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DAMAGE AND FAILURE ANALYSIS OF CONCRETE USING SYNTHETIC 3D MESO-STRUCTURES

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ABSTRACT

Concrete is one of the key materials used in the construction of nuclear power plants, with both structural and shielding functions. Understanding the aging of concrete in service is essential prerequisite for advanced plant life assessment. Aging is associated with changes in the complex heterogeneous structure of concrete, which could be chemically and/or mechanically driven. First steps towards modelling and predicting aging can be made by appropriate representations of concrete at its meso-structural length scale, where it is a three-phase composite, containing mortar, coarse aggregates and voids. This work presents generation and packing algorithms for modelling three-dimensional heterogeneous concrete specimens with randomly distributed spherical, ellipsoidal and polyhedral aggregates and voids, with prescribed size distributions, shape and volume fraction. Models are meshed automatically and include cohesive elements at all interfaces between continuum elements. The cohesive elements represent potential crack paths and their traction-separation laws are different within the mortar, within the aggregates and at the interface between these phases. Mesoscale crack initiation, propagation and coalescence are simulated naturally with the cohesive elements. The models are solved by FEM, and statistically analysed to evaluate the effects of mesostructural parameters on the mechanical behaviour. The proposed methodology provides an effective and efficient tool for damage and failure analysis of concrete, and a comprehensive study was conducted for 3D heterogeneous concretes in this paper.

INTRODUCTION

Concrete is the most widely used construction material in the field of civil engineering due to its good strength and durability relative to its cost. Understanding the characteristics of concrete is essential prerequisite for building construction assessment. Due to its multi-phase composition and quasi-brittle mechanical behaviour, modelling of concrete for structural engineering analysis has been a classical challenge for several decades, and up to now many details such as strain softening, micro-crack propagation, failure mechanisms and size effects are still far from being fully understood.

An extensive literature review recently carried out by Wang et al. (Wang et al., 2015b) shows that numerical image processing technique and parameterization modelling technique are two main approaches to generate a meso-structure model of concrete. Although the mesh generated from images is closest to nature, it is presently very expensive and time-consuming to generate sufficient scanned images from samples to make meaningful statistical analyses (e.g. Man, 2010; Roubin et al., 2014), especially for 3D problems. In the parameterization modelling technique, both direct (e.g. López et al., 2007; Wang et al., 2015b; Wang et al., 2015a) and indirect approaches (e.g. Jivkov and Yates, 2012; Reichert, 2009; Leite et al., 2004; Jivkov and Xiong, 2014) to characterize material random heterogeneity have been used. The indirect approach is able to generate a large number of samples with ease but the key multi-phasic parameters which could significantly influence the mechanical behaviour cannot be considered. The direct approach can take into account most of the key parameters such as shape, size, gradation and spatial distribution of voids and aggregates, phase volume fractions and aggregate-mortar interfaces. So
among all the approaches, it seems that the direct approach is particularly suitable for statistical analysis of concrete samples, and was used in this work.

For meso-structure models of concrete, identification and generation of unit cell geometry is a vital step, aggregates are usually assumed to be spherical for simplicity, as presented in Bazant et al., 1990 and Wriggers and Moftah, 2006. In recent years, considerable attention has been paid to generate various aggregate shapes, e.g., ellipsoidal aggregates using functions with varying parameters (Liu et al., 2014), and polyhedral aggregates by random packing systems (Khelifa and Guessasma, 2013) and Voronoi tessellation methods (Caballero, 2005). It is worth noting that most of the existing meso-structure models of concrete only consider random aggregates (López et al., 2007; Caballero, 2005) but neglect voids. However, X-ray computed tomography (XCT) images of concrete (Landis and Keane, 2010; Man, 2010) clearly show that voids exist in concrete at mesoscale. It is therefore imperative to develop a procedure for automatic generation of morphological details of materials with both randomly distributed aggregates and voids of different shapes.

Several numerical models for crack propagation at mesoscopic level have been used to study the heterogeneity of concrete. Continuum based finite element models are the main approaches employed in the literature (Kwan et al., 1999; Hordijk, 1992). Other alternative approaches have also been developed, such as discrete element model (DEM) (Shiu et al., 2008) and lattice model (Reichert, 2009; Jivkov, 2014). A key issue associated with the DEM and lattice model is the difficulty in determining the equivalent model parameters, which is relatively straight forward for continuum based FE models (Tu and Lu, 2011). The numerical model used in this work for crack propagation at mesoscopic level is based on the cohesive zone model (Wang et al., 2015b). It is becoming more and more popular in modelling crack propagation due to its simple formation, easy implementation in the form of cohesive interface elements (CIEs).

The aim of this work is to develop a holistic procedure for analysis of meso-structure and local properties effects on the macroscopic behaviour of concrete. Firstly, an in-house program HMG (heterogeneous material generator) consisting of particle generation and packing is developed and applied to generate 3D meso-structures of concrete with randomly distributed spherical, ellipsoidal and polyhedral aggregates and voids, respectively. Secondly, interfaces between all aggregate-aggregate, mortar-mortar and aggregate-mortar continuum elements are represented by zero thickness cohesive elements via an in-house program CIEIN (cohesive interface elements insertion). Non-linear cohesive laws for the three types of interfaces are implemented. Thirdly, MCS (Monte Carlo Simulations) are carried out to investigate mechanical behaviour of concrete in a quantitative manner. The outcomes are presented comprehensively and provide valuable information for improved understanding of damage and failure mechanisms of concrete.

MESO-STRUCTURES OF CONCRETE

The aggregate size distributions found in Hirsch (Hirsch, 1962) and summarised in Table 1 is used in this study. Voids with size ranging from 2 to 4 mm as presented in (Hordijk, 1991) are taken into account in this study. A series of cubic concrete samples with dimensions of 50mm×50mm×50mm containing spherical/ellipsoidal voids and spherical/ellipsoidal aggregates (gravel aggregates) and polyhedral aggregates (crushed aggregates) are generated, as shown in Fig. 1, where aggregates are in green and voids are in red. The other phase in the cube represents mortar. The detailed algorithms and procedure in generating meso-structures in both 2D and 3D was programmed using MATLAB (MATLAB, 2011) and can be found in our previous work (Wang et al., 2015b; Wang et al., 2015a).
Table 1 Aggregate size distribution (Hirsch, 1962)

<table>
<thead>
<tr>
<th>Sieve Size (mm)</th>
<th>Total percentage retained (%)</th>
<th>Total percentage passing (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>12.70</td>
<td>0</td>
<td>100</td>
</tr>
<tr>
<td>9.50</td>
<td>39</td>
<td>61</td>
</tr>
<tr>
<td>4.75</td>
<td>90</td>
<td>10</td>
</tr>
<tr>
<td>2.36</td>
<td>98.6</td>
<td>1.4</td>
</tr>
</tbody>
</table>

Fig. 1. 3D mesostructures of concrete ($P_{agg}=30\%$)

FINITE ELEMENT MODELLING

The ANSYS APDL (parametric design language) programs in combination with ANSYS batch processing are developed to provide a powerful tool of automatic mesh generation for a large number of samples required for Monte Carlo simulation. After finite element meshing, a duplicate set of nodes is required at the interfaces in order to simulate the potential micro-crack initiation in cohesive zone model. Here three set of different 6-node zero in-plane thickness cohesive interface elements (CIEs) are pre-inserted into the existing element surfaced by an in-house computer program CIEIN. Three sets of CIEs with different traction-separation softening laws are inserted (see Fig. 2), namely, CIE_AGG inside the aggregates (grey in Fig. 2 (b) and Fig. 2 (d)), CIE_MOR inside the mortar (green in Fig. 2 (b) and Fig. 2 (e)).
(d)), and CIE_INT on the aggregate-mortar interfaces (yellow in Fig. 2 (b) and Fig. 2 (d)). The element and node numbers are denoted as E and N respectively. The detailed numbering of elements and nodes in the initial mesh and the mesh with inserted cohesive elements shows the insertion procedure with the new nodes generated at the same positions and CIEs between the continuum elements. A bilinear cohesive crack model is used here to predict discrete crack propagation in concrete specimens under tension loading. A linear ascending branch is added in the softening curve to model the initially un-cracked material.

![Initial mesh](image1)  
(a) Initial mesh  
(b) Mesh with zero thickness cohesive elements

Fig. 2 Inserting different cohesive elements into mortar-aggregate interface

**RESULTS AND DISCUSSION**

Fig. 3 shows the geometry, boundary and loading conditions of the numerical model. A displacement controlled loading scheme was used and all the analyses were ended at a displacement $d=0.1$ mm and loading time $t=0.005s$ (Wang et al., 2015b). Considering the balance between accuracy and efficiency, the element length 1mm was used for all the meshes in this study (Wang et al., 2015b). Solutions were performed with the commercial software ABAQUS/Explicit.

Stress-displacement curves from a Monte Carlo simulation with 50 realisations are shown in Fig. 4 together with the numerical mean curve and experimental data acquired from tension tests of six samples by Hordijk (Hordijk, 1992). The simulated stress-displacement curves in this work fit well with the experimental scatter. They are similar in terms of clear peak and sharp initial post-peak drop followed by a long shallow tail. The influence of the sample number on the Coefficient of Variation (CoV) of stress at loading point A (i.e. peak stress) and B (i.e. stress at displacement 0.03mm, where largest standard deviation is observed) (see Fig. 4) is shown in Fig. 5. It can be seen that 50 samples are enough to get a convergent value of CoV of stress with a stable fluctuation. It can also be observed that COV of peak stress for different void and aggregate distribution is low (1.5%), which demonstrates that the peak stress is relatively insensitive to the void and aggregate distribution. The notably large differences observed between the softening responses of the different realisations and high CoV of stress at point B illustrates the necessity to do a statistical analysis as the results vary greatly for different aggregate and void distribution, especially in softening range.
Fig. 3. Specimen dimensions, loading and boundary conditions

Fig. 4. Stress-displacement curves obtained from Monte Carlo simulation

Fig. 5. Influence of sample number on the CoV of stress

Fig. 6. Statistical distribution of peak stress from Monte Carlo simulation

Typical macro-crack patterns are observed from the Monte Carlo simulations under uniaxial tension. Fig. 7 presents the crack patterns at softening stage. To clearly visualise the fracture surfaces, four different ways are used: models with damaged cohesive elements (displacement magnification factor of 20), model without cohesive elements (displacement magnification factor of 200), failed interfaces only (displacement magnification factor of 20) and morphology of failed surface. The cracks shown in Fig. 7(a) and Fig. 7(c) are represented by red cohesive interface elements with damage index $D \geq 0.95$ ($D=1$ means complete failure). It could be observed that 3D modeling predicts more realistic fracture surfaces in the thickness direction whereas 2D modeling only assumes plane fracture problems. This result confirms the importance of including the third dimension into the analysis.
CONCLUSION

Models of concrete with random meso-structures comprising ellipsoidal/polyhedral aggregates and spherical/ellipsoidal voids have been generated in this study. Numerical-statistical analysis was carried out using a cohesive zone model to simulate damage and failure of concrete. Crack patterns are realistically simulated using the technique of pre-embedding CIEs. Monte Carlo approach is proposed for investigating the mechanical behaviour of 3D heterogeneous concrete. The main conclusions, based on the results obtained from the statistical analysis under a uniaxial tension loading, are: Pre-peak response and peak stress are relatively insensitive to the aggregate and void spatial distribution; post-peak softening response is sensitive to the spatial distribution of aggregates and voids which demonstrate the necessity of comprehensive Monte Carlo simulations; 3D modelling predicts more realistic crack paths due to the unsmooth, non-planar fracture surfaces, and thus should not be neglected.

Fig. 7. Failure of concrete under tension
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