Learning Constructive Primitives for Real-time Dynamic Difficulty Adjustment in Super Mario Bros

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Abstract—Among the main challenges in procedural content generation (PCG), content quality assurance and dynamic difficulty adjustment (DDA) of game content in real time are two major issues concerned in adaptive content generation. Motivated by the recent learning-based PCG framework, we propose a novel approach to seamlessly address two issues in Super Mario Bros (SMB). To address the quality assurance issue, we exploit the synergy between rule-based and learning-based methods to produce quality game segments in SMB, named constructive primitives (CPs). By means of CPs, we propose a DDA algorithm that controls a CP-based level generator to adjust the content difficulty rapidly based on players’ real-time game playing performance. We have conducted extensive simulations with sophisticated SMB agents of different types for thorough evaluation. Experimental results suggest that our approach can effectively assure content quality in terms of generic quality measurements and dynamically adjust game difficulty in real time as suggested by the game completion rate.

Index Terms—Procedural content generation, machine learning, content quality assurance, constructive primitive, dynamic difficulty adjustment, real-time adaptation, Super Mario Bros.

I. INTRODUCTION

PROCEDURAL content generation (PCG) aims to generate game content automatically via algorithms [1], [2]. Recently, generating personalized game content has become an active research area in PCG [3]. A variety of content adaptation techniques have been proposed and applied to different game genres ranging from platform games to first person shooter [3]. Among them, dynamic difficulty adjustment (DDA) that adapts content difficulty for an individual player is a major strategy for game content adaptation.

Super Mario Bros (SMB) is a classic 2D platform game [4], which has become one of the most popular test beds for PCG research [5], [11], [36]. In SMB, a player runs from the left side of the screen to the right side, fights enemies, and rescues the Princess Peach. SMB has a number of game elements suitable for deploying PCG techniques for content adaptation, e.g., enemies, coins, tubes and cannons. As a result, several adaptive SMB level generators have been studied [6]–[11].

While substantial progresses have been made, there are still several open problems in SMB content or level adaptation. First, content quality assurance is still a fundamental issue in SMB level adaptation since the low quality game content inevitably leads to negative gameplay experience [2], [12], [14]. Filtering out the low quality content in personalized content generation is extremely challenging as adaptive content often has to be generated on-line. Next, the existing game adaptation techniques can be generally divided into two categories: model-free or model-based [3], [15]. In a model-free approach, player model is established for adaptation based on human players’ gameplay data, e.g., playlog and controllable parameters in a game, and their subjective feedback, e.g., affective states such as “fun”, while player model in a model-based approach is derived from psychological emotion theories, e.g., [18], [19] and [20]. To the best of our knowledge, most of the existing SMB adaptation methods fall into the model-free category and model-based adaptation has yet to be investigated for SMB level adaptation. In particular, the real-time model-based DDA that the content difficulty is adjusted dynamically within a level generation still remains unexplored in SMB level adaptation research up to now.

Motivated by the learning-based PCG (LBPCG) framework [14] where a quality evaluation function may be learned from games/levels annotated by game developers, we recently proposed an approach [21] for generating short game segments of high quality, named constructive primitives (CPs), for SMB based on a modified version of Infinite Mario Bros [5]. In this approach, easy-to-design rules are first employed to remove apparently unappealing game segments and a content quality evaluation function working on CPs is then established via machine learning. This hybrid method would allow for addressing the quality evaluation issue more effectively. Nevertheless, the CP learning idea was neither investigated sufficiently nor evaluated thoroughly in our previous work [21]. In addition, our CP-based approach was only preliminarily applied to online level generation to demonstrate its usefulness. Hence, its potential still needs to be explored further.

In this paper, we further develop our hybrid CP generation idea with sufficient justification and thorough evaluation. For model-based adaptation, we come up with a novel performance-driven real-time DDA algorithm to explore the potential of our CP-based generation idea by using SMB as a test bed. We have thoroughly evaluated the quality of our CPs via generic yet objective quality measurements and a comparative study. Subsequently, the effectiveness of our proposed CP-based DDA algorithm is thoroughly evaluated via simulations with sophisticated SMB agents of different types. Experimental results suggest that our data-driven evaluation function effectively encodes multiple quality-related criteria in

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an implicit way and our model-based DDA algorithm working on CPs yields favorable results in real-time adaptation.

The main contributions of this paper are summarized as follows: a) the further development of our hybrid approach to quality assurance of short game segments in SMB [21], which lays the foundation for a new level generation approach in different scenarios; b) a novel CP-based DDA algorithm for real-time adaptation in SMB; and c) a thorough evaluation of our hybrid approach to quality assurance and our CP-based DDA algorithm via simulation.

The remainder of this paper is organized as follows. Sect. II reviews the relevant works. Sect. III presents our approach to generating CPs in SMB. Sect. IV describes our CP-based DDA algorithm. Sect. V reports experimental results, and the last section discusses remained issues and relates ours to previous works.

II. RELATED WORK

In this section, we review the relevant works that motivate our study presented in this paper.

Constructive PCG has been widely applied in adaptive SMB level generation [6]–[9], [11], where human experts design a set of constructive rules that can be converted into high-level game parameters corresponding to concrete game levels. In particular, there exist several constructive approaches in SMB [8], [9], [11] that first generate game segments by exploring the local properties and then merge segments to generate a complete game level via a set of constructive rules. In general, constructive rules were handcrafted with developers’ elaborate knowledge on different content features and their remarkable skills in rule formulation. While constructive rules may make content adaptation easier, they have to ensure that generated content is playable and appealing to individual players, which heavily relies on the understanding of content space and sophisticated knowledge/skills in rule formulation. To ensure that generated content is playable and appealing to individual players, the rule design is rather difficult especially when the content space is complex. Unlike existing constructive SMB generators, our work presented in this paper retains the favorable properties of constructive generators but addresses the content quality assurance issue in a different manner.

Dynamic difficulty adjustment (DDA) is a major technique used in adaptive content generation where the difficulty of content is dynamically adjusted to match an individual player’s skill level and/or to optimize their cognitive/affective experience during gameplay [3], [15]. As described in Sect. I, DDA can be carried out by either a model-free or a model-based method [3], [15]. To the best of our knowledge, however, all the existing SMB level adaptation methods [6]–[10] are model-free; in other words, no model-based DDA has been studied for SMB. Nevertheless, model-based DDA has been studied widely in a variety of games, including real-time strategy [23], prey/predator [22], fighting [27], role playing [25] and car racing [26] games, especially for non-player character (NPC) adaptation. In general, model-based DDA works on the assumption that maximum gameplay enjoyment occurs with the content of a moderate challenge [18]–[20], [22], and can be carried out by different techniques such as evolutionary algorithms (EAs), e.g., [22], [23], reinforcement learning (RL), e.g., [25], [27], and their combination, e.g., [26]. In general, EAs are capable of finding proper game content based on given score metrics from large high-dimensional content space [24] but less efficient in carrying out the real-time DDA due to the population-based computation. In contrast, RL enables a generator to make a rapid adaptation but is more suitable for low-dimensional space exploration [24]. Some efforts [26] have been made to exploit the synergy between EAs and RL in a car racing game. Motivated by the existing model-based DDA approaches and taking the nature of our CPs into account, we employ RL to come up with a model-based DDA algorithm for real-time adaptive SMB level generation. Here, we emphasize that our algorithm works on game geometry adaptation rather than NPC behavior adaptation studied in most of existing model-based DDA approaches.

III. CONSTRUCTIVE PRIMITIVE GENERATION

In this section, we first describe our motivation and main ideas. Then, we present our approach to learning constructive primitives (CPs) in SMB.

A. Overview

Existing SMB level generators work on a huge content space that contains all the complete procedural levels. As there are an enormous variety of combinations among game elements and structures at a procedural level, such a content space inevitably leads to a greater challenge in managing quality assurance and making content adaptation. Nevertheless, a complete procedural level in SMB may be decomposed into a number of short segments as done in [8], [9], [12], [16], [41]. Thus, partitioning a procedural level into fixed-size game segments results in a new content space of lower complexity, which allows us to explore the SMB content space from a different perspective. It is anticipated that the content space of short game segments would facilitate a constructive PCG approach in tackling content quality assurance and real-time content adaptation effectively.

For quality assurance, there are generally two methodologies in developing such a mechanism in PCG [1], [14]: deductive vs. inductive. To adopt the deductive methodology, game developers have to understand the content space fully and have skills in formulating/encoding their knowledge into rules or constraints explicitly. In the presence of a huge content space, however, it would be extremely difficult, if not impossible, to understand the entire content space, which might lead to less accurate (even conflicted) rules/constraints used
in PCG. Nevertheless, we observe that some constraints in SMB are easy to identify. For example, overlapped tubes are unacceptable and easily detected with a simple rule. On the other hand, a learning-based PCG (LBPCG) framework [14] was proposed where an inductive methodology is advocated for quality assurance via learning from annotated data. As video game content is observable but less explainable, it is easier for developers to judge the quality of games (especially in presence of complex content elements and structures) via visual inspection (applying their knowledge implicitly) than to formulate their knowledge into rules formally with sophisticated skills. Thus, a quality evaluation function may be learned from games/levels annotated by developers. This observation suggests that exploiting the synergy between rule-based and learning-based methods would allow for addressing the quality evaluation issue more effectively.

With the motivation described above, we propose a hybrid approach for generating CPs (quality yet controllable game segments) in SMB, where both simple rules and a learning-based method work together. Fig. 1 illustrates the main steps of our approach. First of all, game developers choose a region that covers main variations of game elements and structures in SMB from the entire content space via controllable parameters. Then all the game segments in this region are evaluated based on a set of easy-to-design conflict resolution rules. Finally, subsequent data-driven quality evaluation function deals with more complicated quality issues. Surviving game segments form CPs to facilitate generating adaptive SMB levels.

B. Content Space and Its Representation

A recent study [12] suggests that in SMB, game segments of 20 in length and 15 in height (i.e., the approximate size of a screenful of tiles in SMB) are sufficient to express rich yet diverse types of game elements and structures in a procedural level for 2D platform games. As exemplified in Fig. 2, such game segments are naturally specified by a 2D grid similar to an image. However, this leads to a 300-dimensional content space of massive redundancy, e.g., the uniform background.

Instead of the 2D grid representation, we employ a list of design elements, atomic units in PCG, as our content representation, including initial platform, gaps without/with rock decoration, hill, cannon, tubes without/with flower enemy, boxes without/with coins/powerup, enemies, coins, mushroom and fire flower, as illustrated in Fig. 3. By using this representation, we not only specify the content space concisely but also gain the direct control on low-level geometrical features, e.g., coordinates of tubes and coins. As listed in Table I, 85 content features used in our representation are grouped into 15 categories where a content feature is used to specify and control a design element in a segment. Our representation is similar to those used in the previous work [35], [42]. In this representation, \( x, y, width, height \) and type refer to \( x \), \( y \) coordinates, width, height and type of each design element, while \( w_{before} \) and \( w_{after} \) refer to width of the platform before and after each tube/cannon. Among these features, types of gap, tube, boxes and enemies are nominal features, while the rest are ordinal features. In our content space, the design elements in each type are sorted in a decreasing order along \( x \) dimension. However, there are several redundant parameters in this representation, e.g., if the number of cannons is one, then the parameters for the second and third cannons will be useless. In this case, we simply set all the meaningless parameters to zero. Here, we emphasize that the design elements listed in Table I are fully controllable; game developers can control relevant content features to generate a specific game segment. For example, a mountainous segment may be generated by setting the number of hills to 1 or 2 and other features.

![Fig. 1. The constructive primitive (CP) generation process for SMB.](image1)

![Fig. 2. Typical 20 × 15 game segment instances.](image2)

![Fig. 3. Game design elements. (A) Initial platform. (B) Gaps without/with rock decoration. (C) Hill. (D) Cannon. (E) Tubes without/with flower enemy. (F) Boxes without/with coins/powerup. (G) Enemies. (H) Coins. (I) Mushroom and fire flower.](image3)

<table>
<thead>
<tr>
<th>ID</th>
<th>Description</th>
</tr>
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<tbody>
<tr>
<td>1</td>
<td>height of initial platform</td>
</tr>
<tr>
<td>2</td>
<td>number of gaps</td>
</tr>
<tr>
<td>3 - 11</td>
<td>( x, width ) and type of the 1st - 3rd gap</td>
</tr>
<tr>
<td>12</td>
<td>number of hills</td>
</tr>
<tr>
<td>13 - 18</td>
<td>( x, width ) and height of the 1st and 2nd hill</td>
</tr>
<tr>
<td>19</td>
<td>number of cannons</td>
</tr>
<tr>
<td>20 - 34</td>
<td>( x, y, height, w_{before} ) and ( w_{after} ) of the 1st - 3rd cannon</td>
</tr>
<tr>
<td>35</td>
<td>number of tubes</td>
</tr>
<tr>
<td>36 - 55</td>
<td>( x, y, height, w_{before}, w_{after} ) and type of the 1st - 3rd tube</td>
</tr>
<tr>
<td>56</td>
<td>number of boxes</td>
</tr>
<tr>
<td>55 - 62</td>
<td>( x, y, width ) and type of the 1st and 2nd boxes</td>
</tr>
<tr>
<td>63</td>
<td>number of enemies</td>
</tr>
<tr>
<td>64 - 78</td>
<td>( x, y ) and type of the 1st - 5th enemy</td>
</tr>
<tr>
<td>79</td>
<td>number of coins</td>
</tr>
<tr>
<td>80 - 85</td>
<td>( x, y ) and width of the 1st and 2nd coins</td>
</tr>
</tbody>
</table>

![Table I. Content features.](image4)
randomly, while a pure linear segment is generated by setting the number of hills, \( y \) coordinate of tubes, and cannons to zero.

While design element parameters in Table I have a huge range that specifies the entire content space, we confine our concerned content space to a non-trivial region by setting the maximum number of gaps, hills, tubes, cannons, boxes, coins and enemies to 3, 2, 3, 2, 2 and 5, respectively, in a game segment. Consequently, there are roughly \( 9.72 \times 10^{37} \) different game segments in the content space used in our experiments. This content space is sufficient to generate content with a variety of geometrical features, level structures and difficulties required by SMB. We believe that a larger content space may contain more unplayable or aesthetically unappealing game segments. For instance, a \( 20 \times 15 \) game segment containing more than five enemies or more than three cannons/gaps is too difficult for human to play and appears aesthetically unappealing if there are more than three tubes inside.

C. Conflict Resolution

As the content representation described in Sect. III-B results in overlapped design elements, there are a large number of game segments that contain conflicting design elements in our content space. For instance, “…Tube(6,0,2,0,flower)…Cannon(6,0,4,0,0)…” represents a game segment of at least one tube and one cannon, where \( x, y, \) height, \( \text{w}_{\text{before}}, \text{w}_{\text{after}} \) and type of this tube are 6, 0, 2, 0, 0, and flower, and the \( x, y, \) height, \( \text{w}_{\text{before}} \) and \( \text{w}_{\text{after}} \) of this cannon are 6, 0, 4, 0, and 0. As both the tube and the cannon share the same \( x \) coordinate, the cannon and the tube are overlapped in this game segment. This conflict makes the segment aesthetically unappealing.

To address this issue, we first discard those game segments of geometrically conflicted design elements via a set of simple rules in our approach. Our rules for the above situations are similar to those presented in [35], [42]; i.e., any overlapping among gap, enemy, tubes, cannons, boxes, and coins are forbidden, whilst hills of different heights are allowed to be overlapped and enemy/tube/cannon may also be overlapped with hills in a game segment.

Application of the above-mentioned rules to the entire content space leads to a tailored content space. Learning CPs merely works on this tailored content space.

D. Learning Constructive Primitives

After filtering out those obviously unappealing game segments via rules described in Sect. III-C, the tailored content space still contains a lot of low quality segments, e.g., segments of unreachable coins and boxes, unplayable segments, segments of unbalanced resources and aesthetically unappealing structures. Inspired by the LBPCG framework [14], we would learn a quality evaluation function from annotated game segments to detect unplayable/unacceptable segments.

Thus, the problem in our CP learning is formulated as binary classification. For such a classifier, its input is the 85D feature vector of a game segment and its output is a binary label that predicts the quality of a game segment.

To carry out the aforementioned idea, however, we have to tackle a number of non-trivial problems. After conflict resolution, there are still a huge number of game segments in the tailored content space. It is computationally intractable to deal with all the segments in this content space. To tackle this problem, sampling appears to be a suitable technique as it can generate a much smaller data set of the same properties owned by an original content space. To make a learning-based quality evaluation function, training examples are essential but have to be provided by game developer(s). Although the use of sampling leads to a computationally manageable data set, annotating all the segments in this sampled data set is not only laborious and time-consuming but also may not be necessary if their distribution can be estimated. Clustering analysis provides a manner for exploring the distribution and the structure underlying the sampled data set. Furthermore, we adopt the active learning methodology that enables us to train a classifier with only a small number of most informative game segments annotated by game developer(s) during active learning. To carry out an effective active learning, we exploit the clustering results to minimize the number of annotated game segments required by active learning since game segments residing in all the different clusters are likely to hold the main properties of the entire tailored content space. Thus, clustering analysis not only facilitates active learning but also reveals non-trivial properties of a content space, which allows for using other techniques, e.g., visualization, to understand a large content space and to identify the cause of misclassification in active learning (c.f. Sect. V-A).

As depicted in Fig. 4, our CP learning process hence consists of three stages: sampling (to be computationally tractable), clustering analysis (to explore the distribution and the structure underlying the sampled data set) and active learning (to establish an effective classifier with minimal labeled game segments backed by the clustering analysis). The main techniques used in each stage of our CP learning are presented below.

1) Sampling: For sampling, we apply the simple random sampling (SRS) with replacement [28] to the tailored content space for a manageable data set. In comparison with other sampling approaches, SRS is unbiased and enables each game segment in this tailored content space to be selected with the equal probability. Moreover, it is capable of handling unknown data distribution without using any prior knowledge. Thus,
SRS becomes a proper sampling technique for our approach as we do not know the accurate distribution of our tailored content space.

In sampling, we have to address the issue on the size of a sample that can retain all non-trivial properties underlying the tailored content space. Due to its unknown distribution, we need to apply the sample size determination (SSD) algorithm suggested in [28], [29] to determine the size of our sample. According to the SSD algorithm, the proper sample size, \( N \), for a given data set is estimated by

\[
N \approx \frac{z^2 \delta^2}{d^2} = \frac{1.96^2 \times 49.7749}{0.10^2} = 19121.32 \approx 19000,
\]

where \( z \) stands for the \( z \)-score of 1.96 for a 95% confidence interval, and \( d \) is 0.10 that refers to a small tolerable difference. These values are default in the SSD algorithm. \( \delta^2 \) refers to the maximum variance of the content space among different features. The value of \( \delta^2 \) is 49.7749, which is approximated by the largest variance estimated on several samples of the tailored content space [29]. With the approximation in (1), we sample the tailored content space to yield a sampled data set of 19,000 game segments.

2) Clustering: For clustering analysis, we employ the CURE algorithm [30] on the sampled data set since it is applicable to a data set of unknown data distribution [31] and can uncover the structure underlying data by automatically determining the proper number of clusters underlying a data set [32]. To use the CURE, one has to pre-set four hyper-parameters: the number of clusters, sampling rate, shrink factor and the number of representative points. By using the dendrogram tree resulting from this hierarchical clustering algorithm, the number of clusters is automatically decided by the longest \( k \)-cluster lifetime defined in [32]. The rest of parameters are set to defaults as suggested in [30]; i.e., 0.5 for shrink factor, 2.5% for sampling rate, and 10 representative points, respectively.

As there are three different feature types in our content representation, i.e., numeric, nominal and ordinal, we employ the mixed-variable distance metric [31] in the CURE. The mixed-variable distance \( d(i, j) \) between objects \( i \) and \( j \) is defined by

\[
d(i, j) = \frac{\sum_{f=1}^{F} d_{q}^{(f)}}{F},
\]

where \( F \) denotes the number of features in the content representation and \( d_{q}^{(f)} \) refers to the contribution of feature \( f \) to the overall distance between objects \( i \) and \( j \). Suppose the value of \( f \) for the \( i \)th object is \( x_{q} \), the distance regarding this feature, \( d_{q}^{(f)} \), is measured with a metric dependent on its feature type:

- When \( f \) is numeric: \( d_{q}^{(f)} = \frac{|x_{q} - x_{q,j}|}{\max_{a} x_{a} - \min_{a} x_{a}} \), where \( h \) runs over all data set for feature \( f \).
- When \( f \) is nominal: \( d_{q}^{(f)} = 0 \) if \( x_{q} = x_{q,j} \) and \( d_{q}^{(f)} = 1 \) otherwise.
- When \( f \) is ordinal: compute the \( z_{q} = r_{q} - 1 \), where \( r_{q} \in \{1, ..., M_{f}\} \) are the corresponding ranks of \( M_{f} \) ordered states that \( f \) has. Then, an ordinal feature is converted into numeric via \( z_{q} \).

The above treatment used in the mixed-variable distance metric normalizes distances contributed by different features [31], respectively. These normalized distances tend to eliminate the bias introduced by a feature of a large permissible range and make the overall distance \( d(i, j) \) within a range of \([0, 1]\).

Clustering analysis with the CURE algorithm on the sampled data set leads to 58 clusters, and the detailed experimental results are reported in Sect. V-A1.

3) Active Learning: For active learning, a validation set that holds main properties of the content space is required to evaluate/monitor the generalization performance during active learning. By considering the segment distribution information, we first select a small number of segments randomly from each cluster to form such a validation set of 800 segments totally, where the number of segments selected from each cluster is proportional to the cluster size. The first author of this paper, an experienced game player, labels all 800 game segments in the validation set via visual inspection; up to five seconds are taken in annotating any segments in our experiments. As a result, a binary label is assigned to a segment to indicate its quality; +1/-1 is a label of good/poor quality. The qualitative labeling criteria are based on the annotator’s own knowledge/experience and guided by the existing literatures. Below we summarize the main aspects considered during the annotation:

- **Playability.** There should exist a path between entrance of game level and exit, which allows players to finish the game [1].
- **Resource balance.** Design elements within a quality segment should be distributed in terms of balance [2], [39], [42].
- **Difficulty curve.** A quality segment should not contain unexplainable difficulty spikes/curve [2], [42].
- **Reachability.** All the resources (e.g., coins and boxes) in a quality segment should be reachable [13].
- **Aesthetic properties.** A quality segment should contain meaningful, aesthetically appealing and reasonable structures [2], [12], [39].

Here, we emphasize that the annotator labels a game segment via visual inspection only by taking into account the above-mentioned aspects. In other words, the annotator merely applies his knowledge/experience implicitly in visual inspection (without any explicit yet well-formulated rules in mind).

In general, there are two error types in binary classification: false negative (type-I error) where a high quality segment is misclassified as low quality and false positive (type-II error) where a low quality segment is misclassified as high quality. Obviously, a type-II error could result in a catastrophic effect while a type-I error is less harmful as it simply shrinks the content space slightly. As a result, we formulate our classification as a cost-sensitive learning problem where the type-II error incurs a higher cost in learning. By looking
Algorithm 1 Active Constructive Primitive Learning

Input: Sampled data set $U$ and clustering results on $U$.
Output: WRF binary classifier.
Initialization: Based on the clustering analysis results, create a validation set $V$ of 800 examples.
Active Learning: Annotate 100 segments randomly selected from $U$ via visual inspection to form a training set $L$. Train WRF on $L$ to obtain an initial binary classifier.
repeat
  for all $x_i \in U$ do
    Label $x_i$ with the current WRF.
    Calculate the uncertainty score $s_i$ of $x_i$.
  end for
  Annotate 100 segments of the highest uncertainty score in $U$ to form a new training set $L$.
  Re-train the WRF with the examples in $L$.
until The overall accuracy on $V$ does not increase.
return Classifier WRF.

Algorithm 2 Generating a CP of a Specified Difficulty Level

Input: A specified difficulty level.
Output: A CP of this specified difficulty level.
Generation: Choose a region of interest from the content space via difficulty parameters described in Table II.
repeat
  Randomly select a game segment $g$ from the region of interest.
  Evaluate game segment $g$ via conflict resolution rules and data-driven evaluation function.
until Evaluation results are positive.
return Game segment $g$.

into several state-of-the-art classification techniques, we found that the weighted random forest (WRF) [33], a cost-sensitive oblique random forest [34] classifier, fully meet our requirements for active learning. As an ensemble learning approach, a WRF works based on decision trees trained on randomly partitioned data subsets for classification. Such a classifier can handle a data set of different feature types and offers the feature importance information during active learning, which is extremely useful for developers. To address the cost-sensitive issue, the WRF applies class weights to the information gain during finding optimal splits. In the terminal nodes of each tree, the class prediction is determined via weighted majority vote. The final class prediction of the WRF is also determined via the weighted vote of individual trees. In our experiments, the “optimal” hyper-parameters of the WRF are decided via validation suggested in [33]: 1.3:1 for cost ratio, 30 trees, 5 combined features, 30 feature groups selected at each node and 9 in depth.

Active learning is undertaken on the entire sampled data set excluding 800 segments used to form the validation set described at the beginning in Sect. III-D3. We initially choose 100 segments randomly and label them via visual inspection. Then we use these 100 examples to train an initial WRF. Based on the initial WRF, our active learning works on uncertainty sampling for efficiency. In each iteration of active learning, we find 100 segments of the highest uncertainty scores defined by $s_i = 1 - P(\hat{y}|x_i)$, where $\hat{y}$ is the predicted label of segment $x_i$ and $P(\hat{y}|x_i)$ is the probability of this prediction yielded by the current WRF. Then we annotate those 100 segments to form new examples for re-training the WRF. The active learning carries on until the accuracy of this WRF on the validation set no longer increases. Our active learning algorithm is summarized in Algorithm 1. The detailed results on active learning are reported in Sect. V-A2.

Once the evaluation function is learned, it will be used (along with the conflict resolution rules described in Sect. III-C) to produce CPs in a generate-and-test way. In the next section, we develop an algorithm that combines proper CPs via controllable parameters, which leads to a new adaptive level generator for real-time DDA in SMB.

IV. CP-BASED DYNAMIC DIFFICULTY ADJUSTMENT

In this section, we propose a DDA algorithm by applying the CPs described in Sect. III to real-time content adaptation. This algorithm works on the model-based assumption; i.e., maximum gameplay enjoyment occurs with the content of a moderate challenge [18]–[20], [22], and the appropriate challenge level can be reflected by the game playing performance.

For the model-based DDA, it is essential to define game difficulty levels and to measure the game playing performance. In our CP-based approach, the difficulty-level definition is motivated by the difficulty/leniency metric presented in [35], which suggests that the difficulty of a SMB level may be determined by main design elements. In our work, we use enemies, gaps, cannons and flower tube to define five difficulty levels, as shown in Table II.

TABLE II. DIFFICULTY-LEVEL PARAMETER FOR GAME ADAPTATION.

<table>
<thead>
<tr>
<th>Level</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>number of enemies $\leq 0$; number of gaps $\leq 2$; number of flower tube $= 0$; number of cannons $= 0$; width of gap $&lt; 3$; gaps without rock</td>
</tr>
<tr>
<td>2</td>
<td>number of gaps $= 0$; number of enemies $= 1$; number of cannons $= 0$; number of flower tube $= 0$</td>
</tr>
<tr>
<td>3</td>
<td>number of gaps $\leq 1$; width of gap $&lt; 3$; $1 \leq$ number of enemies $\leq 2$; number of cannons $= 0$</td>
</tr>
<tr>
<td>4</td>
<td>number of cannons $\leq 1$; $1 \leq$ number of enemies $\leq 4$</td>
</tr>
<tr>
<td>5</td>
<td>number of cannons $\geq 1$; number of enemies $\geq 3$</td>
</tr>
</tbody>
</table>

This algorithm works on the model-based assumption; i.e., maximum gameplay enjoyment occurs with the content of a moderate challenge [18]–[20], [22], and the appropriate challenge level can be reflected by the game playing performance. To test the effectiveness of our difficulty level definition, each agent plays 30 games at each difficulty level. The averaging complete rates at difficulty levels 1-5 are 0.71, 0.54, 0.46, 0.42 and 0.38, respectively. It suggests that our difficulty level definition summarized in Table II.
can considerably affect the completion rate. As described in Algorithm 2, a CP of the specified difficulty level can be generated by controlling the content features shown in Table II with support of the conflict resolution rules and the data-driven quality evaluation function described in Sect. III. Measuring a player’s performance may be complicated if all different factors have to be considered. In this paper, we only take into account the survivability on CPs, which will be discussed later on.

In our work, we make use of CPs for real-time DDA, i.e., the performance is measured locally on a CP rather than on a procedural level and the DDA is done instantly in response to a player’s performance on the last played CP. This is naturally a sequential decision process as only the performance regarding the last played CP affects the difficulty level of the next CP to be generated. Thus, we formulate this as a Markovian decision process (MDP) [37] and our goal is hence to find an optimal policy that maximizes the expected long-term performance via adjusting the difficulty of generated CPs. To attain this goal, we define a regret $\rho$ at time $T$ (i.e., after $T$ CPs have been played) as the absolute difference between an expected survival rate and the expectation of rewards:

$$\rho = \left| \theta_{opt} - \frac{1}{T} E\left[ \sum_{t=1}^{T} r_t \right] \right|,$$  

(2)

where $\theta_{opt}$ is a pre-set optimal survival rate on any CP in a level and $r_t$ is a binary reward: $r_t = 1$ if the player survives on the CP played at time $t$ and 0 otherwise. For instance, $\theta_{opt} = 0.8$ means that the performance of the survival rate 0.8 is expected for any CP in an adaptive level. For a given $\theta_{opt}$, levels of proper difficulties can be generated for a player to gain the expected performance. Thus, minimizing the regret in (2) is key to our DDA. To solve this optimization problem, we employ the Thompson sampling [38], an effective and efficient heuristic method used in binary reward case in MDP.

Let $\theta_i$ denote a player’s survival rate at difficulty level $i$ ($i = 1, \cdots, 5$). Thus, a player survives with the probability $\theta_i$ and reciprocally dies with the probability $1 - \theta_i$ when they play a CP of difficulty level $i$. During gameplay, one plays a number of CPs of different difficulty levels sequentially. When a CP of difficulty level $a_t = i$ is completed at time $t$, a binary reward is assigned. Given the player’s survival rate $\theta_i$ corresponding to $a_t$, the reward likelihood is

$$P(r_t|a_t = i, \theta_i) = \theta_i^{r_t}(1 - \theta_i)^{1-r_t}.$$  

(3)

Furthermore, let $D_T = (a_1, r_1), \cdots, (a_T, r_T)$ denote the historical profile regarding corresponding difficulties and rewards after $T$ CPs have been played. By using a conjugate prior, $\theta_i \sim Beta(1, 1)$, the posterior distribution of survival rate based on the likelihood in (3) is $P(\theta_i|D_T) \propto \prod_{t=1}^{T} P(r_t|a_t, \theta_i)P(\theta_i)$, which leads to $\theta_i|D_T \sim Beta(\alpha_i + 1, \beta_i + 1)$ where $\alpha_i$ and $\beta_i$ are the number of survivals and deaths when playing the CPs of difficulty level $i$ in $D_T$.

### Algorithm 3: CP-based DDA for Real-time Content Adaptation

**Input:** Optimal survival rate $\theta_{opt}$.

**Initialization:** $t \leftarrow 0$, $\alpha_i \leftarrow 1$ and $\beta_i \leftarrow 1$ for $i = 1, \cdots, 5$.

**repeat**

$t \leftarrow t + 1$.

if $t = 0$ or $r_{t-1} = 0$ then

For each $i \in \{1, \cdots, 5\}$, sample $\theta_i$ from $Beta(\alpha_i, \beta_i)$.

Choose action $a_t = \text{argmin}_i |\theta_{opt} - \theta_i|$. 

else

For each $i \in \{\max(1, a_{t-1} - 1), a_{t-1}, \min(a_{t-1} + 1, 5)\}$, sample $\theta_i$ from $Beta(\alpha_i, \beta_i)$.

Choose action $a_t = \text{argmin}_i |\theta_{opt} - \theta_i|$.

end if

Generate the chosen CP of $a_t$ using Algorithm 2.

if $r_t = 1$ then

$\alpha_{a_t} \leftarrow \alpha_{a_t} + 1$. //the player survives

else

$\beta_{a_t} \leftarrow \beta_{a_t} + 1$. //the player dies and a new game starts

end if

until Gameplay stops.

For content adaptation, we follow the typical setting in real SMB games: at the beginning, a player is put in small state, i.e., the weakest form of Mario, where the player is not allowed to use powerful weapons (e.g., throwing fireballs) and then turns into other states by powering up with a mushroom or fire flower. Based on the gameplay information recorded in $D_T$, CPs are randomly produced according to $Beta(\alpha_i + 1, \beta_i + 1)$ and the CP of difficulty level $i$ is chosen as a game segment to play if it results in the least regret defined in (2). After a CP of difficulty level $i$ is played, the posterior probability $Beta(\alpha_i + 1, \beta_i + 1)$ is updated based on the performance of the CP. Thus, this content adaptation process continues until a player quits. Our real-time DDA is summarized in Algorithm 3.

### V. Experimental Results

In this section we report experimental results on the CP learning and the real-time DDA. The game engine adopted in our experiments is a modified version of the open-source Infinite Mario Bros used in the Mario AI Championship [11], [36]. The source code used in our experiments as well as more experimental results not reported in this paper are publicly available on our project website.

#### A. Results on Constructive Primitive Learning

Based on the learning algorithms described in Sect. III, we report results on clustering analysis and active learning to explore our content space and to demonstrate the benefit of our data-driven evaluation function.

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1. [http://staff.cs.manchester.ac.uk/~kechen/CP-Mario.html](http://staff.cs.manchester.ac.uk/~kechen/CP-Mario.html)
### TABLE III. RELATIONSHIP BETWEEN CLUSTERS AND MAIN FEATURES

<table>
<thead>
<tr>
<th>Feature</th>
<th>Value</th>
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<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
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<td>56</td>
<td>54</td>
<td>21</td>
<td>6</td>
<td>-</td>
<td>-</td>
</tr>
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<td>49</td>
<td>30</td>
<td>1</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Number of Cannons</td>
<td></td>
<td>50</td>
<td>55</td>
<td>33</td>
<td>13</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Number of Tubes</td>
<td></td>
<td>51</td>
<td>45</td>
<td>17</td>
<td>6</td>
<td>-</td>
<td>-</td>
</tr>
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<td>53</td>
<td>33</td>
<td>13</td>
<td>-</td>
<td>-</td>
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<td>Number of Enemies</td>
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<td>47</td>
<td>55</td>
<td>55</td>
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<td>Difficulty Level</td>
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<td>-</td>
<td>26</td>
<td>29</td>
<td>41</td>
<td>54</td>
<td>36</td>
</tr>
</tbody>
</table>

**Fig. 5.** Exemplary game segments in different clusters.

1) **Cluster Analysis:** Application of the CURE clustering algorithm described in Sect. III-D2 leads to 58 clusters. While all the clustering results are available on our project website, Table III summarizes the non-trivial properties of clusters on seven content features that mainly affect the appearance and styles of game segments. As a content feature has a permissible value range, we hence report the properties of clusters based on each permissible value of a given content feature in Table III where \( M(N) \) denotes that there are \( M \) clusters containing those game segments of a specific value for a given content feature and \( N \) out of those \( M \) clusters have more segments of this value than those of different values regarding this content feature. For example, the first element in Table III is with respect to all the segments containing no gap, i.e., the number of gaps equals zero, and \( 56(46) \) indicates that such segments appear in 56 clusters where 46 out of those 56 clusters have more segments containing no gap than those with gaps.

In general, \( M \) states the number of clusters a feature is distributed and \( N \) indicates the number of clusters this feature is predominant. Hence, both \( M \) and \( N \) facilitate the understanding of the segment distribution in the tailored content space. For instance, \( M \) is 57, 49 and 30, respectively, corresponding to the value of feature NumHills = 0, 1 and 2. It suggests that those segments with the feature NumHills of different values are widely spread in many clusters. In contrast, the corresponding \( N \) values are 48, 9, 1, respectively, which indicates hills of different numbers are not distributed uniformly in those clusters containing hills. It is observed from Table III that segments of different content features are not distributed uniformly, and the tailored content space contain more segments specified by only a few design elements since segments with many design elements are likely to commit to illegitimate overlapping and hence removed by the conflict resolution rules prior to clustering. Thus, the use of conflict resolution rules causes a bias to segments of fewer design elements in our CP generation. The clustering results also reveal the distribution of segments of different difficulty levels (c.f. Table II). Here, we adopt the same notation to report the distribution of segments of difficulty levels 1-5 in Table III. For instance, 26(3) in the bottom row of Table III indicates that there are 26 clusters containing segments of level 1 where only three clusters contain more segments of level 1 than those belonging to other levels.

For intuition, we visualize exemplary game segments in a number of clusters in Fig. 5. It is observed: a) segments in cluster 18 have at least one set of boxes and two sets of coins; b) segments in cluster 38 include at least one tube; c) segments in cluster 50 contain at least two sets of boxes and one cannon; and d) there are at least three enemies, one cannon, and one set of boxes in segments belonging to cluster 57. The exemplification shown in Fig. 5 suggests that our clustering analysis is meaningful since segments within the same cluster contain similar content while those in different clusters vary in terms of geometry and structures. Hence, we use the clustering results to facilitate the subsequent active learning.

2) **Active Learning:** Fig. 6 illustrates the evolutionary performance of our active learning on the validation set described in Sect. III-D3, including type-I and -II error rates as well as their average, the half total error rate (HTER). It is shown in Fig. 6 that active learning reaches an optimum at 1,200 queries with a total of 1,300 queries. While the optimal HTER
is around 11.18%, the corresponding type-I and -II error rates are around 16.67% and 5.69%, respectively. Fortunately, those segments resulting in type-II error do not include unplayable game segments in our experiments; in other words, all the unplayable segments in validation set were classified correctly.

To demonstrate our active learning results vividly, we show several correctly classified and misclassified segments in Fig. 7. For clarification, segments are correctly classified if their labels assigned by our classifier are consistent with the developer’s labels and those are misclassified otherwise. Segments in Fig. 7(T) are correctly labeled as positive. These high quality segments contain playable structures, reachable resources and a meaningful combination capturing an area of challenge and conveying a sense of progression. However, these segments generated by our approach do not seem to appear in handcrafted SMB levels. Segments in Fig. 7(I) should have been labeled as positive since these segments look like appealing short episodes in a procedural level. Unfortunately, they are misclassified as negative by our classifier, which leads to type-I error. Segments in Fig. 7(N) are correctly classified as negative: Fig. 7(N).1 consists of unplayable structure which does not allow a player to pass through; Fig. 7(N).2 contains simple structures and hence lacks a sense of progression; Fig. 7(N).3 and Fig. 7(N).5 appear aesthetically unappealing since arbitrarily lumped enemies, gap, boxes, and tubes are less meaningful; and Fig. 7(N).4 contains unreachable boxes. In contrast, segments in Fig. 7(II) should have also been labeled as negative but misclassified by our classifier, which results in type-II error. It is seen that all game elements, i.e., enemy, cannon, tube flower, in Fig. 7(II).1 and Fig. 7(II).2 are located in a narrow zone in the middle of those game segments. In literature [2], such a situation is named “unexplainable difficulty spikes” that indicates a sudden difficulty increase and hence classified as low quality [2], [42]. Enemy, coins and hill in Fig. 7(II).3 are concentrated in a narrow zone in the middle of the segment, which is also regarded as low quality in literature [39]. Fig. 7(II).4 and Fig. 7(II).5 appear aesthetically unappealing by visual inspection.

By means of clustering results, we find that, to a great extent, the nature of the WRF accounts for misclassification as it needs to optimize the information gain in a statistical sense [31], [34]. We observe that game segments located nearby in the content space (i.e., game segments of a short distance) tend to be assigned the same label by our active learner. For instance, Fig. 7(I).5 is a negative example located in cluster 37. The rest of the segments from cluster 37 are also assigned as negative by our classifier. A similar problem occurs on Fig. 7(I).2 and Fig. 7(I).4. In addition, segments of similar content but distributed in different clusters are also likely to be misclassified. For instance, Fig. 7(N).4 is similar to Fig. 7(II).4 and Fig. 7(II).5 as they all have boxes above gaps, tubes and enemies, but these segments are located in different regions of content space due to the combination with other design elements. Likewise, Fig. 7(I).1 and Fig. 7(I).3 are in a similar situation. Such segments look similar with human visual inspection but often spread over different regions in the content space. This observation resulting from clustering analysis suggests that we are encountering a well-known yet challenging multi-modal classification problem where data within a specific class may distribute in different clusters [31], and it is hard for a classifier including the WRF to yield the error-free performance. Regardless of the WRF, “rare segments”, e.g., Figs. 7(II).1-3, are highly prone to misclassification as such segments are scattered widely with low density in the content space and hence less likely to be drawn in queries during active learning.

As a WRF can automatically find proper content features that maximize the information gain [34], we use the WRF to measure and rank the importance of content features in our CP learning. As a result, Table IV lists the top 20 most important features. It is observed from Table IV that the position and geometrical information on game elements, e.g., their width and height, are among the most important features in our data-driven quality evaluation. Moreover, we find that the first design element, e.g., gap, hill, or enemy, plays a

<table>
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<tr>
<th>Rank</th>
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<th>Rank</th>
<th>Description</th>
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<td>width of the 1st hill</td>
<td>11</td>
<td>width of the 1st box</td>
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<tr>
<td>2</td>
<td>y coordinate of the 1st box</td>
<td>7</td>
<td>type of the 1st cannon</td>
<td>12</td>
<td>number of enemies</td>
</tr>
<tr>
<td>3</td>
<td>x coordinate of the 1st hill</td>
<td>8</td>
<td>y coordinate of the 1st box</td>
<td>13</td>
<td>y coordinate of the 1st hill</td>
</tr>
<tr>
<td>4</td>
<td>height of the 1st hill</td>
<td>9</td>
<td>width of the 2nd coin</td>
<td>14</td>
<td>width of the 1st enemy</td>
</tr>
<tr>
<td>5</td>
<td>number of hills</td>
<td>10</td>
<td>x coordinate of the 1st box</td>
<td>15</td>
<td>y coordinate of the 1st tube</td>
</tr>
<tr>
<td>6</td>
<td>y coordinate of the 1st enemy</td>
<td>11</td>
<td>number of enemies</td>
<td></td>
<td></td>
</tr>
<tr>
<td>7</td>
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<td>12</td>
<td>number of enemies</td>
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<td></td>
</tr>
<tr>
<td>8</td>
<td>type of the 1st cannon</td>
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<td>x coordinate of the 2nd box</td>
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<td>width of the 2nd box</td>
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</tr>
<tr>
<td>12</td>
<td>number of enemies</td>
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<td>13</td>
<td>x coordinate of the 2nd box</td>
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<tr>
<td>14</td>
<td>y coordinate of the 2nd hill</td>
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</tr>
<tr>
<td>15</td>
<td>y coordinate of the 1st tube</td>
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</tr>
<tr>
<td>16</td>
<td>width of the 2nd box</td>
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<tr>
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<td></td>
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</tr>
<tr>
<td>20</td>
<td>y coordinate of the 2nd coin</td>
<td></td>
<td></td>
<td></td>
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</tr>
</tbody>
</table>

Fig. 7. Test game segments labeled by our classifier. (T) Correctly classified positive segments. (I) Segments leading to type-I error. (N) Correctly classified negative segments.(II) Segments leading to type-II error.
more important role than the subsequent design elements in a segment (c.f. Sect. III-B). Due to the nature of the WRF, those content features often lead to small information gain and are hence likely to have a low importance score.

In summary, the above experimental results demonstrate that the evaluation function learned from the sum total of 2,100 labeled game segments (1,300 for active learning and 800 for validation) effectively eliminates low quality game segments in terms of its performance on the validation set.

B. Quality Assessment of Constructive Primitives

While the effectiveness of our data-driven evaluation function has been assessed from a machine learning perspective in Sect. V-A, we further examine the quality of CPs generated with this evaluation function by using a number of generic yet objective content quality measurements that have been already validated thoroughly in [39].

In our experiment, we employ the objective quality metrics [39] that statistically measure content quality based on a number of procedural levels generated by a level generator, including strategic resource control ($f_s$), area control ($f_a$), area control balance ($b_a$), and exploration ($E$). Among these metrics, $f_s$ measures how close treasures, e.g., coins, boxes, are to enemies; $f_a$ measures how far the placement of design elements, e.g., enemies, tubes, cannons, are away from each other; $b_a$ measures how balanced a distribution of design elements is; and $E$ measures the exploration efforts to reach the exit from entrance. To a great extent, $E$ indicates the content geometric complexity. In our experiment, the $E$ scores are normalized to the range of $[0,1]$. The formal definition of these metrics can be found in [39]. Apart from above metrics, we further use Peter Lawford’s A* agent [36] to evaluate the playability ($P$) of game levels as this agent can survive on almost all playable levels regardless of their difficulty levels.

As a CP is a short game segment rather than a complete level, it is impossible to make a direct comparison between CPs and complete levels produced by other level generators. To enable the comparison, we generate a complete level by cascading CPs or game segments. In our experiments, we thus generate two sets of procedural levels: Sets A and B. In Set A, a level is composed of randomly selected CPs that are classified as high quality by our data-driven evaluation function, while a level in Set B consists of those randomly generated game segments that survive from conflict resolution rules but are rejected by our evaluation function. For a thorough evaluation, we compare our approach with those sophisticated SMB level generators, Notch [5] and Grammar Evolution (GE) [35], as well as several generators developed for Mario AI Championship [11]. Each of generators including ours generates 100 procedural levels for evaluation where a level has a size of 200 in width and 15 in height. In other words, a CP-based level is composed of 10 game segments of equal size: eight CPs, one initial and one ending segments. In our experiments, the default parameters as suggested in their works are always used for a fair comparison.

We conduct a Wilcoxon rank sum test to confirm a hypothesis that our CP-based levels in Set A outperform other SMB level generators stated above in terms of the aforementioned objective quality metrics (via a pairwise comparison). Fig. 8 shows the 95% confidence interval for the mean of quality scores in terms of different metrics. From Fig. 8, it is evident that our levels in Set A generally yield favorable results in terms of different metrics. Our levels in Set A result in a higher $f_s$ score than those generated by all others apart from GE. This suggests that acting as their “guardians”, treasures, e.g., coins and boxes, in our CP-based levels are close to enemies [39]. Our levels in Set A further lead to a higher $f_a$ score than all others and a $b_a$ score not lower than all apart from Shimizu’s, Takahashi’s and Baumgarten’s, which implies that design elements, e.g., enemies, tubes, cannons, in our CP-based levels are reasonably distributed in light of balance. As described in Sect. III-D3, resource balance is one of our labelling criteria, which accounts for higher $f_a$ and $b_a$ scores on Set A over Set B. In general, $E$ reflects the complexity of game geometry. The $E$ scores of levels in Sets A and B appear relatively low due to the content space adopted in our experiments (c.f. Sect. III-B), e.g., there are two hills at most, which leads to less complex levels than those used in other works. For playability measured by $P$, our levels in Sets A along with Notch’s and Takahashi’s levels do not produce unplayable levels while others do in this experiment. The much higher $P$ value on Set A over Set B benefits from active learning as playability is considered in labelling segments for training examples.

In summary, this comparative study suggests that our data-driven evaluation function works well in generating quality game content. In particular, the substantial gain for levels in Set A over those in Set B clearly shows the effectiveness of our active learning in content quality assurance.

\[ \text{Fig. 8. Quality assessment results with different metrics for various SMB level generators.} \]
C. Results on Real-time DDA

According to [7], the use of agents for a DDA test may benefit from stable agents’ behavior, their diversified playing styles and a wide range of skills. In our simulations, we hence employ 14 sophisticated yet different SMB agents (submitted to the Gameplay track of the Mario AI Competition [36]), Lawford’s, Sloane’s, Baumgarten’s, Ellingsen’s, Lopez’s, Schumann’s, Polikarpov’s, Forward, Erickson’s, Perez’s, CyberNeuron, Scared, Tulacek’s and Oliveira’s agents, to test our CP-based real-time DDA algorithm. For performance evaluation, we use the completion rate and the online learning behaviour.

1) Completion Rate: Progression is one of the most commonly used criteria to evaluate a DDA algorithm [36]. As a result, we adopt completion rate, a variant of progress defined in [36], for performance evaluation. Completion rate refers to the ratio of the actual distance travelled over to the length of a game level being played; that is, the distance from the x-coordinate of the start to the x-coordinate where the player died divided by the total width of the level. For reliability, each of 14 agents plays on four sets of adaptive games generated by Algorithm 3 corresponding to different optimal survival rates, \( \theta_{opt} = 0.70, 0.80, 0.87, 0.95 \), where each set consists of 200 levels and a level is limited to a maximum length of 200. For a baseline, we also randomly generate 200 levels of the same size and refer them to static games as no DDA is applied and each agent also plays all the games in this static game set. Fig. 9 shows the 95% confidence interval for the mean of completion rates achieved by 14 agents on four aforementioned game sets. As shown in Fig. 9, Lawford’s, Sloane’s and Baumgarten’s agents outperform other agents in terms of the averaging completion rate thanks to the A* algorithm used in their implementation. Hence, we regard these three agents as “skillful players” and, accordingly, all the rest as “novices”. It is observed from Fig. 9 that our real-time DDA algorithm works well for all the novice agents given the fact that their completion rates on adaptive game sets are considerably higher than those on the static game set, which implies easier levels were dynamically generated to improve their performance. Nevertheless, the DDA performance varies for three skillful agents. While the completion rates of Baumgarten’s agent are achieved as expected, our algorithm does not work well for Lawford’s and Sloane’s agents. According to [36], these two
Fig. 11. Exemplar procedural levels generated by our CP-based DDA algorithm for 14 different agents when the optimal survival rate $\theta_{opt}$ is set to 0.8. (A) Lawford’s agent. (B) Sloane’s agent. (C) Baumgarten’s agent. (D) Ellingsen’s agent. (E) Lopez’s agent. (F) Schumann’s agent. (G) Polikarpov’s agent. (H) Forward agent. (I) Erickson’s agent. (J) Perez’s agent. (K) CyberNeuron agent. (L) Scared agent. (M) Tulacek’s agent. (N) Oliveira’s agent.
agents almost always survive from all the procedural levels regardless of difficulty. Thus, our algorithm hardly finds games from the current content space (c.f. Sect. III-B) to challenge them unless this content space is expanded by including much more difficult games. From Fig. 9, it is also evident that a higher value of $\theta_{opt}$ generally leads to a higher completion rate, which suggests our algorithm works properly for DDA.

2) Online Learning Behavior: We further examine the online learning behavior of our DDA algorithm with three representative agents: Oliveira’s, Lopez’s and Baumgarten’s agents. Oliveira’s and Lopez’s agents are novices but have different playing styles, while Baumgarten’s agent is a skillful player. In our simulation, each of three agents played in a gameplay episode consisting of 50 successive game levels generated by our DDA algorithm by setting $\theta_{opt}=0.80$ and 0.70, where a game level is composed of up to 10 CPs and, in other words, its length is limited to 200 at maximum. For comparison, three agents also played an episode of 50 randomly generated static game levels of the same length. For reliability, we repeated this simulation for 30 trials and the mean and the standard error of completion rates achieved by three agents are shown in Fig. 10.

From Fig. 10(A) and 10(C), it is seen that the averaging completion rates of Oliveira’s and Lopez’s agents are significantly higher than those on static games ($p<.005$ in both cases) after playing five and 14 game levels, respectively, thanks to the adaptation that generates the levels appropriate to Oliveira’s and Lopez’s agents. In contrast, the completion rates of Baumgarten’s agent gradually decrease as observed from Fig. 10(E) where the averaging complete rates on adaptive game levels are always significantly lower than those on their static counterparts after 17 levels were played ($p<.005$) thanks to the adaptation that keeps generating more and more difficult levels. From Fig. 10 (A), (C), and (E), it is also seen that the convergence time of Lopez’s and Baumgarten’s agents is longer than that of Oliveira’s agent since the survival rate of those two agents on static games is closer to the optimal survival rate $\theta_{opt}=0.80$. This suggests that the convergence time for a specific agent could be minimized by finding a proper yet personalized optimal survival rate $\theta_{opt}$. Furthermore, it is clearly seen from Fig. 10 that the game completion rates on adaptive games resulting from $\theta_{opt}=0.70$ are lower than those on their counterparts corresponding to $\theta_{opt}=0.80$ due to increasing difficulties in adaptive games for $\theta_{opt}=0.70$. The above simulation results indicate that our DDA algorithm is able to generate easy or challenging games flexibly by controlling the optimal survival rate $\theta_{opt}$.

For demonstration, we illustrate exemplified procedural levels generated by our DDA algorithm for 14 different agents in Fig. 11. In those levels shown in Fig. 11(A)-(C) for three skillful players, Lawford’s, Sloane’s and Baumgarten’s agents, there are more enemies, cannons and gaps than those generated for other 11 agents. Those levels shown in Fig. 11(D)-(K) are at the intermediate difficult level where there are several enemies, gaps, cannons and flower tubes, which tends to match their skill capacities of Ellingsen’s, Lopez’s, Schumann’s, Polikarpov’s, Forward, Erickson’s, Perez’s and CyberNeuron agents. In those levels shown in Fig. 11(L)-(N) for complete novices, Scared, Tulacek’s and Oliveira’s agents, there exist fewer enemies (two of the three levels have no enemies at all) than those generated for more skillful agents as illustrated in Fig. 11(A)-(K). It is observed from Fig. 11(L)-(N) that those levels generated for three complete novices are much less appealing than others. In our simulations not reported here due to the limited space, we notice that three complete novices generally do not perform well for most of game levels generated by all the SMB level generators described in Sect. V-B including ours in terms of game completion given the fact that they are very easily killed by gaps, enemies, tube flowers, and cannons due to a lack of required skills. To enable three complete novices of very limited skills to maintain a survival rate towards $\theta_{opt}=0.8$, our DDA algorithm has to find those CPs of few gaps without tube flowers, cannons, and enemies in constructing proper adaptive games, which is responsible for those unappealing levels shown in Fig. 11(L)-(N).

In summary, it is evident from the simulation results reported above that our CP-based DDA algorithm works effectively in dynamically adjusting the content difficulty in response to agents’ local performance of playing a level in real time.

VI. DISCUSSION

In this section, we discuss the issues arising from our work and relate ours to pervious works.

As elucidated in Sect. III-D, clustering analysis facilitates understanding our content space and generating a validation set for active learning. A fundamental requirement for effective active learning demands a validation set that consists of only a small number of representative game segments holding as many statistical properties of the content space as possible. There might be an alternative yet more efficient way1 to generate such a validation dataset. Instead of clustering analysis, one could apply their prior knowledge to choose several key content features and then use those features to partition the content space into a number of regions corresponding to different combinations of their feature values. Likewise, a validation set is formed by choosing a small number of segments from each of the different regions resulting from this partition. While the partition method is more efficient in generating a validation set, our statistical analysis on the representativeness [28], a measurement on the statistical properties that a sample inherits from the sampled population, suggests that a validation set generated with clustering analysis has higher representativeness than that yielded by the aforementioned content space partition method. Despite a computational burden, clustering

\footnote{1An anonymous reviewer suggested a partition method.}
analysis may be rewarded with a more informative validation set for active learning.

In terms of game content quality, automatically generated SMB levels are generally worse than those handcrafted levels [2]. Apart from constructive approaches reviewed in Sect. II, there are other approaches in SMB to address this issue but most of them handcraft evaluation functions for quality assurance, e.g., [35], [41], [42]. However, formulating a complete set of heuristic rules is challenging since game content is observable but less explainable and hard to abstract. Instead, Reis et al. [12] merged human-annotated game segments to form quality levels. Unlike ours, theirs has to make a great deal of effort in obtaining enough annotated segments for level generation and needs to address the controllability issue in addition. On the other hand, other researchers aim to generate high quality levels with human-authored levels rather than domain knowledge. Dahlskog and Togelius [16] used design patterns learned from human-authored SMB levels to generate levels. Snodgrass and Ontañón [43] learned Markov chains from human-authored SMB levels to formulate constructive rules for level generation. Summerville and Mateas [44] used the LSTM to learn sequences from existing human-authored procedural levels and the path information. However, formulating reliable yet effective constructive rules or diverse design patterns from human-authored levels without any domain knowledge might be very difficult since there are a limited number of such levels; there are only 32 human-authored levels in SMB [16], [43]. Thus, additional information, e.g., path information, has to be required to assure the playability of game levels [44]. In contrast, we explore and exploit the synergy between rule-based and learning-based methodologies to produce quality building blocks, constructive primitives. Our data-driven evaluation function implicitly encodes multiple quality-related criteria via developers’ visual inspection on training segments. Thus, our approach significantly distinguishes from handcrafting constraints, e.g., [35], [41], [42], formulating constructive rules, e.g., [6]–[9], and learning models/patterns from a limited number of human-authored levels [16], [40], [43], [44]. As a learning-based approach, however, ours does not yield the error-free performance, which implies low quality segments could appear in a procedural level. In general, different developers may have different opinions on game quality. Although this subjectivity is a general issue regardless of methodologies, our current work is limited as only one developer is employed to annotate data for active learning. Nevertheless, this issue may be tackled via crowdsourcing, which has been attempted in [12].

For real-time DDA, we hypothesize that there is a strong relationship between performance, e.g., survival rate, and gameplay experience based on the previous studies [18]–[20], [22]. Hence, we formulate our DDA as a binary reward MDP problem and solve it with Thompson sampling. It is noticed that some model-based approaches [25]–[27] proposed under other game genres also treat DDA an MDP problem. In their approach, however, the degree of player’s survival/winning rate, e.g., Q-learning and dynamic scripting, is not tunable directly. It is also unclear how to use these approaches to tackle a binary reward MDP problem. Nevertheless, our work in DDA is subject to a number of limitations: (a) our proposed DDA algorithm is model-based and the hypothesis based on psychological theories has yet to be confirmed by human players in SMB; b) the adaptation process does not seem rapid for agents; and (c) it still remains unknown on how to find a proper optimal survival rate for an individual player. In addition, our rule-based difficulty level definition for game segments (c.f. Table II) tends to explore the whole content space for generating diverse games but seem less accurate, which accounts for less stable performance in adaptation.

The previous works [8], [9] have investigated segment-based experience-driven content adaptation in SMB, where they learned a mapping from player’s behavior, e.g., playlog, and the segment properties, e.g., controllable parameters, onto the player’s affective states. By means of their methods, our CP-based DDA algorithm can be straightforwardly converted into a model-free algorithm for experience-driven DDA. Based on the experience on a CP self-reported by a player, we can establish a mapping function required by a model-free method in the same manner. Moreover, our CP-based generator could adapt game content even more easily since all the properties of game content can be directly controlled via CPs. Unfortunately, the existing model-free methods in SMB [8], [9] entirely rely on the self-reported feedback on short segments, which severely interrupts the gameplay experience [3]. Thus, such an extension does not seem promising. On the other hand, the use of subjective feedback on an entire procedural level has also been studied in SMB, e.g., [6], [7], [10], which could minimize interruption of the gameplay experience. Nevertheless, such techniques are not applicable to real-time DDA studied in this paper. Hence, it remains as an open problem how to adapt content via CPs in the presence of subjective feedback on an entire procedural level.

In conclusion, we have presented a novel approach to real-time DDA in SMB via learning constructive primitives and carried out a thorough evaluation. Experimental results suggest that our data-driven content quality evaluation function works well for content quality assurance and our CP-based DDA algorithm is capable of adjusting content difficulty in real time to match different agents’s performance. As our CPs are fully controllable, they are also applicable to online level generation in SMB as demonstrated in our previous work [21]. With the insight into CPs gained in this paper, our previous CP-based online SMB level generation method certainly needs to be further investigated for improvement. In our ongoing work, we are going to tackle all the remaining issues discussed above by exploring state-of-the-art machine learning techniques and alternative content representations. Furthermore, we would
explore the feasibility in extending our approach to other video game genres, e.g., first-person shooter.

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REFERENCES

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