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A Holistic Stray Current Assessment of Bored Tunnel Sections of DC Transit Systems

C. A. Charalambous, Member, IEEE, I. Cotton, Senior Member, IEEE, P. Aylott, N. Kokkinos

Abstract—In considering the stray current design for DC Transit Systems the stakeholders should comply with the objective that the stray current design requirement is to minimise the impact of the stray current on both the supporting infrastructure and on the third party infrastructure. This paper defines a holistic stray current assessment for Bored Tunnel Sections (B.T.S.) of DC Transit Systems, by utilising a Boundary Element (B.E.) platform. The method developed enables the stray current performance of various design options and characteristics to be assessed on the tunnel system. Most importantly, the methodology proposed offers the means to evaluate the stray current performance of a B.T.S. in terms of its geometry and topology. Finally the post-processing steps that facilitate the benchmarking of the results against the relevant EN standards are discussed.

Index Terms—DC Transit Systems, Stray Current Design and Control, Bored Tunnel Sections, Tunnel Service Insulation, Boundary Element Method.

I. INTRODUCTION

Stray current leaking from the rails in the nearby vicinity of a train drawing power has to return to the rail at a point closer to the supply substation. Corrosion will occur at each point that current transfers from a metallic conductor, such as a reinforcement bar in concrete, to the electrolyte (i.e. the concrete). Hence stray current leakage can cause corrosion damage to the rails, the tunnel reinforcement and to external buried pipework. Severe damage may occur as a result of stray current leakage [1].

It is worth noting that, for a ballasted track laid across a site with no reinforced concrete structures or buried metallic services, all of the stray current flow will be through the soil. Should parallel buried metallic conductors be added to the site, then these will have a lower resistance than the surrounding soil and will offer a superior stray current path. If these conductors are then fragmented into a series of short segments with soil in between, then the attractiveness of the conductors as a stray current path is lost. Acceptable stray current control can be consequently achieved by a set of design measures embracing a number of characteristics of the railway system. The optimum set of measures for any individual DC railway is a balance of the different constraints each system will have. In broad terms, railway design issues that impact on stray current can be summarised as: a) conductivity of the return circuit (i.e. the rails), b) insulation of the return circuit from earth, c) spacing of supply substations, d) train current demand, e) regenerative breaking and f) substation and system earthing. However, many of these parameters are inevitably fixed early in the design process. The stray current control design requirement is therefore to minimise the impact of the stray current on the supporting infrastructure and on third party infrastructure. Once a system is operational, the largest sole factor that modifies the stray current levels is the resistance of the rails to earth – this factor can vary by up to 1000 times (typically over the range 0.1 $\Omega$·km to 100 $\Omega$·km) and poor control of this has often been the critical factor behind excessive rail and infrastructure corrosion.

For a Bored Tunnel System (B.T.S.) the primary stray current corrosion risk is to the rails and their fixings, and to the tunnel walls. In order to offset this risk the longitudinal conductivity of the tunnel system should be minimised and the longitudinal conductivity of the stray current collection system (SCCS) should be maximised. The SCCS is used to perform the longitudinal interconnection defined in EN 50122-2 7.2.2. However unless the trackbed concrete can be insulated from the tunnel segments it will never be possible to achieve a 100% control of the stray current within the stray current collection system. Thus, when approaching the design of the stray current systems for the B.T.S. the impact of the parallel metallic conductors in the system, the spread of stray current across them and the effect of insulating those conductors from the tunnel reinforcement should be carefully examined.

Consequently, the main objective of this paper is to define a holistic stray current assessment for a B.T.S., which may be applied in the early stages of the design process. The assessment proposed is based on a Boundary Element (B.E.) platform [2]. The advantage lies in the fact that the method and models developed enable the stray current performance of various designs options and characteristics to be assessed on the tunnel system. The design options incorporated and evaluated in this paper are based on variations of the civil drawings and on other particulars of a real system. Most importantly, the methodology proposed offers the means to assess the system in terms of its geometry and topology. Finally the post-processing steps that facilitate the
benchmarking of the results against the relevant EN standards are discussed.

II. THE STATE OF THE ART AND BEYOND

Simulators of different approaches and scales have been reported in an attempt to investigate the generation of stray currents resulting from the operation of DC rail transit systems. Many of these simulation endeavours are based on simple models having a rail system represented by resistive networks [3]. This was a widely adopted method which modeled the rails’ series resistance and their corresponding resistance to earth. However, this kind of modeling accounts only for primary leakage currents from the rail to earth.

Consequently, more complex (resistive-type) simulation models have been reported in [4] and [5]. These models may account either for single or double track DC networks with multiple traction substations and track paralleling huts. They can therefore calculate the track to earth potential profiles, the total stray current of the system and the potential profile of a stray current collection mat which may be present in the system. Nevertheless the underlying limitation of these models arises from their incompetence to account for the soil’s resistivity effect on the level of stray currents, as well as to model the effect of stray currents on any third party infrastructure in the nearby vicinity.

Another reported study [6] investigates the effect of placing metallic structures –such as reinforced concrete- in parallel to the railway at some distance below the track. The fundamental principle of this study is similar to the resistive network’s modelling philosophy, described above. Nevertheless, the proposed model in [6] permits the analysis of both earthed metallic structures and reinforced concrete structures. It is acknowledged though, that the model is limited to simple geometry and is inevitably based on numerous design assumptions. Moving further [7], [8] and [9] report the use of resistive networks in performing dynamic simulations. The dynamic simulations are specifically utilised for a) evaluating the maximum potential rise on the transit system [7], b) investigating the effect of three different earthing schemes (solidly-bonded, floating and diode-bonded) on the rail potential and on the stray current level [8] and c) computing and validating the rail-to-earth potential for a diode-bonded scheme [9].

A diversified method for calculating the stray currents levels of DC transit systems is reported in [10]. In this work the rail is treated as a transmission line (shunt energised) excited by a finite current source. The work suggests that a current source may be used to represent: a) the current injected into the rails by a train, b) the current absorbed by a substation and c) the current resulting from a regenerative braking train.

On another note, the work reported in [11] incorporates a spherical electrode model to analyze the stray current activity. In particular the negative return system is modelled using spherical electrodes as a means to represent intentional or inadvertent connections to earth. It is shown that the flow of current through earth can be calculated by knowing: a) the potential (at each evaluation point) to distant earth, b) the resistivity of the soil and c) the effective size of each electrode.

On a final note, a finite boundary method has been formulated to describe the principles behind the need for stray current control [12]. This work examines the relationship between the stray current collection system design and its efficiency. By following the same modeling principles the importance that soil resistivity has, on the corrosion risk of the traction system and of the third-party infrastructure, is reported in [13]. Such information, through the methodology developed, is ultimately used to vary the level of stray current protection across a light rail system to ensure a consistent lifetime across the whole system [14]. The work reported in [15] details a mix of methods and software to model the stray current interactions of dc rail systems under dynamic operation.

Finally, the work reported in [16] introduces a 3D FE-model for modeling the northern part of the Islands Brygge station (Copenhagen Metro traction system). The model comprises sections of a bored tunnel and the anodes of a cathodic protection system placed in the soil around the tunnel diaphragm walls. The model is able to calculate high potential and current density sections along the tunnel segments. However, the polarity of the current on the tunnel segments (i.e. whether an element receives or discharges current) cannot be distinguished.

A. Advancements of the Proposed Method beyond the State of the Art

Bearing in mind the existing methods for stray current modelling and control, the underlying motivation of this work is to provide a method that can assess the stray current performance of all elements that may be embraced in a B.T.S. Thus, the impact of the parallel metallic conductors in the B.T.S, the spread of stray current across them (and across the stray current collection grid) as well as the effect of insulating any tunnel services from the tunnel reinforcement should be carefully modelled and examined.

Consequently, our proposed method relates in firming the existing stray current modelling and control endeavours by providing the following advancements over the existing methods: a) Assess the impact of proposed civil drawings on stray current performance: The method and models developed can evaluate the stray current performance of various designs of complex geometry and characteristics. b) Assess the stray current performance of all elements embraced in a B.T.S: The method and models developed can evaluate the stray current performance of the tunnel segments and tunnel services. The tunnel segments are not electrically continuous, however electrically conductive tunnel services may be attached to them. c) Assess the level of insulation and earthing practice of tunnel services: The model developed allows for the tunnel services to be continuous but examines the impact of different levels of insulation between these and the tunnel segment reinforcement. Furthermore it can examine the impact on the stray current collected by tunnel services should these be solidly earthed for safety precautions. d) Assess the stray current performance of third-party infrastructure: The model can assess the effect of stray current on any metallic
infrastructure that lies in the nearby vicinity of the tunnel system.

III. PROPOSED MODEL DESCRIPTION

The model is developed following an assessment of the infrastructure elements considered likely to contribute to the stray current performance of a B.T.S.

Fig. 1 illustrates a cross-section of a realistic B.T.S along with actual dimensions, labeling the most important features that are crucial in assessing its stray current performance.

Fig. 1. Cross Section of a realistic B.T.S with actual dimensions in mm.

A. Description of B.E. Model

The simulation model is formulated within the MALZ module of the CDEGS software [2]. The MALZ module allows currents to be injected and collected at various points in a network of conductors that are placed in a soil environment. It further computes the flow of these currents through each individual conductor within the network. It thus offers the advantage of computing a stray current and a voltage distribution along the length of the system modeled. In particular the model has simulated a 2 km section of a B.T.S and assumed a uniform construction and standard along its length. The impact of a single point load at the midpoint with traction supply substations at each end was considered. The ideal computer model formulated is illustrated in perspective view by Fig.2. With reference to Fig.2 the numbered items are described in more detail:

1) Tunnel Segments (Item 1)

A ring of precast steel reinforced segments may support the bored tunnel. The reinforcement in adjoining segments (both circumferential and longitudinal) should not be in direct electrical contact and segments may be bolted together through PVC sleeves. Therefore the tunnel segments are not electrically continuous. However, two segments (item 1 – left and right) are considered in the model, since electrically conductive tunnel services may be attached to them. While the tunnel segments are approximately 1m in length, they are modelled as 25m segments in the computer model to restrict the overall number of conductors. The tunnel services are attached to these segments at regular intervals via bonds.

2) Tunnel Services (Items 2 &10)

The tunnel services are modelled as galvanised steel conductors. By way of an example, the tunnel services are modeled to represent an overall tunnel service cross-sectional area of 79 mm² (item 2), equating to a conductor radius of 5 mm and an overall tunnel service cross-sectional area of 314.16 mm² (item 10), equating to a conductor radius of 10 mm. The model allows for the tunnel services to be continuous but examines the impact of different levels of insulation between these and the tunnel segment reinforcement. Examples of tunnel services that may be conductive along the tunnel length are the fire main, the pumping main, cable trays, handrails, etc.

3) Running rails (Items 3 &4)

The running rails (e.g. UIC54) are modeled as conductors having a longitudinal resistance of 40 mΩ per kilometer. This may be approximately a 19% increase in the nominal longitudinal resistance of 36.3 mΩ per kilometer to account for wear that will take place during the running of the system (cross-sectional area reduction of 16%). Furthermore, as it is not possible to model discrete insulator pads in the software, the effect is modeled by assuming the rails are coated with a resistive coating [16]. This coating is set accordingly to account for resistances to earth for a) service (40Ω.km) and b) design (100Ω.km) values, as design examples (EN50122-2 levels are much lower). It is noted that in reality these values will be project specific. The developed model for the running rails is able to account that the traction return current goes through both rails of each track. The positioning of the two running rails in Fig.1 is geometrically accurate with respect to each other and with respect to the other elements of the design.

4) Stray Current Collection Grid – Longitudinal and Transversal Steel Bars (Items 5 &6)

The Stray Current Collection System (S.C.C.S.) has been realised in the developed model as a geometric replicate of an example system illustrated by Fig. 3. The S.C.C.S. embraces the Stray Current Collection Grid (S.C.C.G.) and the Stray Current Collection Cable (S.C.C.C.). The S.C.C.G. employs steel bars which are longitudinally placed (item 5) under each rail (4 steel bars x Φ16 mm for each running rail - that is 2 x 4 steel bars x Φ16 mm for a single track). This design provides an overall S.C.C.G. cross-section of 1608 mm² per track. Under each rail the four longitudinal steel bars are transversally spaced at a distance of 150 mm. At intervals of
50 m the longitudinal steel bars are bonded to sets of transverse steel bars (item 6). This example also assumes that the S.C.C.G. is embedded in the concrete trackbed at a distance of 250 mm below the upper concrete surface.

Fig. 3. Perspective view of the stray current collection system (S.C.C.S.)

5) Stray Current Collection Copper Cable – (Items 7 & 8)

In the developed model, the Stray Current Collection Cable (S.C.C.C. - item 7) is bonded to the S.C.C.G. through flexible bare cables (item 8) at 100 m intervals. Both cables are made from copper and their size is taken in the model as 95 mm². The cables are coated to ensure that current leakage from the collector cables to earth does not take place. The developed model may assess the system’s stray current performance under various design options (e.g. cables’ size and relative position).

6) Third-Party Infrastructure (Item 9)

The conductor (item 9) representing the third party infrastructure serves the scope of assessing the effect of stray current on the soil surrounding the tunnel system. Within the model developed it takes the form of a metallic (heavy duty galvanised steel) coated conductor, which may be located at a range of distances from the tunnel system.

B. Description of Soil Models

From an earthing design perspective, designs should be based on the highest likely soil resistivity figure; however from a stray current perspective the worst case should be the lowest likely measured figure. The model developed has incorporated a three-layer horizontal soil model [2], as illustrated by Fig. 4.

Fig. 4. Plan view of the arrangement of conductive elements and the soil models

The upper layer of the soil model is assigned an extremely high resistivity of $10^{14}$ $\Omega$m, to eliminate any leakage current to flow from the rails to tunnel services in an upward direction. With this arrangement, any leakage current that would reach the tunnel services should find its path through parts of the tunnel segments that sit within the concrete layer (middle layer). This arrangement mirrors the real situation well and is computationally stable. As stated above, a portion of the tunnel segments is situated in the middle soil layer which is assigned a resistivity of 180 $\Omega$.m. This represents the concrete present within the tunnel. The middle soil layer also embraces the running rails and the S.C.C.S. Current from the running rails must flow through concrete to reach the S.C.C.S. or alternatively the tunnel segments and services. It must also pass through the concrete to reach the surrounding soil. The lower layer of the soil model is assumed to have a resistivity of 15 $\Omega$m (i.e. a lowest likely measured figure) and represents the soil surrounding the tunnel.

C. Base Input Data and Assumptions

Table I tabulates the base input data and assumptions employed in the subsequent simulations for assessing the stray current performance of the B.T.S. design as discussed in A and B.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Track length &amp; power supply</td>
<td>2 km single track with a supply substation at either end.</td>
</tr>
<tr>
<td>Traction current</td>
<td>2000 A static load injected at mid-point.</td>
</tr>
<tr>
<td>Rail resistance</td>
<td>40 m$\Omega$/km (UC54)</td>
</tr>
<tr>
<td>Rail conductance (resistance to earth)</td>
<td>100 $\Omega$.km</td>
</tr>
<tr>
<td>Soil Model Resistivity</td>
<td>Upper: $10^5$ $\Omega$.m Middle: 180 $\Omega$.m (Concrete) Lower: 15 $\Omega$.m</td>
</tr>
<tr>
<td>Soil Model Width</td>
<td>Upper: 5.8 m Middle: 1m (Concrete) Lower: Infinite</td>
</tr>
<tr>
<td>Stray Current Collection Grid (S.C.C.G.)</td>
<td>2 x 4 steel bars x $\Phi$16 mm for a single track</td>
</tr>
<tr>
<td>Stray Current Collector Cable (S.C.C.C)</td>
<td>95 mm² - copper – bonded to S.C.C.G. at 100m intervals</td>
</tr>
<tr>
<td>Stray current collector cable termination at substations</td>
<td>Floating</td>
</tr>
<tr>
<td>Tunnel Reinforcement</td>
<td>$\Phi$20 mm - Steel (Tunnel segments electrically isolated along the length of tunnel)</td>
</tr>
<tr>
<td>Tunnel Services</td>
<td>79 mm² / 314.16 mm² - galvanised steel</td>
</tr>
<tr>
<td>Insulation of internal tunnel infrastructure (handrail, fire main etc.) from segment reinforcement</td>
<td>(1) solid connection (no insulation) (2) insulated to different levels</td>
</tr>
<tr>
<td>Third Party Infrastructure</td>
<td>1963 mm² - galvanised steel</td>
</tr>
</tbody>
</table>

IV. SIMULATION RESULTS AND ANALYSIS

The simulations are carried out using a 1 km section of the tunnel system illustrated by Fig. 2. The simulation takes about 2.5 hours to be completed on a standard computer (2GHz processor, 3GB RAM). The 1km section simulated is representative (symmetrical) of a 2 km section of tunnel with a single train at the center and a substation at each end. 2000 A is taken to be injected by a train placed at 0 m and this is collected by a substation at the far end of the tunnel (Fig. 5).

Fig. 5. Simulation of a 1km section system

This represents the worst static case scenario in terms of stray current performance evaluation. The 2000 A flows through the running rails and therefore produces a rise in the rail to earth potential which in turn results in stray currents. In a floating rail system, the stray currents are determined by the resistance of the trackwork insulators. A rough calculation of the expected stray current can be made by hand. Take 2000 A flowing through two rails with a resistance of 40 m$\Omega$/km.
Since the two rails are in parallel, the overall potential difference between the rail ends will be 40 V. In the
convention of this modeling, this will appear on the rails as
+20V to remote earth near the train and –20V to remote earth
near the substation. A positive voltage implies a current
leaking out of a conductor by corrosion; a negative voltage
implies a current leaking into a conductor. At 500 m down the
track the voltage to remote earth will be 0 V. The running rail
is taken to have a resistance to earth of 100 Ωkm. The
resistance to earth of 500 m of running rail is therefore 200 Ω.
The total stray current leaving the running rail will therefore be
given by 10 V (the average running rail voltage along a 500 m
length) divided by 200 Ω, in other words 50 mA. The total
stray current will therefore be approximately twice this, 100
mA, since there are two running rails which each allow current
to leak to earth.

Fig. 6 illustrates the rail to earth voltage (for Rail1 –item 3)
simulated by the B.E model of Fig. 2. It can be shown that the
same profile is obtained for Rail2. Moreover, Fig. 7 shows the
stray current profile produced by the modeling software for
rail1. The total stray current flowing from the rail1 where the
potential is above 0V is 50.317mA whereas the total stray
current flowing from the rail2 is calculated at 50.201mA.
Therefore the total stray current produced by both rails is
100.52 mA which verifies the value obtained by hand
calculations.

Fig. 7 Simulated Stray Current Profile (Rail1)

Fig. 8 illustrates the simulated geometrically accurate 3D
plot of the net leakage current [17] profile expected by the
S.C.C.G (2 x 4 bars x Φ16 mm for a single track – Fig. 2).
Fig. 9 illustrates the simulated geometrically accurate 3D plot
of the current retained by the proposed S.C.C.G. As previously
noted the simulations were designed to assess the ability of a
floating stray current system, i.e. one not connected to the
running rails. Consequently the S.C.C.G with the help of the
S.C.C.C. (i.e. S.C.C.S.) must collect the current from the point
of release into the tunnel and move it to the substation situated
some distance away from the train.

Table II reveals that the S.C.C.S. modeled has an efficiency
of 76%. The efficiency value obtained is based on the
maximum current that can be collected on aggregate, by the
S.C.C.G and the S.C.C.C. Table II also reports that the tunnel
services, when completely isolated from the tunnel segments
collect no current. Furthermore, the tunnel segments can
collect a limited amount of current (0.1%) as these are not
electrically continuous. Finally the 3rd party infrastructure
which lies in the nearby vicinity of the tunnel system modelled

<table>
<thead>
<tr>
<th>Description</th>
<th>Current (mA)</th>
<th>% of Total Stray Current Collected</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total Stray Current Rails</td>
<td>100,518</td>
<td></td>
</tr>
<tr>
<td>Total Stray Current S.C.C.S.</td>
<td>75,681</td>
<td></td>
</tr>
<tr>
<td>Retained Current S.C.C.G.</td>
<td>43,761</td>
<td>43.536</td>
</tr>
<tr>
<td>Retained Current S.C.C.C.</td>
<td>32,330</td>
<td>32.164</td>
</tr>
<tr>
<td>Total Stray Current Tunnel Segments</td>
<td>0.855</td>
<td></td>
</tr>
<tr>
<td>Retained Current Tunnel Segments</td>
<td>0.100</td>
<td>0.148</td>
</tr>
<tr>
<td>Total Stray Current Tunnel Services</td>
<td>0.000</td>
<td></td>
</tr>
<tr>
<td>Retained Current Tunnel Services</td>
<td>0.000</td>
<td></td>
</tr>
<tr>
<td>Total Stray Current 3rd party Infrastructure</td>
<td>0.243</td>
<td></td>
</tr>
<tr>
<td>Retained Current 3rd party Infrastructure</td>
<td>0.148</td>
<td>0.148</td>
</tr>
</tbody>
</table>
collects a small amount (0.148%) of the stray current leaking from the rails.

Moving further, Table III tabulates the sensitivity study performed to assess the effect of tunnel service insulation from the segment reinforcement, on the system’s performance. Three different conductors (serving as bonds) have been employed each having the following resistance values: 0.01Ω/km, 2.5 Ω/km and 1 MΩ/km. It is clear from Table III that improvements in the tunnel service insulation from the segment reinforcement above the level of 1 MΩ/km have no impact in this particular example (i.e. 1 MΩ/km of insulation can be adequate to completely isolated the services).

Table IV tabulates the sensitivity study performed to assess the relative positioning of the S.C.C.G. with respect to the upper concrete surface (see Fig. 3). It is revealed that shifting the S.C.C.G. a 100mm closer to the upper concrete surface the efficiency of the stray current collection system is improved by 3.6%, when compared to the base model input data (i.e. 250 mm distance from the upper concrete surface).

V. STRAY CURRENT LEVELS UNDER VARYING CONDITIONS

For assessing the stray current performance of the system under operational conditions it is rather necessary to rely on power simulation data. The assessment of the power simulation data should reveal what the average current on the system within an individual section in the hour of highest traffic is. The data may also provide information regarding the daily average taking account of the operating timetable as well as information regarding the maximum peak train current.

Within the preceding sections the model looked at a static case under a 2000 A load. However, in reality the trains may draw significantly higher currents than this and give rise to rail voltages significantly higher than 20 V. A determination of the stray current levels under real life conditions can be achieved by applying scaling factors to the model results.

A variation in track current will influence the leakage current distribution due to the resulting alteration of rail-to-earth potential. A doubling in track current will lead to a doubling in voltage and hence a resulting doubling of leakage current density along the rail. This is a linear effect. Thus for a 4000 A peak single train load the total rail leakage current of 100 mA from 2000 A at 100 Ωkm single track will increase to 200 mA.

Furthermore, the rail to earth potential is determined by the currents flowing through the rail. Unless there is significant leakage that causes a change in the rail current flow, the leakage current density is proportional to the resistance of the rail insulation. Variations in the rail to earth resistance can therefore be taken to have a linear relationship with the leakage current density. Table VI shows the predicted stray current levels, arising from the model of Fig.1, for a range of traction currents (1000A, 2000A, 3000A and 4000A) and for a
range of rail resistances to earth (40 Ωkm and 100 Ωkm). For example the stray current levels for a 4000 A single train system compliant with the EN 50122-2 [18] requirements for rail to earth resistance of 2 Ωkm single track would be some 10 A. compared with the case studies examined. Consequently, the stray current levels obtained for all traction currents under 40 Ωkm and 100 Ωkm can be benchmarked against the permitted minimum values posed by EN 50122-2.

**TABLE VI**

<table>
<thead>
<tr>
<th>Stray Current With Single Train 1 km away from Substation drawing Current:</th>
<th>1000 A</th>
<th>2000 A</th>
<th>3000 A</th>
<th>4000 A</th>
</tr>
</thead>
<tbody>
<tr>
<td>RE:2 Ωkm</td>
<td>2.5 A</td>
<td>5 A</td>
<td>7.5 A</td>
<td>10 A</td>
</tr>
<tr>
<td>RE:40 Ωkm</td>
<td>125 mA</td>
<td>250 mA</td>
<td>375 mA</td>
<td>500 mA</td>
</tr>
<tr>
<td>RE:100 Ωkm</td>
<td>50.3 mA</td>
<td>100.5 mA</td>
<td>150.8 mA</td>
<td>201 mA</td>
</tr>
</tbody>
</table>

*EN 50122-2: 2010 permitted minimum

**A. Estimating Stray Current Density on Reinforcement**

For a single train load, the leakage current density from and to the rail will vary linearly between the train and supplying substations. Fig. 11 shows the calculated rail leakage current density for the 2000 A / 100 Ωkm base case.

![Fig. 11. Rail leakage current density (amps per metre length of rail) for a single train at the mid-point between two substations 2 km apart drawing 2000 A with a uniform rail to earth resistance of 100 Ωkm single track](image)

From Fig. 10, the worst case current density from the rail is at the substation and equals approximately 0.2 mA/m. Thus the worst case current density from the S.C.C.G to rail is 0.2 mA per meter length. However, this assumes that: (a) the rail to earth resistance at each baseplate is the same and gives the combined effective resistance of 100 Ω for the 1km section between train and substation. This is an unlikely situation and the 100 Ω resistance is more likely to be derived from a small proportion of baseplates with a lower than expected resistance, (b) the longitudinal rail resistance is also uniform – i.e. there is even wear along the length of the rail and the welded joints are all of uniformly low resistance, (c) the trackbed reinforcement and concrete, together with the tunnel systems, are also electrically uniform and (d) the external soil environment is uniform.

Given that this degree of system uniformity across all of the infrastructure components is very unlikely, especially once the system is in operation, it is more reasonable to assume that there will be a concentration of stray current return to the rail over a possibly short distance. In order to apply a more credible worst case than the 0.2 mA/m given above, a range of scenarios can be assumed as illustrated by Fig. 12. The results of Fig. 12 are based on a conservative method for calculating the average stray current per length of a single track line as per (1). Where p is the percentage (%) of the stray current that will return to the rails within a specified shorter length and Iₜ is the total stray current flow from the rails.

\[ J = \frac{p \times I_{t}}{d} \]  

For example, given the total calculated stray current flow of 100.52 mA (see Table II), the worst case stray current leakage under the design level of 100 ohm.km into the trackbed concrete from the S.C.C.G would be 1.17mA/m when assumed that 35% of the total stray current flow will return to the rails within a 30 m length. This example provides a safety margin of approximately x 5.9 when compared to the 0.2 mA/m of Fig 11. The safety factors will decrease proportionately with further reduction in rail to earth insulation (e.g. 40Ω.km for service operation) towards the EN 50122-2 permitted minimum; at some conditions the 2.5 mA/m level can be exceeded.

**TABLE VII**

<table>
<thead>
<tr>
<th>DATA FOR VOLTAGE DROP CALCULATIONS – EN 50122-2</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
</tr>
<tr>
<td>L</td>
</tr>
<tr>
<td>Lc</td>
</tr>
</tbody>
</table>

**B. Estimating Longitudinal Voltage Drop on Reinforcement**

The notes of EN 50122-2 suggest that the acceptance criteria for successful control of stray current corrosion should be: a) corrosion potential change limited to an average of +100 mV and b) longitudinal potential drop along a structure limited to 100 mV under average current load. Both conditions are applied to averages measured in the hour of highest traffic.

Calculations have been performed for the proposed S.C.C.S in accordance with the equations (2) and (3) given in EN 50122-2 as per the data tabulated in Table VII. The calculated Uₜ for a 1 km length of S.C.C.S. is 10mV.

\[ U_{t} = 0.5 	imes I_{t} 	imes L 	imes \frac{R'_{x} 	imes R'_{y}}{(R'_{x} + R'_{y})} \times \left[ 1 - \frac{L_{c}}{L} \times \left( 1 - \frac{1}{e^{\frac{L}{L_{c}}}} \right) \right] \]  

\[ L_{c} = \frac{1}{\sqrt{\left( R'_{x} + R'_{y} \right) \times G_{xy}}} \]  

However it is acknowledged in EN 50122-2 that this calculation method is very conservative. This is due to the fact that the method does not take into account any reducing effects such as the conductance per unit length of the tunnel structure versus earth.
In contrast to the above calculation, Fig. 13 illustrates the corresponding simulated 3D voltage to earth profile along the S.C.C.S by using the model of Fig. 2. The calculated profile takes into account the influence of all the metallic elements of the tunnel system. It appears that the voltage of the system varies from -2mV to +2mV giving a maximum end to end voltage of 4mV. The model therefore provides a more credible method for estimating longitudinal potential drop along the collection grid system of a B.T.S.

Fig. 13 Simulated Voltages to Earth Profile - S.C.C.S.

VI. CONCLUSIONS

Bearing in mind the existing methods for stray current modelling and control, this paper proposes a method that can assess the stray current performance of all elements that may be embraced in a B.T.S. Thus, the impact of the parallel metallic conductors in a B.T.S, the spread of stray current across them (and across the stray current collection grid) as well as the effect of insulating any tunnel services from the tunnel reinforcement are modelled and examined with the aid of a F.E. platform. Consequently this work firms any existing stray current modelling and control endeavours by providing a number of modelling advancements. Finally the post-processing steps that facilitate the benchmarking of the results against the relevant EN standards are discussed.

VII. REFERENCES


VIII. BIOGRAPHIES

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