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Time Reversal Technique based on Spatio-Temporal Windows for Through the Wall Imaging

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Abstract—Time Reversal (TR) imaging methods have recently generated considerable interest due to their robustness and ability to locate multiple targets. However, problems arise when the targets are behind an obstructing material. We develop a pre-processing algorithm for TR imaging methods to obtain images of targets hidden behind a wall, applying temporal and spatial windows on the full-Multistatic Data Matrix (MDM). By using temporal-windows, we divide the full-MDM into sub-MDMs. We further segment the sub-MDMs spatially by selecting its elements corresponding to a predetermined number of antennas in space. We take the singular value decomposition of the sub-MDMs to obtain singular value distributions as well as singular vectors which we analyse individually and use for the Multiple Signal Classification (MUSIC) TR imaging method. The obtained images from these localised sub-MDMs collectively yield to clearer images of scenarios than we can obtain using the full-MDM.

Index Terms—TR, MUSIC, MDM

I. INTRODUCTION

THE Time Reversal (TR) method which was first introduced in acoustics [1] has found applications in various disciplines ranging from non-destructive testing [2], underwater communications [3] [4] and medicine [5] [6]. TR has also been studied for Ground Penetrating Radar (GPR), Through the Wall Imaging (TWI) [7] and under lossy conditions [8] [9]. One of the main problems with GPR [10] [11] and TWI [12] [13] is performance degradation in the presence of clutter signal from an obstructing surface between the antennas and the targets. In [10], sliding spatial windows in GPR detect and localise dielectric targets shallowly buried in the ground. A study in TWI [14] is among other works [15] [16] using the target initial reflection method to locate a target hidden behind a brick wall. It was shown in [17] [18] that the Multiple Signal Classification (MUSIC) algorithm can be applied to locate spatially extended targets hidden behind a wall using beamforming. A recent study used TR to locate targets behind a wall by using a single antenna, as both a transmitter and a receiver, from multiple locations, under conditions for which the clutter contribution varies minimally with antenna location [19]. Hence, the signals received are added up making the clutter signal maximum as they are in phase. However the

configuration does not obtain a full-Multistatic Data Matrix (MDM) and hence, its application is limited. The two-stage MUSIC algorithm proposed in [20] is useful for identifying a weak targets, the responses from which have been masked due to clutter signal from an obstacle (a stronger scatterer). However the algorithm assumes having prior knowledge of the radii of the targets.

We propose a novel TR based imaging algorithm utilising simultaneously both temporal and spatial windows with which the TR-MUSIC method [21] produces better images of the medium of interest than is possible with the full-MDM in the presence of clutter. Our algorithm involves the partitioning of the elements of the full-MDM and hence the signals, to create multiple sub-MDMs which give a clearer picture of the medium than the full-MDM when used with the MUSIC method. Furthermore the spatio-temporal windows isolate the responses from targets at different times and locations in the scenario and we obtain localised information in time and space. Hence signals from the targets closer to the Time Reversal Array (TRA) antenna are contained in the earlier time-windows while signals from targets further away are contained in the later time-windows. We consider a scenario containing a target located behind a brick wall and introduce our spatio-temporal window imaging algorithm to the TR methods to locate the target and get an image of the scenario. We explain the our algorithm and discuss its application to the MUSIC methods in Section II. In Section III, we analyse the results obtained by firstly, applying our algorithm to a scenario with a well resolved target and then a case with the target closer to the wall, where clutter and target signals overlap. Finally we emphasize the advantage of the spatial windows by applying our algorithm to a scenario with two targets.

II. THE SPATIO-TEMPORAL WINDOW ALGORITHM

The Decomposition Of the Time-Reversal Operator (DORT in its French acronym) and MUSIC methods [22] [23] [24] [25] are TR techniques which take advantage of the TR invariance. These methods utilise singular vectors of the MDM, whose elements $k_{s,r}(t)$, are obtained by transmitting a signal from N TRA antenna elements, one at a time, and recording the response signal in the medium at all antennas, where s is the transmitting antenna and r is the receiving antenna. The distance between the antennas are assumed to be equally spaced. The full-MDM, $\mathbf{K}(t)$, which contains vital information about the targets in the medium, is represented by $\mathbf{K}(\omega)$ in the frequency domain. The singular value decomposition (SVD) of $\mathbf{K}(\omega)$ gives the singular values $\Lambda(\omega)$ as well as

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Fig. 1. The geometry of the FDTD scenario with one PEC sphere behind a brick wall

Fig. 2. The signal observed at the first antenna in Fig. 1 when a pulse was transmitted from the same antenna and line-of-sight signal is removed and the time-windows which sum to give a magnitude of 1

unitary matrices $\mathbf{U}(\omega)$ and $\mathbf{V}(\omega)$ which contain the left and right singular vectors respectively.

Due to the presence of clutter signal in $\mathbf{K}(t)$, the singular value distribution as well as the phase and magnitude distributions of the singular vectors obtained from SVD are greatly distorted and difficult to analyse. The reflections from the wall dominate the MDM in power which is crucial for the application of the MUSIC methods. Consequently, the ability of TR-MUSIC methods to localise the target is adversely affected. By using temporal and spatial windows, we separate the signals contained in the $\mathbf{K}(t)$, to multiple sub-MDMs. The SVD of the sub-MDMs gives singular values and singular vectors which we use with the TR imaging methods to create images. Hence, rather than the global information contained in the full-MDM, we obtain localised information from various

parts of the scattering medium in the sub-MDMs, which reduces the number of targets to be detected at one time. Some of the benefits of localised information have already been shown in [10].

A. Temporal-windowing

We select the Hanning window [26] as our time-window. By subsequent time-shifting, we obtain temporal-windows to completely cover the whole signal duration of interest. The m th time-window is obtained as

$$W_m(t) = 0.5 \left(1 - \cos \left(\frac{2\pi(t-\tau_m)}{P} \right) \right) \quad (1)$$

for $\frac{P(m-1)}{2} \leq t \leq P + \frac{P(m-1)}{2}$ and otherwise $W_m(t) = 0$, where τ_m is the time shift and P is the window interval. In order to avoid loss of data, the time-windows are shifted in time from one another to ensure that the addition of the time-windows gives a magnitude of 1. Hence, the time shift is defined as $\tau_m = \frac{P(m-1)}{2}$ ($1 \leq m \leq M$) where $M = \lfloor \frac{T}{P \cdot 0.5} - 1 \rfloor$ is the number of time-windows needed to cover the time simulated, T , for the scenario, and $\lfloor \cdot \rfloor$ represents a floor function that maps a real number to the largest previous integer.

Fig. 2 shows signal $k_{1,1}(t)$ and the Hanning time-windows as well as their summation which yields a magnitude of 1 ensuring that no vital information is lost from the full-MDM. By multiplying the Hanning windows $W_m(t)$ by the elements of the full-MDM $k_{s,r}(t)$, one at a time, we obtain M sub-MDMs as

$$\mathbf{K}_m(t) = \begin{pmatrix} k_{1,1}(t)W_m(t) & \dots & k_{1,N}(t)W_m(t) \\ \vdots & \ddots & \vdots \\ k_{N,1}(t)W_m(t) & \dots & k_{N,N}(t)W_m(t) \end{pmatrix}. \quad (2)$$

B. Space-windowing

We further segment $\mathbf{K}_m(t)$ in space by selecting elements of $\mathbf{K}_m(t)$ obtained from a set of N_s antennas where $1 \leq N_s \leq N$. Hence, for $\mathbf{K}_m(t)$, we obtain the l th sub-MDM as

$$\mathbf{K}_{m,l}(t) = \begin{pmatrix} k_{l,1}(t)W_m(t) & \dots & k_{l,L}(t)W_m(t) \\ \vdots & \ddots & \vdots \\ k_{L,l}(t)W_m(t) & \dots & k_{L,L}(t)W_m(t) \end{pmatrix} \quad (3)$$

where $L = N_s - 1 + l$ and $1 \leq l \leq N + 1 - N_s$.

C. Setting the Window parameters

The effectiveness of the spatio-temporal window algorithm depends on the size of the time-window P and space-window N_s . A very small time-window ($P \ll$ the excitation pulse width) means that $\mathbf{K}_{m,l}(t)$ does not provide enough signal diversity to obtain reasonable images. However if P is large enough for a single $\mathbf{K}_{m,l}(t)$ to contain the entire information of the full-MDM, then the algorithm reduces to the standard

TR imaging. Assuming the excitation pulse width is Υ , the minimum size of the time-window is chosen to be Υ . Hence

$$P \geq \Upsilon. \quad (4)$$

This ensures that a single time-window covers the initial excitation signal transmitted from the TRA antennas.

Furthermore the minimum value of N_s for each scenario is dictated by the signal to null subspace threshold obtained from the full-MDM. Since the MUSIC methods utilise the singular vectors in the null subspace, N_s should be greater than the number of singular values in the signal subspace N_t of the full-MDM to ensure that we retain noise in the sub-MDMs. Therefore

$$N_s > N_t. \quad (5)$$

D. Utilising the sub-MDMs

By performing the FFT on the elements of sub-MDM $\mathbf{K}_{m,l}(t)$ we obtain $\mathbf{K}_{m,l}(\omega)$. Furthermore the SVD on $\mathbf{K}_{m,l}(\omega)$ gives

$$\mathbf{K}_{m,l}(\omega) = \mathbf{U}(\omega, m, l) \mathbf{\Lambda}(\omega, m, l) \mathbf{V}^*(\omega, m, l) \quad (6)$$

where $\mathbf{\Lambda}(\omega, m, l)$ are $N_s \times N_s$ real diagonal matrices containing the singular values in descending order and, $\mathbf{U}(\omega, m, l)$ and $\mathbf{V}(\omega, m, l)$ are $N_s \times N_s$ unitary matrices containing the left and right singular vectors of $\mathbf{u}_n(\omega, m, l)$ and $\mathbf{v}_n(\omega, m, l)$ for $1 \leq n \leq N_s$, respectively. We know $\mathbf{u}_n(\omega, m, l) = \mathbf{v}_n^*(\omega, m, l)$ when $\mathbf{K}_{m,l}(\omega)$ is symmetric [22].

The singular vectors obtained from $\mathbf{K}_{m,l}(\omega)$ are used to create images of the scenario using the TR-MUSIC method. The MUSIC method involve obtaining the scalar product of the singular vectors and the steering vectors $\mathbf{g}(\bar{\mathbf{r}}, \omega)$. The steering vectors represent the relative phase shifts from the spatial location, $\bar{\mathbf{r}}$, to the centre of the TRA antennas a wave experiences through the medium, where $\bar{\mathbf{r}} = x\mathbf{i} + y\mathbf{j}$. $\mathbf{i}$ and $\mathbf{j}$ are unit vectors in the x and y directions, respectively. We assume the target is in free space. The MUSIC method utilises singular vectors in the null subspace rather than the signal subspace. The singular vectors in the signal subspace correspond to the significant singular values. The ratio of consecutive singular values corresponding to singular vectors in the same subspace (either signal or null subspace) tends to be lower than the ratio of consecutive singular values whose corresponding singular vectors are in different subspaces. Hence, for $\mathbf{K}(\omega)$, we can say the singular vectors, corresponding to the first $N_t(\omega)$ singular values, are in the signal subspace if $N_t(\omega)$ satisfies

$$\frac{\lambda_{N_t(\omega)}(\omega)}{\lambda_{N_t(\omega)+1}(\omega)} = \max_{1 \leq n \leq N-1} \left(\frac{\lambda_n(\omega)}{\lambda_{n+1}(\omega)} \right). \quad (7)$$

We consider the Centre Frequency (CF) MUSIC and Ultra-WideBand (UWB) MUSIC methods [22] to utilise the singular vectors from the sub-MDMs. The MUSIC methods are capable of locating non-resolved targets as long as the number of targets is less than the number of antennas [25]. The UWB methods provide statistical stability which the CF methods do not in random media. By using the null subspace singular vectors from the sub-MDMs for the MUSIC methods we obtain

the sub-CF-MUSIC and sub-UWB-MUSIC imaging functionals. We define the total sub-CF-MUSIC imaging functional as the summation of all sub-CF-MUSIC imaging functionals to obtain

$$\mathbf{M}_\Gamma(\bar{\mathbf{r}}, \omega_c) = \sum_{l=1}^L \sum_{m=1}^M \left[\sum_{n=N_t(\omega_c)+1}^{N_s} \mathbf{g}(\bar{\mathbf{r}}, \omega_c) \cdot \mathbf{u}_n(\omega_c, m, l) \right]^{-1} \quad (8)$$

where ω_c is the centre frequency of interest. Similarly, the summation of the sub-UWB-MUSIC imaging functionals gives the total sub-UWB-MUSIC imaging functional as

$$\mathbf{M}_{\Gamma_{UWB}}(\bar{\mathbf{r}}) = \sum_{l=1}^L \sum_{m=1}^M \left[\int_{\Omega} \sum_{n=N_t(\omega)+1}^{N_s} \mathbf{g}(\bar{\mathbf{r}}, \omega) \cdot \mathbf{u}_n(\omega, m, l) d\omega \right]^{-1} \quad (9)$$

where Ω is the frequency range of interest.

III. NUMERICAL SIMULATIONS

A. The FDTD scenario with one well-resolved target

Fig. 1 shows the geometry of a scenario with one well-resolved PEC sphere, whose radius is 15 mm and conductivity is 10^7 S/m, in a homogeneous medium (free-space) hidden behind a brick wall. A 300×300 2D FDTD space was used for the numerical simulation. The FDTD parameters for the brick wall are 0.02 S/m for conductivity and 3.8 for relative permittivity. The aim of this experiment is to locate the PEC sphere, assuming the location of the target is unknown despite the presence of an obstructing brick wall. A first derivative of Gaussian pulse, with a centre frequency of 2 GHz, is transmitted from $N = 13$ TRA antenna elements, one at a time. The frequency range of interest is $f_1 \leq f \leq f_2$ where f_1 and f_2 satisfy $S(f_1) = S(f_2) = 0.1$ and $S(f)$ is the normalised spectrum of the excitation signal. The excitation used in this paper gives $f_1 = 0.3$ GHz to $f_2 = 4.8$ GHz. The TRA antennas, parallel to the wall and half a wavelength at 2 GHz apart from each other, were used to record signals which give the full-MDM $\mathbf{K}(t)$, containing information from the target as well as clutter signal from the brick wall. In this numerical simulation, actual antennas are not modelled but instead soft point sources [27] and observation points were used to mimic antennas. By applying the time-windows and space-windows to full-MDM $\mathbf{K}(t)$ we obtain sub-MDMs $\mathbf{K}_{m,l}(t)$. (5) with $\varsigma = \frac{\lambda}{2}$ gives $N_s \geq 3$.

Fig. 3 shows the singular value distribution of the full-MDM. Fig. 3(a) and (b) show the singular value distribution across the frequency range and at the centre frequency of interest, respectively. When (7) is applied to Fig. 3(b) we obtain $N_t(\omega_c) = 2$ which is used in (8).

Fig. 4 shows the CF-MUSIC and UWB-MUSIC (from 0.3 to 4.8 GHz) images obtained for the scenario in Fig. 1 using the full-MDM while Fig. 5 shows the total sub-CF-MUSIC and total sub-UWB-MUSIC (from 0.3 to 4.8 GHz) images when $P = \Upsilon$ and $N_s = 7$.

Fig. 3. Singular value distribution of the full-MDM for the scenario in Fig. 1 (a) over the frequency range of interest, (b) at the centre frequency ω_c

Fig. 4. The CF-MUSIC and UWB-MUSIC images produced using the full-MDM, where $\times$ represents the TRA antennas' locations and $\circ$ represents the target location

Fig. 5. The total sub-CF-MUSIC and total sub-UWB-MUSIC images produced when $P = \Upsilon$ and $N_s = 7$, where $\times$ represents the TRA antennas' locations and $\circ$ represents the target location

Fig. 6. The normalised cross section at $y = 1.15\text{m}$ in Fig. 4 and Fig. 5 obtained using the full-MDM MUSIC method, the total sub-MUSIC method and the reference

Fig. 6 shows the cross section of Fig. 4 and Fig. 5 obtained using the full-MDM MUSIC method, the total sub-MUSIC

Fig. 7. The total sub-CF-MUSIC and total sub-UWB-MUSIC cross range resolution at half maximum of $M_\Gamma(\bar{r}, \omega_c)$ and $M_{\Gamma_{UWB}}(\bar{r})$ at $y = 1.15\text{m}$, varying N_s and P

Fig. 8. The accuracy of the total sub-CF-MUSIC and total sub-UWB-MUSIC imaging functional in locating the PEC target when N_s and P are varied

method and the cross section of the image of a reference. We obtain the reference by implementing standard TR imaging with the full-MDM on a scenario similar to Fig. 1 but without a wall. Hence, the reference has the best possible resolution attainable for the MUSIC methods. As in Fig. 4 the full-MDM did not detect the target. However the total sub-CF-MUSIC and total sub-UWB-MUSIC imaging functional yield images that accurately locate the target despite the loss of resolution from the reduced TRA antenna aperture and time-windows.

Fig. 7 shows the cross range resolution of the total sub-CF-MUSIC and total sub-UWB-MUSIC images at $y = 1.15\text{m}$, varying N_s and P . We obtain the cross range resolution at half maximum of $M_\Gamma(\bar{r}, \omega_c)$ and $M_{\Gamma_{UWB}}(\bar{r})$ at the corresponding cross section. Fig. 8 shows the accuracy of the total sub-CF-MUSIC and total sub-UWB-MUSIC images in locating the PEC target, varying N_s and P . We define the accuracy as the distance between the location of the maximum of $M_\Gamma(\bar{r}, \omega_c)$ or $M_{\Gamma_{UWB}}(\bar{r})$ and the actual location of the PEC target. We observe that we retain the accuracy and the resolution of the images as we initially increase the size of the time-windows P . However, when P gets large enough for a single sub-MDM to contain the entire information of the full-MDM, the algorithm reduces to the standard TR imaging and we are unable to locate the target due to clutter. We observe from Fig. 7 that for a scenario with a single PEC target we attain higher resolution as we increase size of the spatial windows N_s due to the increase in aperture. However the advantage of spatial windows is

Fig. 9. Signals observed at (a) the first antenna when a pulse was transmitted from the same antenna ($k_{1,1}(t)$) and (b) the thirteenth antenna when a pulse was transmitted from the first antenna ($k_{1,13}(t)$) with the line-of-sight signal removed

Fig. 10. The CF-MUSIC and UWB-MUSIC images produced using the full-MDM, where $\times$ represents the TRA antennas' locations and $\circ$ represents the target location

Fig. 11. The total sub-CF-MUSIC and total sub-UWB-MUSIC images produced when $P = \Upsilon$ and $N_s = 7$, where $\times$ represents the TRA antennas' locations and $\circ$ represents the target location

emphasized in scenarios containing multiple targets as shown in Section III-C.

B. Scenario with clutter and target signal overlapped

We simulate a scenario, with overlap between clutter signal and target signal in the full-MDM, by moving the target, shown in Fig. 1, 0.4 m towards the brick wall. Fig. 9 shows $k_{1,1}(t)$ and $k_{1,13}(t)$ from the full-MDM obtained from the scenario with clutter and target signal overlapped. The spatio-temporal windows are applied to the full-MDM to obtain sub-MDMs $K_{m,i}(t)$.

Fig. 10 shows the CF-MUSIC and UWB-MUSIC (from 0.3 to 4.8 GHz) images obtained for the scenario using the full-

Fig. 12. The normalised cross section at $y = 0.75\text{m}$ in Fig. 10 and Fig. 11 obtained using the full-MDM MUSIC method, the total sub-MUSIC method and the reference

Fig. 13. The geometry of the FDTD scenario with two PEC sphere behind a brick wall

MDM. Fig. 11 shows the total sub-CF-MUSIC and total sub-UWB-MUSIC (from 0.3 to 4.8 GHz) images obtained for the scenario, with clutter and target signal overlap, when $P = \Upsilon$ and $N_s = 7$.

Fig. 12 shows the cross section of Fig. 10 and Fig. 11 obtained using the full-MDM MUSIC method, the total sub-MUSIC method and the cross section of the image of a reference. The total sub-MUSIC functionals give images that accurately locate the target.

C. Scenario with two targets

The advantage of spatial windows is emphasized when we apply the temporal and spatial window imaging algorithm to a scenario containing multiple targets. Fig. 13 shows the geometry of a scenario with two well-resolved PEC spheres in a homogeneous medium (free-space) hidden behind a brick wall.

Fig. 14 shows the total sub-CF-MUSIC and total sub-UWB-MUSIC (from 0.3 to 4.8 GHz) images obtained for the scenario in Fig. 13 when $P = 8 \cdot \Upsilon$ and $N_s = 7$. The images locate the targets which is not achieved by the Full-MDM.

Fig. 15 and Fig. 16 shows the cross range resolution of the total sub-CF-MUSIC and total sub-UWB-MUSIC images at

Fig. 14. The total sub-CF-MUSIC and total sub-UWB-MUSIC images produced when $P = 8 \cdot \Upsilon$ and $N_s = 7$, where $\times$ represents the TRA antennas' locations and $\circ$ represents the location of targets

Fig. 15. The total sub-CF-MUSIC and total sub-UWB-MUSIC cross range resolution at half maximum of $M_\Gamma(\bar{r}, \omega_c)$ and $M_{\Gamma_{UWB}}(\bar{r})$ at $y = 1.15\text{m}$, varying N_s and P

Fig. 16. The total sub-CF-MUSIC and total sub-UWB-MUSIC cross range resolution at half maximum of $M_\Gamma(\bar{r}, \omega_c)$ and $M_{\Gamma_{UWB}}(\bar{r})$ at $y = 1.25\text{m}$, varying N_s and P

$y = 1.15\text{m}$ where PEC target 1 is located and at $y = 1.25\text{m}$ where PEC target 2 is located, varying N_s and P . We observe that as we increase P , we retain the resolution of the images until the algorithm reduces to standard TR problems. Fig. 15(a) shows that we obtain the highest resolution for PEC target 1 when $N_s = 3$ and $P = 8 \cdot \Upsilon$ for the total sub-CF-MUSIC image while Fig. 15(b) shows that we obtain the highest resolution when $N_s = 5$ and $P = 4 \cdot \Upsilon$ for the total sub-UWB-MUSIC image. Similarly, Fig. 16(a) shows that we obtain the highest resolution for PEC target 2 when $N_s = 3$ and $P = 4 \cdot \Upsilon$ for the total sub-CF-MUSIC image

Fig. 17. The geometry of the FDTD scenario with one PEC sphere and one extended target behind a brick wall

Fig. 18. Singular value distribution of the full-MDM for the scenario in Fig. 17, (a) over the frequency range of interest, (b) at the centre frequency ω_c

while Fig. 16(b) shows that we obtain the highest resolution when $N_s = 11$ and $P = 8 \cdot \Upsilon$ for the total sub-UWB-MUSIC image. Hence, Fig. 15 and Fig. 16 demonstrate that we can locate the targets with increased resolution, when the time windowed sub-MDMs are further segmented by spatial windows, despite the reduction of the TRA antenna aperture as a negative effect. The spatial windows further segregate the signals from different target into different sub-MDMs, leading to images which more accurately represent the scenario.

Fig. 17 shows the geometry of a scenario identical to Fig. 13 containing one PEC sphere whose radius is 15 mm and one extended PEC target added, whose length is 0.2 m and width is 1.5 cm, in a homogeneous medium (free-space) hidden behind a brick wall. Fig. 18 shows the singular value distribution of the full-MDM obtained for the scenario in Fig. 17. Fig. 18(a) and (b) show the singular value distribution across the frequency range and at the centre frequency of interest, respectively. Although extended scatterers in freespace tend to produce a smooth change in the singular values, the presence of the wall, which is also an extended scatterer, close to the TRA antennas dominates the singular value distribution

Fig. 19. The total sub-CF-MUSIC and total sub-UWB-MUSIC images produced when $P = 8 \cdot \Upsilon$ and $N_s = 11$, where $\times$ represents the TRA antennas' locations and $\circ$ and $\square$ represent the location of targets

regardless of the targets behind the wall. Hence by applying (7) to Fig. 18(b) we obtain $N_t(\omega_c) = 2$ which is used in (8). Fig. 19 shows the total sub-CF-MUSIC and total sub-UWB-MUSIC (from 0.3 to 4.8 GHz) images obtained for the scenario in Fig. 17 when $P = 8 \cdot \Upsilon$ and $N_s = 11$. We observe from the images that our algorithm locates the PEC sphere and the presence of an extended target which is not achieved using the Full-MDM for the MUSIC method.

IV. CONCLUSION

The TR-MUSIC imaging methods suffer in performance when there is significant clutter in the full-MDM due to an obstruction between the TRA antennas and the target. We developed and applied a spatio-temporal window algorithm to extract information on targets by segmenting the full-MDM into sub-MDMs. Using sub-MDMs, we obtained images that localised the targets hidden behind a brick wall which is not possible through the classical utilisation of the full-MDM.

In the future, more complex scenarios containing multiple targets with a wall containing metallic rebars can be considered as they produce extra scattering which may benefit the resolution by enhancing the effective aperture [28]. Additionally, the impact of randomness in the background medium and dispersion in the wall media can be considered as an extension of the current work.

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