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Natural Language Statistical Features of LSTM-generated Texts

Marco Lippi*, Marcelo A Montemurro*, Mirko Degli Esposti, and Giampaolo Cristadoro

Abstract—Long Short-Term Memory (LSTM) networks have recently shown remarkable performance in several tasks dealing with natural language generation, such as image captioning or poetry composition. Yet, only few works have analyzed text generated by LSTMs in order to quantitatively evaluate to which extent such artificial texts resemble those generated by humans. We compared the statistical structure of LSTM-generated language to that of written natural language, and to those produced by Markov models of various orders. In particular, we characterized the statistical structure of language by assessing word-frequency statistics, long-range correlations, and entropy measures. Our main finding is that while both LSTM and Markov-generated texts can exhibit features similar to real ones in their word-frequency statistics and entropy measures, LSTM-texts are shown to reproduce long-range correlations at scales comparable to those found in natural language. Moreover, for LSTM networks a temperature-like parameter controlling the generation process shows an optimal value—for which the produced texts are closest to real language consistent across all the different statistical features investigated.

Index Terms—Long Short-Term Memory Networks, Natural Language Generation, Long-Range Correlations, Entropy, Authorship Attribution.

I. INTRODUCTION

Building artificial systems capable of mimicking human creativity has long been one of the aims of Artificial Intelligence (AI) [1]. In this work, we focus on the problem of Natural Language Generation (NLG), which encompasses the capability of machines to synthesize text in a way that resembles spoken or written language typically employed by humans [2]. This research field has recently known a period of great excitement, mostly due to the huge development in the area of deep learning [3], whose methods and algorithms have certainly contributed to move significant steps forward.

Deep learning techniques have in fact produced stunning results in a variety of different research fields and application domains, and one of the major successes has been that of generative models [4]. In the area of NLG, many studies have been dedicated to specific, focused applications, such as image and video captioning [5], [6], poem synthesis [7], or lyric generation [8]. In all these cases, the considered generated texts are relatively short (captions, poems, lyrics) and correlations between words rarely span across several sentences. The scenario totally changes when we consider longer texts, such as novels. Natural language has been widely studied within this context, and notoriously it shows statistical properties in the distribution of terms, as well as long-range correlations between words [9], [10], [11]. In comparison to short texts such as captions, this is a much more challenging setting to imitate for machines.

In this work, we aim to provide an extensive empirical evaluation of texts generated with Long-Short Term Memory (LSTM) networks, one of the most widely used deep learning models for NLG. Our goal is to quantitatively assess whether LSTM texts do share some similarities with natural language that is commonly produced by humans. To this aim, we trained an LSTM network with a corpus that consists of a collection of novels by Charles Dickens. Such network is trained to predict the next character of a given text, and thus it can be employed to iteratively generate a document of any desired length. The setting was adopted in several works (e.g., see [12] and citations therein).

In our experimental framework we evaluated several different aspects of machine-generated texts, comparing them against the statistics of real language and Markov-generated samples. First, we analyzed fundamental linguistic properties typically shown by texts, such as Zipf’s [13] and Heaps’ [14] laws for words. Second, we studied whether the generated texts presented long-range correlations, which are commonly encountered in human-generated texts, but difficult to reproduce for machines. As a third point, we compared the entropy of the generated texts with the one of the original corpus. We then moved our analysis to a higher level, by carrying out a preliminary study looking at characteristics dealing with the style and quality of the generated texts: in particular, we analyzed the degree of creativity and plagiarism of the artificial texts with respect to the dataset on which the LSTM was trained, by looking at longest common subsequences. We also assessed whether an authorship attribution algorithm would capture some analogy between the generated text and the original one, in terms of author’s style.

Surprisingly, very few studies have been dedicated to a thorough analysis and to a quantitative evaluation of the similarities between texts created by machines and texts created by humans. Karpathy et al. [12] also provide an experimental analysis of LSTM networks trained for character-by-character text generation, but they focused their study on a qualitative evaluation of the cell activations within the neural architecture: for example, they looked for open and closed parentheses or quotes, that typically span a few tens or hundreds of characters.

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Their claim that the LSTM model is capable of capturing long-range dependencies is thus only supported by such qualitative evidence, without giving a deep insight in the characteristics of the generated documents. Lin and Tegmark [15] compared natural language texts with those generated by Markov models and LSTMs, exploiting metrics coming from information theory. Their analysis shows that LSTMs are capable of capturing correlations that Markov models instead fail to represent, yet the range of correlations they consider is still quite limited (up to 1,000 characters). Conversely, Takahashi and Tanaka-Ishii [16] reported that LSTM language models have limitation in reproducing such long-range correlations if measured with a method based on clustering properties of rare words; note however that their analysis is still limited to a range of $\sim 1,000$ words, and the corpus they employ for training is much smaller than the one used in our experiments. Ghodsi and DeNero [17] instead, analyzed some statistical properties of text generated by a Recurrent Neural Network Language Model (RNNLM), in particular focusing on the length of sentences, the vocabulary distribution, and the distribution of specific grammatical elements, such as pronouns. In a complementary study, Lake and Baroni [18] focused on short-scale structures of the overall statistical properties of pseudo-texts. They showed that RNNs are able to exploit systematic compositionality, and thus also to reproduce, for example, some abstract grammatical generalizations.

The remainder of the paper is organized as follows. Section II will describe the LSTM model used in our experiments. Section III will present the statistical methods employed for the quantitative evaluation of the artificial text properties. Section IV will describe the corpora used to train our model, and Section V will report and discuss the experimental results. Section VI will finally conclude the paper, also pointing for future research directions.

II. LONG SHORT-TERM MEMORY NETWORKS

Long Short-Term Memory networks (LSTMs) are recurrent neural networks (RNNs) that have been first developed at the end of the 90s, achieving remarkable results in applications dealing with input sequences [19]. Such model was specifically designed to address the issue of vanishing gradients, that greatly limited the applicability of standard RNNs [20]. Within the “deep learning revolution” that Artificial Intelligence has been undergoing in the last decade, LSTMs have regained popularity, being now widely used in a huge number of research and industrial applications, including automatic machine translation, speech recognition, text-to-speech generation (e.g., see [21] and references therein).

A. General framework

RNNs allow to process sequences of arbitrary lengths, by exploiting $L$ hidden layers $h'_t$, with $t = \{1, \ldots, L\}$ whose cells are functions not only of the layer input $x_t$, but also of the hidden layer at the previous time step: $h'_t = f(x_t, h'_{t-1})$. RNNs are typically trained with Backpropagation Through Time (BPTT) [22], by unfolding the recurrent structure into a sort of temporal chain through which the gradient is propagated, up to a certain number $K$ of time steps. Unfortunately, this method suffers from the well-known problem of vanishing or exploding gradients [23], [20], which makes plain RNNs scarcely used in practice. LSTMs overcome this issue by exploiting a more complex hidden cell, namely a memory cell, and non-linear gating units, that control the information flows into and out of the cell.

Basically, the LSTM cells are capable of maintaining their state over time, of forgetting what they have learned, and also of allowing novel information in. An example of such a cell is depicted in Figure 1. The model is based on the concept of cell status at time $t$, namely $C_t$, which depends on three gates: an input gate $i_t$ that can let new information into the cell state, a forget gate that can modulate how much information is forgotten from the previous state, and an output gate $o_t$ that controls how much information is transferred to the upper layers. The following equations describe the behaviour of an LSTM layer (we drop the layer index $\ell$ in order to simplify the notation):

\begin{align}
    f_t &= \sigma_f(W_f x_t + U_f h_{t-1} + b_f) \\
    i_t &= \sigma_i(W_i x_t + U_i h_{t-1} + b_i) \\
    o_t &= \sigma_o(W_o x_t + U_o h_{t-1} + b_o) \\
    C_t &= f_t \odot C_{t-1} + i_t \odot \sigma_c(W_c x_t + U_c h_{t-1} + b_c) \\
    h_t &= o_t \odot \tanh(C_t)
\end{align}

where all $\sigma_f, \sigma_i, \sigma_o$ are typically the sigmoid function, $\sigma_c$ is typically the tanh function. The $h_t$ and $C_t$ recurrent connections allow the propagation of information through time.
B. LSTM for text generation

The most widely employed LSTM architecture for text generation is based on character-level sentence modeling. Basically, the input of the network consists in $M$ characters, that correspond to a fixed-size portion of text, whereas the number of output neurons is the total number $S$ of possible symbols in the text, each neuron corresponding to one of such characters. The output layer consists in a softmax layer, so that each symbol has an associated probability, and all such probabilities sum up to 1. A hard way of generating texts is to pick the character with the highest probability as the next one in the sequence, and to feed it back into the network input. A soft alternative (which is the one used in practice) allows to sample the next character in the sequence from the probability distribution of the output cells: in this way the output of the network is not deterministic, given the same initial input sequence. With such an iterated procedure, texts of any length can be generated. The hidden states of the cells keep track of the “memory” of the network, so as to exploit also information not directly encoded in the input any more. This generation phase can be controlled by a parameter $T$, usually named temperature. Different temperature values can be tuned in order to obtain a smoother or sharper softmax distribution from which characters are generated: in particular, the final softmax layer in the LSTM computes the probability of each symbol $j$ as follows:

$$P_j = \frac{\exp\left(\frac{y_j}{T}\right)}{\sum_{i=1}^{S} \exp\left(\frac{y_i}{T}\right)}$$  \hspace{1cm} (6)

where $y_i$ are the output values for each symbol that are fed to the softmax layer. Large values of $T$ lead towards a more uniform distribution of symbol probabilities, whereas when $T$ tends to zero, the distribution is more skewed towards the most probable symbol.

Such a model is trained in a classic supervised learning setting, where the input training corpus is fed to the network, using as target the true (known) next character, as it appears in the corpus. If the cell states are not reset as subsequent input windows are presented to the network, long-range dependencies can in principle be captured by the model.

Note that, in principle, the same task could be modeled at a word level, thus training the LSTM network to predict the next word in the text, rather than the next character. Although this solution may appear more appropriate way for modeling the problem, it has two main limitations: (i) the number of possible output classes of the network would become huge, being the total number of distinct words in the input corpus, leading to a much more difficult optimization problem, which would likely require a larger number of training examples; (ii) the set of possible output words would be limited to those appearing in the training corpus, which could be enough in many cases, but would limit the creativity of the network.

III. Methods

We now present the methods we employ in order to quantitatively evaluate the characteristics of the artificially generated texts with respect to the original, human-generated texts.

A. Zipf’s and Heaps’ laws for words

Natural languages show remarkable statistical properties in their word statistics. The two best known examples are Zipf’s [13] and Heaps’ [14] laws in language, which refer to universal features related to word frequencies.

Zipf’s law states that if the word frequencies of any sufficiently long text are arranged in decreasing order, there is a power-law relationship between the frequency and the corresponding ranking order of each word. More explicitly, if we denote the rank of a word by $r$, the Zipf’s law states the following relationship between the rank and the frequency of a word at that rank position $f(r)$, as follows:

$$f(r) = Ar^{-\beta}.$$  \hspace{1cm} (7)

This relationship is roughly the same for all human languages, the exponent $\beta$ taking values close to 1.

Heaps’ law states that the number of the different words (i.e the size of the vocabulary) after seeing $t$ consecutive words in a text, obeys approximately the following relationship:

$$n(t) = Bt^\nu$$  \hspace{1cm} (8)

with exponent $\nu$ typically taking values smaller than 1 [26].

B. Long-Range Correlations

Linguistic laws on the scaling of words frequencies, like Zipf’s and Heaps’, do not reveal any statistical structure that depends directly on word order. Zipf’s rank-frequency distribution would be unaltered after a random shuffling of all words in text, and similarly for the average behaviour predicted by Heaps’ law. Statistical measures that capture structure at the sequence level in texts involve correlations and spectral analysis [27].

Correlations in language are known to be of the power-law type [9], [10], [11], decaying as $C(\tau) \propto \tau^{-\gamma}$, where $\tau$ is the distance between symbols – e.g. words or characters. It is possible to characterize the structure of long-range correlations using the method of Detrended Fluctuation Analysis (DFA) [28], [29]. The first step in the method involves the mapping of the symbol sequence onto a numerical time-series, by assigning a number to each basic symbol in the sequence. In order to preserve the maximum of structure from the text sources, we performed the mapping at character level— including all punctuation signs, numbers, capital letters, and accented forms. The procedure to assign a number to each character followed similar lines to the method employed in [10], where in the present case each character is replaced by its rank. Thus, the most frequent character is assigned the number 1, the second most frequent the number 2, and so on. For a sequence of length $N$, the character at position $t$ in the time series, with $t \in \mathbb{N}$, can be represented by the number $x(t)$, and the following random-walk can be constructed:

$$X(t) = \sum_{i=1}^{t} (x(i) - \langle x \rangle)$$  \hspace{1cm} (9)

where $\langle x \rangle$ represents the mean of the times series. The time series $X(t)$ is then split into windows of length $L$, and in each
of those windows the corresponding stretch of the series is fitted by a straight line by means of least squares. These linear fits represent the local trend within each of the windows of length $L$. The sequence of length-$L$ trends can be concatenated in a piecewise manner defining a piecewise linear function $Y_L(t)$. Then we compute the average fluctuations at scale $L$, that is the deviations from the trend, defined as follows:

$$F(L) = \left( \frac{1}{N} \sum_{t=1}^{N} (X(t) - Y_L(t))^2 \right)^{1/2}. \quad (10)$$

The nature of the correlations present in the original time series can be evaluated by observing the dependence of $F(L)$ on $L$. In particular, the growth of fluctuation with the scale $L$ will be given as $F(L) \sim L^\alpha$, with $0 < \alpha < 1$. In the case of an uncorrelated or short-range correlated time series $x_t$, we have $F(L) \sim L^{1/2}$. However, in the presence of long-range correlations of the power-law type in the original time series $x_t$, the fluctuation exponent $\alpha$ will differ from $1/2$ [29], with $\alpha > 1/2$ for persistent (positive) correlations and $\alpha < 1/2$ for anti-persistent (negative) correlations.

C. Entropy and KL-divergence estimation

The entropy of a symbolic sequence can be interpreted as a quantification of the degree of predictability in the sequence. A high level of predictability of consecutive values in a sequence implies a low level of surprise about future symbols, which is linked to a low entropy. On the other hand, a sequence with a high degree of randomness will be characterized by a high level of surprise in the identity of future symbols, and result in a high value for the entropy. Therefore, the determination of the entropy of language serves as a quantification of its degree of order. Early attempts to determine the entropy of language were based on the close link between entropy and predictability [30]. However, the estimation of the entropy from long sequences of written text, requires the estimation of block probabilities, which poses a serious computational challenge, due to the presence of long-range correlations in language. The required sample size needed for an accurate estimation of the block probabilities grows exponentially with the length of the block, thus quickly rendering insufficient any available amount of text. This difficulty can be overcome through the link between entropy and predictability mentioned above. The degree of predictability in a sequence determines how much it can be compressed by a lossless compression method. Sequences with high predictability can be compressed more than sequences with a higher degree of randomness. In particular, it can be shown that under general assumptions of stationarity and ergodicity, the entropy rate of a stochastic source is a lower bound to the length per symbol of any encoding of it [31]. Hence, the entropy of symbolic sequences can be estimated by means of efficient lossless compression algorithms [32], [33], [34]. We estimated the entropy of long character sequences using an implementation of the algorithm proposed by Lempel and Ziv [32], [35], [36], which relies on the estimation of redundancy by looking for matches between future and past substrings in a symbolic sequence. Implementations of entropy estimation algorithms based on these methods have proved to work well for symbolic sequences even in the presence of long range correlations as those found in language [34], [37].

The Kullback-Leibler (KL) divergence $D(P|Q)$ is a measure of relative entropy between two probability distributions $P$ and $Q$ [31]. When $P \equiv Q$ then the KL-divergence is zero, but it takes positive values when $P \neq Q$. It can be shown that the $D(P|Q)$ is a measure of the extra number of bits that are required to encode typical sequences with the distribution $P$, when using a code based on $Q$ [31]. This interpretation suggests that $D(P|Q)$ can also be estimated using compression algorithms in which one signal is compressed using past sequences in the second signal. More specifically, the KL divergence $D(P|Q)$ can be written as [31]

$$D(P|Q) = H_P(Q) - H(P) \quad (11)$$

where $H(P)$ is the entropy of the distribution $P$ and $H_P(Q)$ is the cross-entropy between $P$ and $Q$. Let us assume that two text sequences produced by the stochastic source with probability distribution $P$ are represented by $X = \{x_t\}_{t=1}^N$, and those produced by $Q$ as $Z = \{z_t\}_{t=1}^M$. Then, for notational succinctness let us write the information quantities explicitly in terms of the generated sequences, therefore representing the KL-divergence between $P$ and $Q$ as $D(X|Z)$. With this notation, we have $D(X|Z) = H_X(Z) - H(X)$. A compression-based algorithm proposed in [38] permits to compute the cross-entropy $H_X(Z)$ based on the symbolic sequences $X$ and $Z$. Then, the KL-divergence is obtained by subtracting the entropy of the sequence $X$ from the cross-entropy $H_X(Y)$. The KL divergence is a non-symmetric quantity and in order to have a distance-like measure between character sequences $X$ and $Y$, we defined a symmetrized divergence as $D_s(X,Y) = (D(X|Y) + D(Y|X))/2$.

Another measure that is strictly related to entropy, and that is widely used for the evaluation of artificial texts, is perplexity [39], which can be computed as the geometric mean of the inverse probability for each predicted word in the a document [40], [41], where probabilities are typically estimated on a language model trained on a larger corpus.

D. Creativity and Authorship Attribution

Providing a quantitative method able to address the creativity of a given algorithm for artificial texts generation is a complex task. In this paper we consider two distinct yet strictly intertwined aspects: we aim to measure at what extent the algorithm is capable of capturing the stylistic traits of a given author, while, at the same time, avoiding to perform just a plagiarism of the training corpus.

Measuring the Longest Common Subsequence (LCS) is one of the simplest way to implement the idea of quantitatively measuring plagiarism: given the $k$-th character $x_k$ of the artificial text, we denote by $L_k$ the length of the longest subsequence starting at $x_k$ that is also contained in (thus, plagiarized from) the training corpus. Different statistics of the set of all $L_k$ can be used to quantify how various algorithms are able to reproduce some stylist traits of a given corpus while generating innovative texts, not written before. Here we adopt...
the simplest one and consider the maximum over the whole artificial text: \( \hat{L} = \max_k L_k \) (see [42] and [43]).

We now move our analysis to a higher level, by exploring how artificial texts resemble the style of the training author. Stylistic traits are supposed to reflect subtle choices of the author in terms of vocabulary, syntactic constructions and structural composition, to mention a few. As such, a comprehensive quantification of the style of an author is out of reach. On the other hand, a very simple feature such as the frequency distribution of \( n \)-gram of letters has been successfully selected as a key ingredient in some of the most effective approaches to authorship attribution [44], [45].

We use one of the state-of-the-art algorithms to test the automatic attribution of the author of our artificial texts. The implemented method is in fact one of the two methods that have been successfully used for the attribution of Antonio Gramsci’s papers [44]. Essentially, each method defines a kind of similarity distance between texts. Let us very briefly describe just the first method used here, referring to [45] for further details. The method is based on (characters) \( n \)-grams and it is probably one of the simplest possible measures on a text: after a first experiment based on bigram frequencies presented in 1976 by Bennett [46], Kešelj et al [47] published in 2003 a paper in which \( n \)-gram frequencies were used to define a similarity distance between texts (see also [48]). The similarity distance was introduced and discussed in [44]: we call \( \omega \) an arbitrary \( n \)-gram, and we denote by \( f_X(\omega) \) and \( f_Y(\omega) \) the relative frequencies with which \( \omega \) occurs in text \( X \) and \( Y \). \( D_n(X) \) is the \( n \)-gram dictionary of text \( X \), that is, the set of all \( n \)-grams which have non-zero frequency in \( X \) (similarly for \( Y \)) and we define what we will call the \( n \)-gram distance between text \( X \) and text \( Y \) as

\[
d_n(X,Y) := \frac{1}{|Z|} \sum_{\omega \in D_n(X) \cup D_n(Y)} \left( \frac{f_X(\omega) - f_Y(\omega)}{f_X(\omega) + f_Y(\omega)} \right)^2
\]

(12)

where the denominator \(|Z| = |D_n(X)| + |D_n(Y)|\) is the sum of the number of different \( n \)-grams in the two dictionaries, respectively, while the inner sum is taken over all the different \( n \)-grams occurring in the two texts.

Suppose the goal is to decide whether a given document \( X \) has been authored by author \( A \) or not. The approach adopted in [44] consists in first collecting \( m \) documents from author \( A \) and \( m \) documents from an author \( B \) (or, in general, from more authors). The distance of the candidate text \( X \) to these documents is then used, with the help of a simple probabilistic method, to produce a similarity index \( I(X) \), \(-1 \leq I(X) \leq 1\) (see [44] for details on the method). Values of the index close to 1 (respectively, \(-1\)) reveal a very strong attribution to author \( A \) (respectively, \( B \)), while values close to 0 indicate a very weak attribution (see [44], [45] for more details).

IV. CORPORA

Our aim was to train an LSTM network on a large corpus obtained from a single author, which would then allow to perform the experiments on authorship attribution and to assess whether the model was capable of capturing some stylistic features of its “teacher”. We employed the works by Charles Dickens, since he was a very prolific author whose bibliography is freely available in plain text format at ProjectGutenberg[4]. We collected a total of eighteen works by Charles Dickens, which resulted in a corpus of over 24 millions characters.

For the authorship attribution experiments, we also collected a smaller corpus of texts, some still from Charles Dickens, and some others from a different author. Clearly, these additional texts from Dickens needed to be disjoint from those in the larger corpus, on which the LSTM network had to be trained. Regarding non-Dickens documents, we collected texts by Robert Louis Stevenson, who was also a prolific author of the XIX century[5]. For this second corpus, we collected 30 documents both for Dickens and for Stevenson, each consisting of 10,000 characters.

V. EXPERIMENTS

The experiments with LSTMs were run using the torc-rnn package[6]. We trained an LSTM network with two layers and 1,024 cells in each layer. As customary in text generation experiments with LSTMs[12], the training set was split into chunks of length equal to \( K \) characters: in this way, gradients in truncated backpropagation are propagated up to \( K \) steps back, but the status of each LSTM cell is not reset after each example, so that longer-range correlations can in principle be learnt. We used \( K = 100 \). To avoid overfitting, a dropout equal to 0.7 was applied, and a validation set (4\% of the whole corpus) was exploited to monitor the loss function during training.

In order to compare the statistics of the LSTM texts with that of other non-trivial models, we also generated artificial texts based on \( m \)-order Markov processes. In particular, a family of \( m \)-order Markov models were trained from the Dickens’ corpus, with \( m \) taking values 2, 4, 6, 8, 10, and 12. The models were used to generate artificial texts starting from a seed taking from the original corpus.

Tables I and II show some examples of texts generated with different temperatures from the LSTM, and by different Markov models, respectively.

A. Zipf’s and Heaps’ Laws

As a first test comparing the statistics of the LSTM-generated texts to other models capable of rendering stochastic

\[ \text{http://gutenberg.org} \]

1. We used the following works: A tale of two cities, David Copperfield, Oliver Twist, Bleak house, Great expectations, The life and adventures of Nicholas Nickleby, The old curiosity shop, The Pickwick papers, Dombey and son, Little Dorrit, Life and adventures of Martin Chuzzlewit, Our mutual friend, Barnaby Rudge, A Christmas Carol, The uncommercial traveller, Hard times, Letters, A child’s history of England.

2. We used excerpts from the following works: Signal-man, A Christmas tree, The poor relation’s story, The schoolboy’s story, Hunted down, Pictures from Italy, The chimes, The haunted man and the ghost’s bargain, Tom Tiddler’s ground, The wreck of the Golden Mary.

3. We used excerpts from the following works: Treasure island, The strange case of Doctor Jekyll and Mister Hyde, Kidnapped, The Black Arrow.

4. [https://github.com/jcjohnson/torch-rnn](https://github.com/jcjohnson/torch-rnn)
versions of texts, we looked and the distribution of words frequencies. We first evaluated the Zipf’s law, by measuring the relationship between the rank in the set of words, ordered by frequency, and word frequency itself. Figure 2A shows the rank-frequency distributions of words in the LSTM texts for temperatures in the range 0.1-3.0. The plot also shows in black the result for the original Dickens corpus. We fitted the value of the exponent within the region between ranks $10^2$ and $10^3$ to determine more clearly the behavior with temperature, which showed a clear power-law behaviour consistently across all but the two extreme temperatures. Figure 2B shows the resulting value of the Zipf’s exponent $\beta$ as a function of temperature in the range 0.3-2.0. LSTM texts generated with low temperatures have a frequency rank distribution which decays faster with rank. On the contrary, for higher temperatures the distribution flattens, showing a smaller exponent $\beta$. The dashed line in the figure shows the value of the exponent estimated from the Dickens’ corpus, which intercepts the LSTM results at a temperature between 0.8 and 0.9, approximately.

A similar analysis was performed on the Markov-generated texts. Figure 2C shows the rank-frequency distribution for texts generated with Markov models models of order 2, 4, 6, 8, 10, and 12. Interestingly, there is little variation of the behavior of the distribution as a function of the Markov order. This is also corroborated by the estimation of the exponent, presented in Figure 2D, which shows the exponent of the Markov texts with a value slightly below that of the original source.

In order to assess the validity of Heaps’ law for the artificial language, we computed the statistics of the vocabulary growth for the LSTM and Markov texts. Figure 2A shows the results for the LSTM texts for a range of temperatures from 0.1 to 3.0. For comparison, the curve for the original text is shown in black. Figure 2B represents the results of fitting the power-law behavior in the region for $t > 1000$, using the same range of temperatures shown for the $\beta$ exponent in Figure 2B. The dashed line, which represents results for the original text, cuts the LSTM data at a point between temperatures 0.7 and 0.8.
Fig. 2. Zipf’s law in LSTM and Markov-generated texts. A) Zipf’s rank-frequency distribution in LSTM texts, for temperatures in the range 0.1-3.0. B) Exponent $β$ measured in the region between ranks $10^2$ and $10^3$ of the Zipf’s distributions for LSTM texts as a function of the temperature. C) Zipf’s rank-frequency distribution for Markov-generated with orders 2 to 12. B) Exponent $β$ measured in the region between ranks $10^2$ and $10^3$ of the Zipf’s distributions for the Markov-generated texts as a function of model’s order. In panels B and D the dashed line corresponds to the exponent measured in the Dickens’ corpus.

B. Long-Range Correlations and entropy

Beyond the statistics of word frequencies, natural texts show correlations that span hundreds or thousands of characters, showing power-law decay. While a direct measure of these correlations is possible in principle, more efficient methods are based on spectral [27] or fluctuation [28], [29] properties of the sequences. In particular, we tested the LSTM generated texts using Detrended Fluctuation Analysis (DFA) [28], [29] applied to linguistic character sequences. By means of DFA it is possible to estimate such exponent $α$, by fitting a power law to the dependence of the fluctuations $F(L)$ with the scale $L$. We estimated the dependence of $F(L)$ with the scale $L$ for LSTM texts generated at different temperatures and for the Markov-generated texts for different orders. Figure 4A shows the normalised fluctuations $F_n(L)$ as a function of the scale $L$ for LSTM-generated texts together with the results for the original Dickens’ corpus and a shuffled realisation of it. In all cases there are signs of power-law behavior for a wide range of scales, with the exception of the two extreme temperatures $T = 0.1$ and $T = 3.0$. Although the data corresponding to the shuffled text seems to have a less steep slope than the LSTM samples, a more quantitative analysis is required to compare the extent of correlations. In Figure 4B we show the estimations of the exponent $α$ obtained by fitting a power-law to the data in panel A in the region spanned by scales $L = 10^2 \ldots 10^4$. For comparison, the full black line corresponds to the result for the original Dickens’ text while the dashed line is the result obtained from the shuffled text. The full black circles are the averaged of the estimation of the exponent from the 10 available samples, and as small squares the figure shows the result for each sample. It is in the region between of temperatures between 0.5 and 1.0 that the exponent $α$ es closest to the value for the original text. However, while the dispersion of individual sample measures are very broadly spread for temperatures close to 0.5 they are tightly clustered around the mean for $T = 1.0$. A similar analysis was done on the Markov-generated texts. Figure 4C shows the result of the DFA for Markov texts of orders from 2 to 12, and a comparison to the original and shuffled texts. From the plot it is already clear that all the Markov-generated texts have a structural correlation that resembles more the shuffled text than the original one. This trend is corroborated in Figure 4D, which displays the estimated exponent $α$ as a function of the Markov order. In all cases, the value of the exponent is very
closed to the value obtained in the case of the shuffled text. Our final test to probe the statistical structure of the LSTM texts consisted in the estimation of entropy measures. The first estimation corresponded to a symmetrized KL-divergence (see Section III) between the LSTM for different temperatures and original text, estimated by means of compression algorithms that are sensitive to the long-range structure of the signal. Figure 5A shows the divergence as a function of the temperature. There is a well-defined minimum at $T \sim 1$, indicating that at that temperature the structure of the LSTM text is closest to the original. Figure 5C shows a similar plot for the Markov texts. Interestingly, the Markov texts also approximate the structure of the original texts asymptotically for larger orders. While the previous analyses showed the behavior of a distance-like quantity, the entropy is a more direct estimation of the statistical structure of a signal. Panels B and D in Figure 5 show the value of the entropy for the LSTM and Markov texts as a function of the temperature and order respectively. In both cases the horizontal line corresponds to the value of the entropy of the original text. For LSTM, lower values of temperature produce texts with small entropy, thus easier to compress, since they show repetitive patterns. As the temperature grows, the entropy also grows, with the texts becoming the most similar to the original around $T \sim 0.9$ (in line with our analyses) and far more disordered for larger values of $T$. The Markov texts, instead, show a monotonic approximation to the entropy of the original text remaining slightly above even for the higher orders considered.

To complete the analysis, we also computed the perplexity of texts generated by the LSTM, using the KenLM library. To do this, we learned a bigram language model on the original Dickens corpus and then we computed the perplexity both for the artificial texts, and for the off-sample Dickens documents in the test corpus used for authorship attribution. The results are perfectly in line with those obtained with entropy computation via compression, with values of temperature around 0.9-1.0 producing texts that are the most similar to the original ones also in terms of perplexity.

C. Creativity and Authorship Attribution

In order to assess the degree of plagiarism (and, thus, of creativity) of the generative models, we measured the length of the Longest Common Subsequence (LCS) between the artificial texts and the training corpus. As for the texts

https://github.com/kpu/kenlm
generated by Markov models, not surprisingly the length of the LCS rapidly grows with the order of the model, going from a value of 19 for order 2, up to 73 and 125 for order 10 and 12, respectively. For LSTM networks, the length of the LCS instead results to be lower, with values comprised between 40 and 60 when the temperature is in the range between 0.4 and 1.2. For smaller and larger temperatures, the value of the LCS is clearly smaller, since the generated texts have a much less realistic structure, and it is hence less probable to encounter patterns that are identical to the original. In order to better position the aforementioned values with regards to a sort of self-plagiarism that could be encountered in a subset of the works in the training corpus, we also computed the length of the LCS of the novel “Oliver Twist” with respect to a collection made up of five other novels by Dickens, the length of the LCS in this case resulted to be 45 characters.

For the experiments on authorship attribution, we used the Dickens and Stevenson corpora described in Section III-D. For a fixed temperature of the generated text, attribution is performed by averaging over 10 samples of artificial texts, using $n$-grams from $n = 1$ up to $n = 12$. Temperature is varied in the range 0.3-1.0, while for Markov texts we tested orders from 2 up to 12, with a step of 2. To assess the validity of the attribution algorithm, we compare the attribution of the generated texts with that of real texts. In particular, for each of the 30 Dickens and Stevenson documents, we employ the remaining 29 documents of each author to perform attribution either Dickens or Stevenson. The curves in Figure 6 show the value of the index $I(X)$ defined in Section III-D as a function of $n$-grams (on the x-axis) and either temperature for LSTM (panel A) or order for Markov texts (panel B), respectively. The attribution of real texts performs extremely well, with a maximum for $n = 6$ and $n = 10$ for Dickens and Stevenson, respectively. For LSTM, while the texts are indeed always correctly attributed to Dickens, it is interesting to notice how the best results are again achieved for values of temperature around 0.8-1.0, while for lower temperatures the attribution with larger $n$-grams largely decreases, since the generated texts tend to reproduce periodic (hence, less realistic) patterns. Not surprisingly, Markov texts with order greater than 6 are also well attributed to Dickens, due to the high degree of plagiarism described in the section V.C.

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8These were: David Copperfield, A Tale of Two Cities, Bleak House, Great Expectations, Hard Times.
VI. CONCLUSIONS

Deep learning has recently brought a real revolution to the field of natural language generation. In this paper, we investigated at what degree texts generated by an LSTM network resemble texts generated by humans. To this aim, we presented an extensive experimental evaluation where we compared several characteristics of artificial and original texts, starting from statistical properties that natural language typically shows, such as the distribution of word frequencies and long-range correlations, up to higher-level analyses, such as the attribution of authorship. Our study shows that LSTM-generated texts share many characteristics with natural language. In particular,
the experimental results highlight the fact that the temperature parameter has a crucial role in producing texts that resemble those created by humans, and that there exists an optimal range of values that induces the highest degree of similarity. Very interestingly, we also illustrated how a network trained on a single-author corpus can produce texts that are attributed to that author, according to authorship attribution algorithms.

The study presented in this paper opens the doors to many interesting research directions, which we plan to investigate in future works. First, we aim to compare the semantic information of the original and the artificial texts. In fact, it is clear from the samples shown in the experimental section, that LSTM texts are still far from human-generated texts in terms of semantics, although showing similar statistical properties. Within this context, we also plan to study the grammatical correctness of the generated texts. Then, we aim to move the analysis of these statistical properties of the LSTM texts to different languages, in order to assess whether there are some languages that are easier or more difficult to reproduce for a machine. We also want to further investigate the problems of authorship attribution and plagiarism, for which in this paper we only presented some seminal experiment. We plan to employ a larger corpus, in order to compare several authors, genres and languages, and to test different algorithms for authorship attribution.

REFERENCES


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