,2} > 0, |h_1|^2 > \frac{\varepsilon_1}{\rho_R} \right\} \\ &= \Pr \left\{ |h_2|^2 > H(|h_1|^2), \rho_R > \rho_{R,2} > 0, |h_1|^2 > \frac{\varepsilon_1}{\rho_R} \right\}, \end{aligned} \quad (59)$$

where $H(|h_1|^2) = \frac{\rho_{R,2} - 2g(|h_1|^2)}{g^2(|h_1|^2)}$, and $g(|h_1|^2) = \frac{\rho_R |h_1|^2 - \varepsilon_1}{(\varepsilon_1 + 1) |h_1|^2}$.

Recall that the users' channel gains have been ordered as $|h_1|^2 \leq |h_2|^2$. Therefore, Q_4 in (59) can be further expressed as follows:

$$\begin{aligned} Q_4 &= \Pr \left\{ \underbrace{|h_2|^2 > |h_1|^2 > K(\rho_{R,2}, \rho_R)}_{Q_{41}} \right\} \\ &\quad + \Pr \left\{ \underbrace{|h_2|^2 > H(|h_1|^2), \frac{\varepsilon_1}{\rho_R} < |h_1|^2 < K(\rho_{R,2}, \rho_R)}_{Q_{42}} \right\}, \end{aligned} \quad (60)$$

where $K(\rho_{R,2}, \rho_R) = \frac{\rho_{R,2}(\varepsilon_1 + 1)^2 - 2\rho_R + \sqrt{\Delta(\rho_{R,2}, \rho_R)}}{2\rho_R^2}$, $\Delta(\rho_{R,2}, \rho_R) = (\rho_{R,2}(\varepsilon_1 + 1)^2 - 2\rho_R)^2 + 4\rho_R^2(\varepsilon_1^2 + 2\varepsilon_1)$.

Based on (48), the first factor in (60), Q_{41} , can be calculated as follows:

$$\begin{aligned} Q_{41} &= \sum_{i_1, i_2 \in \{1,2\}} \int_{\frac{\varepsilon_2}{\rho}}^{\infty} \int_{\frac{\varepsilon_1}{\rho_R}}^{\infty} \int_x^{\infty} d_{i_2}^\alpha e^{-d_{i_2}^\alpha y} dy \\ &\quad \times d_{i_1}^\alpha e^{-d_{i_1}^\alpha x} dx d^\alpha e^{-d^\alpha z} dz \\ &= \sum_{i_1, i_2 \in \{1,2\}} \frac{d_{i_1}^\alpha d_{i_2}^\alpha}{d_{i_1}^\alpha + d_{i_2}^\alpha} \int_{\frac{\varepsilon_2}{\rho}}^{\infty} e^{-(d_{i_1}^\alpha + d_{i_2}^\alpha)K(\rho_{R,2}, \rho_R) - d^\alpha z} dz \\ &= d^\alpha \int_{\frac{\varepsilon_2}{\rho}}^{\infty} e^{-(d_1^\alpha + d_2^\alpha)K(\rho_{R,2}, \rho_R) - d^\alpha z} dz. \end{aligned} \quad (61)$$

The second factor in (60), Q_{42} , can be calculated by applying (48) as follows:

$$\begin{aligned} Q_{42} &= \sum_{i_1, i_2 \in \{1,2\}} \int_{\frac{\varepsilon_2}{\rho}}^{\infty} \int_{\frac{\varepsilon_1}{\rho_R}}^{\infty} \int_{H(x)}^{\infty} d_{i_2}^\alpha e^{-d_{i_2}^\alpha y} dy \\ &\quad \times d_{i_1}^\alpha e^{-d_{i_1}^\alpha x} dx d^\alpha e^{-d^\alpha z} dz \\ &= \sum_{i_1, i_2 \in \{1,2\}} d_{i_1}^\alpha \int_{\frac{\varepsilon_2}{\rho}}^{\infty} \int_{\frac{\varepsilon_1}{\rho_R}}^{\infty} e^{-d_{i_2}^\alpha H(x) - d_{i_1}^\alpha x} dx \\ &\quad \times d^\alpha e^{-d^\alpha z} dz. \end{aligned} \quad (62)$$

The second factor in (58), Q_5 , can be evaluated as follows:

$$\begin{aligned} Q_5 &= \left\{ \frac{1}{2} \log_2 (1 + \rho_R |h_1|^2) \geq R_1^*, \rho_R > 0, \rho_{R,2} = 0 \right\} \\ &= \left\{ |h_1|^2 > \frac{\varepsilon_1}{\eta(\rho |h|^2 - \varepsilon)}, \frac{\varepsilon}{\rho} < |h|^2 < \frac{\varepsilon_2}{\rho} \right\} \\ &= \int_{\frac{\varepsilon}{\rho}}^{\frac{\varepsilon_2}{\rho}} e^{-\frac{(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta(\rho z - \varepsilon)}} d^\alpha e^{-d^\alpha z} dz \\ &= \int_{\frac{\varepsilon}{\rho}}^{\infty} e^{-\frac{(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta(\rho z - \varepsilon)}} d^\alpha e^{-d^\alpha z} dz \\ &\quad - \int_{\frac{\varepsilon_2}{\rho}}^{\infty} e^{-\frac{(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta(\rho z - \varepsilon)}} d^\alpha e^{-d^\alpha z} dz. \end{aligned} \quad (63)$$

Similar to (49), the first integral in (63) can be obtained as follows:

$$\begin{aligned} &\int_{\frac{\varepsilon}{\rho}}^{\infty} e^{-\frac{(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta(\rho z - \varepsilon)}} d^\alpha e^{-d^\alpha z} dz \\ &= e^{-\frac{d^\alpha \varepsilon}{\rho}} \sqrt{\frac{4d^\alpha (d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta \rho}} \mathbf{K}_1 \left(\sqrt{\frac{4d^\alpha (d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta \rho}} \right). \end{aligned} \quad (64)$$

Substituting (61)-(63), and (64) into (58), and using the fact that $\bar{P}_1^{C,II} = 1 - \bar{P}_1^{C,II}$, the first part of the theorem is proved.

Note that $\Delta(\rho_{R,2}, \rho_R)$ in $K(\rho_{R,2}, \rho_R)$ can be upper bounded as follows:

$$\begin{aligned} \Delta(\rho_{R,2}, \rho_R) &= (\rho_{R,2}(\varepsilon_1 + 1)^2 - 2\rho_R)^2 + 4\rho_R^2(\varepsilon_1^2 + 2\varepsilon_1) \\ &= (\varepsilon_1 + 1)^4 \left(\rho_{R,2}^2 - \frac{4\rho_{R,2}\rho_R}{(\varepsilon_1 + 1)^2} + \frac{4\rho_R^2}{(\varepsilon_1 + 1)^2} \right) \\ &< (\varepsilon_1 + 1)^4 (\rho_{R,2} + \rho_R)^2. \end{aligned} \quad (65)$$

Therefore, $K(\rho_{R,2}, \rho_R)$ can be upper bounded by applying (65) as follows:

$$\begin{aligned} K(\rho_{R,2}, \rho_R) &= \frac{\rho_{R,2}(\varepsilon_1 + 1)^2 - 2\rho_R + \sqrt{\Delta(\rho_{R,2}, \rho_R)}}{2\rho_R^2} \\ &< \frac{\rho_{R,2}(\varepsilon_1 + 1)^2 - 2\rho_R + (\varepsilon_1 + 1)^2(\rho_{R,2} + \rho_R)}{2\rho_R^2} \\ &< \frac{3(\varepsilon_1 + 1)^2}{2\rho_R} < \frac{c_1}{\rho_{R,2}}, \end{aligned} \quad (66)$$

where $c_1 = \frac{3(\varepsilon_1 + 1)^2}{2}$.

Based on (66), Q_{41} in (61) can be lower bounded as follows:

$$\begin{aligned} Q_{41} &= d^\alpha \int_{\frac{\varepsilon_2}{\rho}}^{\infty} e^{-(d_1^\alpha + d_2^\alpha)K(\rho_{R,2}, \rho_R) - d^\alpha z} dz \\ &\geq d^\alpha \int_{\frac{\varepsilon_2}{\rho}}^{\infty} e^{-\frac{(d_1^\alpha + d_2^\alpha)c_1}{\eta(\rho z - \varepsilon_2)} - d^\alpha z} dz \\ &= e^{-\frac{d^\alpha \varepsilon_2}{\rho}} \sqrt{\frac{4d^\alpha(d_1^\alpha + d_2^\alpha)c_1\varepsilon_1}{\eta\rho}} \mathbf{K}_1 \left(\sqrt{\frac{4d^\alpha(d_1^\alpha + d_2^\alpha)c_1\varepsilon_1}{\eta\rho}} \right) \\ &\approx \left(1 - \frac{d^\alpha \varepsilon_2}{\rho}\right) \left(1 + \frac{d^\alpha(d_1^\alpha + d_2^\alpha)c_1\varepsilon_1}{\eta\rho} \ln \frac{d^\alpha(d_1^\alpha + d_2^\alpha)c_1\varepsilon_1}{\eta\rho}\right) \\ &\approx 1 - \frac{\ln \rho}{\rho}. \end{aligned} \quad (67)$$

Since $e^{-(d_1^\alpha + d_2^\alpha)\kappa_1} \leq 1$, Q_{41} in (61) can be upper bounded as follows:

$$\begin{aligned} Q_{41} &= d^\alpha \int_{\frac{\varepsilon_2}{\rho}}^{\infty} e^{-(d_1^\alpha + d_2^\alpha)K(\rho_{R,2}, \rho_R) - d^\alpha z} dz \\ &\leq d^\alpha \int_{\frac{\varepsilon_2}{\rho}}^{\infty} e^{-d^\alpha z} dz \\ &= e^{-\frac{d^\alpha \varepsilon_2}{\rho}} \approx 1 - \frac{1}{\rho}. \end{aligned} \quad (68)$$

Since $e^{-d_{i_2}^\alpha H(x)} \leq 1$, Q_{42} in (62) can be upper bounded as follows:

$$\begin{aligned} Q_{42} &\leq \sum_{i_1, i_2 \in \{1, 2\}} d_{i_1}^\alpha \int_{\frac{\varepsilon_2}{\rho}}^{\infty} \int_{\frac{\varepsilon_1}{\rho_R}}^{\kappa_1} e^{-d_{i_1}^\alpha x} dx d^\alpha e^{-d^\alpha z} dz \\ &= \sum_{i_1, i_2 \in \{1, 2\}} \int_{\frac{\varepsilon_2}{\rho}}^{\infty} \left(e^{-d_{i_1}^\alpha \frac{\varepsilon_1}{\rho_R}} - e^{-d_{i_1}^\alpha K(\rho_{R,2}, \rho_R)} \right) d^\alpha e^{-d^\alpha z} dz. \end{aligned} \quad (69)$$

Based on (67) and (68), Q_{42} can be further bounded as follows:

$$0 < Q_{42} < \frac{\ln \rho}{\rho} - \frac{1}{\rho}. \quad (70)$$

Similar to (67), $e^{-\frac{d^\alpha \varepsilon_2}{\rho}} \sqrt{\frac{4d^\alpha(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta\rho}} \mathbf{K}_1 \left(\sqrt{\frac{4d^\alpha(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta\rho}} \right)$ in Q_5 can be approximated as follows:

$$\begin{aligned} &e^{-\frac{d^\alpha \varepsilon_2}{\rho}} \sqrt{\frac{4d^\alpha(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta\rho}} \mathbf{K}_1 \left(\sqrt{\frac{4d^\alpha(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta\rho}} \right) \\ &\approx 1 - \frac{\ln \rho}{\rho}. \end{aligned} \quad (71)$$

Similar to Q_{41} , $\int_{\frac{\varepsilon_2}{\rho}}^{\infty} e^{-\frac{(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta(\rho z - \varepsilon)}} d^\alpha e^{-d^\alpha z} dz$ in Q_5 can be bounded as follows:

$$1 - \frac{\ln \rho}{\rho} < \int_{\frac{\varepsilon_2}{\rho}}^{\infty} e^{-\frac{(d_1^\alpha + d_2^\alpha)\varepsilon_1}{\eta(\rho z - \varepsilon)}} d^\alpha e^{-d^\alpha z} dz < 1 - \frac{1}{\rho}. \quad (72)$$

Combining (67), (68), (70), (71) with (72), and noting that $P_1^{C,II} = 1 - Q_{41} - Q_{42} - Q_5$, we have

$$P_1^{C,II} \approx \frac{\ln \rho}{\rho}. \quad (73)$$

Therefore, the second part of the theorem is proved, and the proof is complete.

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