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Tying different knots in a molecular strand

David A. Leigh^{1,2*}, Fredrik Schaufelberger^{2,4}, Lucian Pirvu^{2,4}, Joakim Halldin Stenlid³, David P. August², Julien Segard²

¹School of Chemistry and Molecular Engineering, East China Normal University, 200062 Shanghai, China.

²Department of Chemistry, University of Manchester, Oxford Road, Manchester, M13 9PL, UK.

³Department of Physics, AlbaNova University Center, Stockholm University, S-10691 Stockholm, Sweden.

⁴These authors contributed equally: Lucian Pirvu, Fredrik Schaufelberger.

*e-mail: david.leigh@manchester.ac.uk

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Abstract

A piece of rope or cord can be tied into different knots with their, often contrasting, properties exploited in a range of applications, from shoelaces to the knots used for climbing, fishing and sailing.¹ Although knots are found in DNA and proteins,² and form randomly in other long polymer chains,^{3,4} there is currently a lack of methods for tying⁵ different sorts of knots in a synthetic nanoscale strand. Here we show that interspersing coordination sites for different metal ions within an artificial molecular strand enables it to be tied into multiple knots. Three topoisomers—an unknot (0₁) macrocycle, a trefoil (3₁) knot,⁶⁻¹⁵ and a three-twist (5₂) knot—were each selectively prepared from the same molecular strand by using transition metal and lanthanide ions to guide chain folding in a manner reminiscent of the role played by protein chaperones.¹⁶ We find that the metal-ion-induced folding can proceed with stereinduction: for one knot a lanthanide(III)-coordinated crossing pattern only formed with a copper(I)-coordinated crossing of particular handedness. In an unanticipated finding, metal ion coordination was also found to be able to translocate an entanglement from one region of a knotted molecular structure to another, resulting in an increase in writhe (topological strain) in the new knotted conformation. The knot topology affects the chemical properties of the strand: while the tighter 5₂ knot can bind two, different, metal ions simultaneously, the looser 3₁ isomer can only bind either one Cu(I) ion or one Lu(III) ion. The ability to tie nanoscale chains into different knots offers new opportunities to explore for modifying the structure and properties of synthetic oligomers, polymers and supramolecules.

Main

The way that strand crossing patterns define knot topoisomerism¹⁷ is reminiscent of the stereochemical relationship between asymmetric centers in conventional organic molecules¹⁸. As the handedness of existing asymmetric centres can influence that of new stereocenters formed in chemical reactions,¹⁹ we wondered if a similar approach could be used to control topology in chemical synthesis, i.e. whether the stereochemistry of some strand crossings could determine the crossing orientation of others? This could allow access to molecular knots of low symmetry; a contemporary challenge for knot synthesis as the topologies prepared to date have generally relied on high symmetry self-assembly²⁰ of multiple building blocks^{6-8,11-14,21-24}. Nature folds peptide chains to reach discrete 3D structures, including knots,^{2,25,26} often through the assistance of chaperones that guide folding to a particular conformation through the myriad of possible pathways. Chaperones accelerate the knotting of methyltransferases by several orders of magnitude²⁷ and promote the formation of the 5₂-twist knot of human protein ubiquitin hydrolase^{28,29}. We investigated the use of metal ion coordination in a conceptually similar manner, to fold³⁰⁻³² a synthetic molecular strand into particular, well-defined,³³ entanglements (Fig. 1a). We envisaged that the crossing stereochemistry could then be covalently captured by ring-closing olefin metathesis³⁴ (RCM) to form the corresponding closed-loop topologies, such as a three-twist (5₂) knot (Fig. 1b). The latter is a low symmetry topology found in DNA and proteins,² but inaccessible using current synthetic chemistry strategies^{35,36}.

The strategy we devised to tie a molecular thread into different knots is to intersperse 'guest-orthogonal' binding sites within the strand such that various discrete 'tangles'^{17,36,37} (simple crossing patterns that can be combined to form knots³⁸) are formed by activating some, all or none of the different binding

sites in the strand. This produces a metallofoldamer³² that can be programmed to fold selectively into any one of several differently knotted intermediates. Pentatopic ligand strand **L1** (Fig. 1b) features two kinds of metal complexation sites: (i) bidentate 1,10-diphenylphenanthroline (dpp) units, two of which bind to Cu(I) ions in a tetrahedral coordination geometry,^{6,39} and (ii) tridentate 2,6-pyridine dicarboxamide (pdc) groups, three of which coordinate to trivalent lanthanide cations to form a trimeric circular helicate⁴⁰. By alternating the binding sites in the sequence pdc-dpp-pdc-dpp-pdc, higher order entanglements can be introduced through stepwise folding and threading of the strand ends through an intermediate containing an internal loop (Fig. 1a). The lanthanide trimeric helicate is forced to be of Λ -helicity because of the steric requirements of (*R*)-stereocentres adjacent to the pdc groups.^{41,42} The chirality enforced in those crossings can be used to select the stereochemistry of the Cu-coordinated loop (Fig. 1c), a process analogous to using existing chirality to control the stereochemistry of new asymmetric centres in conventional stereoselective synthesis¹⁹.

Figure 1. Tying molecular strand L1 into a three-twist (5_2) knot through metal-ion-induced folding and entanglement. a) Stepwise folding, threading and covalent-capture of a pentatopic ligand with interspersed metal binding sites. b) Ligand **L1** contains three 2,6-pyridine dicarboxamide (pdc) sites (purple/blue) which code for the enantioselective formation of a $[+3]$ tangle under Ln(III) coordination, and two 1,10-diphenylphenanthroline (dpp)

sites (green) which code for a [+2] or [-2] tangle upon Cu(I) coordination. A three-twist (5_2) knot is tied through stepwise metal ion addition (Cu(I) then Lu(III)) and subsequent macrocyclization via ring-closing olefin metathesis. Reaction conditions: (i) $(\text{Cu}(\text{CF}_3\text{SO}_3))_2$ -toluene, MeCN/ CH_2Cl_2 1:2, 50 °C, 16 h, 93%. (ii) $\text{Lu}(\text{CF}_3\text{SO}_3)_3$, MeCN, 80 °C, 16 h. (iii) Hoveyda-Grubbs 2nd Generation catalyst, $\text{CH}_3\text{NO}_2/\text{CH}_2\text{Cl}_2$ 1:1, 50 °C, 20 h, 14% over two steps. For full experimental details, including synthesis of **L1**, see Supplementary Information. Letter annotation in chemical structure refers to general proton environments. c) Outcomes that could occur without control of crossing stereochemistry. Only Λ -stereochemistry at both the Ln(III) and Cu(I) centres is observed for the experimentally synthesized molecular 5_2 -knot. Regarding the nomenclature used in this paper: Λ - and Δ - (e.g. Λ_{Lu}) are standard descriptors for the helicity around metal centres and indicate the coordination stereochemistry at metal centers in the open-ended strand, **L1**. For closed-loop structures, (+ X_y) and (- X_y) are Alexander-Briggs notation^{17,36} for the enantiomers of a knot with X crossings and y index number (i.e. a particular pattern of X crossings). So '(+5₂)-**1**•[Cu][Lu]' indicates a copper(I) and lutetium(III) coordination complex of the (+)-enantiomer of the 5_2 -topology of chemical structure **1**.

Tying a 5_2 knot in a molecular strand

Combining ligand **L1** (Fig. 1b) with $[\text{Cu}(\text{CF}_3\text{SO}_3)]_2$ -toluene in MeCN/ CHCl_3 at 50 °C, smoothly generated **L1**•[Cu], as evidenced by mass spectrometry and ¹H NMR chemical shifts (see for example H_i and H_h , Fig. 2a and b, and the Supplementary Information section S7). There is no induced circular dichroism in the phenanthroline region (see Fig. 2d and Supplementary Fig. S73-S74) indicating that the Cu(I)-coordinated crossing forms without stereocontrol (a [± 2] tangle; Fig. 1c). The central pdc unit of the strand is within the closed loop of **L1**•[Cu]. As the strand ends are positioned on opposite faces of the **L1**•[Cu] loop, coordination of a lanthanide ion to the three pdc residues to form the circular helicate motif requires the strand to thread through the loop from different sides. The length of the spacers between the pdc and dpp groups were chosen using molecular modelling (see Supplementary Information section S6.5), such that Λ -handedness of the Cu(I)-coordinated loop allows the strand ends to thread through the loop more easily to form the Λ -helical Lu(III)-coordination complex.

Treating complex **L1**•[Cu] with $\text{Lu}(\text{OTf})_3$ in MeCN, followed by covalent capture through ring closing olefin metathesis,³⁴ afforded predominantly one major species, **1**•[Cu][Lu], as indicated by mass spectrometry and ¹H NMR spectroscopy. The bimetallic structure was isolated as **1**•[Cu][Lu][CF_3SO_3]₄ after purification by exhaustive size-exclusion chromatography (SEC) in 13% yield over 3 steps from **L1** (the yield for the isolated material is low in part because of the difficulty in separating the product from the small amounts of other, likely misfolded, species also formed). Electrospray ionization mass spectrometry (ESI-MS) was consistent with a ring-closed [Cu][Lu] complex (Figs. S14-S16, m/z **1**•[Cu][Lu]⁴⁺ 770.0, **1**•[Cu][Lu][CF_3SO_3]³⁺ 1076.0, **1**•[Cu][Lu][CF_3SO_3]₂²⁺ 1688.3) and ¹H NMR spectroscopy confirmed the entangled structure of the knot (Fig. 2c, Figs. S27 and S28). Among the spectral changes that occur upon knotting, protons H_h of the phenanthroline rings shift upfield from a single signal at 7.0 ppm in the metal-free strand, **L1** (Fig. 2a), into four distinct signals at 5.6-6.1 ppm in bimetallic complex **1**•[Cu][Lu] (Fig. 2c), indicative of Cu(I) binding to the dpp units to form a clasp crossing, and pronounced diastereotopic environments caused by the chiral lanthanide-coordinated tangle (similar effects observed for H_k , H_j , H_i and H_d). Several of the methyl groups (H_e) undergo upfield shifts, reflecting their shielded positions in the folded structure (Fig. S13). Diffusion-Ordered Nuclear Magnetic Resonance Spectroscopy (DOSY-NMR) confirmed the complex to be a single species (Fig. S39), smaller in size than the corresponding unknot macrocycle, (0₁)-**1** (Fig. S34, Table S2), and consistent with an energy-minimized modelled structure of the compact, entangled, structure of the 5_2 knot (Figs. 2e and f).

Figure 2. Spectroscopic characterisation and modelled structure of molecular knot $(+5_2)-1\bullet[Cu][Lu]$. a-c) 1H NMR spectra (600 MHz) of the three-twist knot tying process: a) ligand **L1** (298 K, $CDCl_3$); b) Cu(I)-coordinated complex **L1•[Cu]** (298 K, $CDCl_3$); c) bimetallic three-twist knot $(+5_2)-1\bullet[Cu][Lu]$ (343 K, $MeCN-d_3$). Key proton resonances are designated with the lettering indicated in Fig. 1b. Primes following letters are used to indicate that previously indistinguishable chemical environments no longer appear equivalent due to the more strongly expressed diastereotopic environments in the chiral knot structure. For full structural assignments see Supplementary Information. d) CD spectra (298 K) after key steps in the strand-folding process. Compounds **L1** and **L1•[Cu]** measured in CH_2Cl_2 (0.025 mM) and $(+5_2)-1\bullet[Cu][Lu]$ in $MeCN$ (0.1 mM). e) Optimized low-

energy geometry (B3LYP-D3/6-311g(d,p)//6-31g(d) with the RECP basis set for Lu, see Supplementary Information for details) of the three-twist knot, (+5₂)-1•[Cu][Lu], in space-filling representation. f) Corresponding stick representation of (+5₂)-1•[Cu][Lu] (hydrogens omitted for clarity). g) Folding pathway dependence on the sequence of metal ion addition (see Supplementary Information, section S5.2).

As the asymmetric carbon atoms adjacent to the pdc units force the Lu(III)-(pdc)₃ tangle to have Λ -stereochemistry,³⁸ the stereochemistry of the Cu(I)-(dpp)₂ clasp crossing determines the knot topology. The pronounced CD response in the π - π^* transitions of the phenanthroline chromophore (Fig. 2d, right) results from one handedness of the Cu(I)-coordinated centre being preferentially selected during the threading step. Literature precedence⁴³ for chiral Cu(I)-(dpp)₂ junctions is that a negative Cotton effect at 330 nm corresponds to Λ -handedness of the clasp crossing. This means that the topology and stereochemistry of the product is (+5₂)-1•[Cu][Lu]. A strong chiral response for the phenanthroline groups is present for the crude reaction mixture following ring-closing olefin metathesis, indicating that the folding proceeds with a significant degree of selectivity for a specific topoisomer (Fig S5). Hence, the stereoselectivity in this region does not arise during the purification process. Rather topological stereoselection, in the form of a chiral tangle selecting the handedness of a racemic one, occurs during the second metal-induced strand folding step. This results in a single enantiomer (Λ -handedness at the Cu(I) centre) of a single knot topoisomer (5₂), in an analogous manner to diastereoselective synthesis in conventional organic chemistry. The energy-minimized structure of (+5₂)-1•[Cu][Lu] (Fig. 2e and 2f), obtained by simulated annealing with semi-empirical PM7 modelling, followed by optimization by density functional theory (DFT) calculations, confirmed the spectroscopic and stereochemical assignment of the experimentally prepared knot (see Supplementary Information, section S6). The simulated circular dichroism spectrum of (+5₂)-1•[Cu][Lu] reproduced the experimental CD data, including correct prediction of the handedness of the Cu-clasp crossing in the phenanthroline region and the helicity of the Lu-circular helicate (Fig. S12).

Folding pathway for the 5₂ knot

The folding to the 5₂ knot was found not to be under thermodynamic control, as adding the metal ions in different sequences produced different outcomes (Figs. 2g and S6, S7). Adding Lu(III) to **L1** generated (Λ_{Lu})-**L1**•[Lu] (Fig. 2g, lower pathway), to which subsequent addition of Cu(I) salts led to a red precipitate that could not be redissolved, presumably a mixture of Cu(I)-coordinated oligomers and polymers. Adding both Cu(I) and Lu(III) salts simultaneously to **L1** (Fig. 2g, middle pathway) produced some red precipitate together with a modest amount of ($\Lambda_{Cu}, \Lambda_{Lu}$)-**L1**•[Lu][Cu], the fully folded precursor to the 5₂ knot. Only stepwise addition of first Cu(I), then Lu(III) (Fig. 2g, top pathway), afforded ($\Lambda_{Cu}, \Lambda_{Lu}$)-**L1**•[Lu][Cu] as the major, correctly folded, intermediate that could subsequently be covalently captured by RCM to form the 5₂ knot.

3₁ knot synthesis and tangle migration

Strand **L1** could be tied into a different knot by simply omitting the Cu(I)-coordination step (Fig. 3a). The strand ends of (Λ_{Lu})-**L1**•[Lu] were subsequently joined by ring closing olefin metathesis (Fig. 3a, step ii). After several rounds of SEC, trefoil knot (-3₁)-1•[Lu] was isolated in 60% overall yield from **L1**. DOSY-NMR confirmed the new knot to be a single molecular species (Fig. S37), mass spectrometry showed its molecular mass to be that of 1•[Lu] (Fig. S17-S19, m/z 1•[Lu]³⁺ 1005.6, 1•[Lu][CF₃SO₃]²⁺ 1582.5), and CD spectroscopy indicated helically chiral pdc groups coordinated to Lu(III) (Fig. 3b, blue trace). The ¹H NMR spectrum of (-3₁)-1•[Lu] in MeCN-*d*₃ is broad at room temperature (Fig. S26) but sharpens at 343 K (Fig. 3c, top trace), revealing proton chemical shifts (e.g. H_d and H_e) indicative of the strand crossings being located in the region of the Lu(pdc)₃ coordination motif.

Figure 3. Tying molecular strand L1 into a trefoil (3_1) knot. a) Synthesis of molecular trefoil knot $(-3_1)\text{-}1\text{•[Lu]}$ from ligand **L1** and subsequent entanglement transposition by displacement of Lu(III) with Cu(I). Reaction conditions: (i) $\text{Lu}(\text{CF}_3\text{SO}_3)_3$, MeCN, 80 °C, 16 h. (ii) Hoveyda-Grubbs 2nd Generation catalyst, $\text{CH}_3\text{NO}_2/\text{CH}_2\text{Cl}_2$ 1:1, 50 °C, 40 h, 60% over two steps. (iii) $(\text{CH}_3\text{CN})_4\text{Cu}(\text{CF}_3\text{SO}_3)$, MeCN, RT, 10 min, 15% (after SEC purification). b) CD spectra (MeCN, 0.1 mM, 298 K) of the two knot conformers $(-3_1)\text{-}1\text{•[Lu]}$ (blue) and $(-3_1)\text{-}1\text{•[Cu]}$ (purple). c) ^1H NMR spectra (600 MHz, MeCN- d_3 , 343 K) of the entanglement transposition from $(-3_1)\text{-}1\text{•[Lu]}$ to $(-3_1)\text{-}1\text{•[Cu]}$. Key ^1H signals highlighted, lines indicate changes following addition of Cu(I) to $(-3_1)\text{-}1\text{•[Lu]}$. For full assignments, see Supplementary information.

When investigating whether lutetium-coordinated trefoil knot $(-3_1)\text{-}1\text{•[Lu]}$ could still bind to an additional Cu(I) ion through the free dpp binding sites, a surprising result was obtained (Fig. 3a, step iii and Fig. 3c, bottom trace). Within five minutes of adding $\text{Cu}(\text{OTf})\cdot 4\text{MeCN}$ to a solution of $(-3_1)\text{-}1\text{•[Lu]}$ in MeCN at room temperature, the solution turned dark red. However, instead of a bimetallic complex, ESI-MS showed that only a single metal ion was bound by the trefoil knot (Figs. S20-S21, m/z 1•[Cu]^+ 2905.1); a Cu(I) ion had displaced the Lu(III) ion. An identical species could be prepared step-wise by first

demetallating $(-3_1)\text{-}1\cdot[\text{Lu}]$ with tetraethylammonium fluoride (Et_4NF) in MeCN and then remetallating with $\text{Cu}(\text{OTf})\cdot 4\text{MeCN}$ (see Supplementary Information, section S7). The ^1H NMR spectrum of the resulting complex, $(-3_1)\text{-}1\cdot[\text{Cu}]$, shows the metal ion to be coordinated to the dpp sites with the pdc sites vacant (Fig. 3c, bottom trace). The CD spectrum for $(-3_1)\text{-}1\cdot[\text{Cu}]$ shows a strong Cotton effect at 330 nm (Fig. 3b, purple trace), but unlike $(+5_2)\text{-}1\cdot[\text{Cu}][\text{Lu}]$ this Cotton effect is positive. This corresponds to transfer of the Λ -helicity from the $\text{Lu}(\text{pdc})_3$ tangle to the new clasp crossing site through an additional twist and shift in the position of entanglement within the trefoil knotted chain (Fig. 3a, step iii). This transposition results in an increase in topological writhe from 3 in $(-3_1)\text{-}1\cdot[\text{Lu}]$ to 4 (in $(-3_1)\text{-}1\cdot[\text{Cu}]$). In topological terms^{17,36} the additional nugatory crossing can be introduced via a Reidemeister I+III sequence (Fig. S4). Circular dichroism (Fig. S9) showed that $\text{Cu}(\text{I})$ coordination to the isomeric unknot macrocycle ($0_1\text{-}1$) proceeds without chiral induction in the phenanthroline region, demonstrating that the transfer of handedness to the dpp sites in $(-3_1)\text{-}1\cdot[\text{Cu}]$ is a consequence of the chiral trefoil knot topology, rather than a reflection of the asymmetric centers adjacent to the pdc groups in the strand. The transfer of the location of entanglement from one well-defined region of a knot to another opens up the intriguing possibility of using metal ions, or other stimuli, to manipulate the conformation and writhe of knotted loops in a form of molecular 'cat's cradle'⁴⁴.

Figure 4. Metal-free topoisomer synthesis and characterisation. a) Synthesis of metal-free topoisomers (+5₂)-1, (-3₁)-1 and (0₁)-1 and their corresponding MALDI-TOF spectra. Reaction conditions: (i) Hoveyda-Grubbs 2nd Generation catalyst, CH₂Cl₂, 50°C, 40 h, 35%. (ii) Et₄NF, MeCN/CH₂Cl₂ 50:1, RT, 2 h, 57%. (iii) (CH₃CN)₄Cu(CF₃SO₃), MeCN, RT, 10 min, 15%. (iv) KCN, MeCN/H₂O/CH₂Cl₂ 1:5:5, RT, 16 h; then Et₄NF, MeCN/CH₂Cl₂ 1:1.6, RT, 1 h, 66%. b) ¹H NMR spectra (600 MHz, CDCl₃, 325 K) of the topoisomers (0₁)-1 (top), (-3₁)-1 (middle) and (+5₂)-1 (bottom). c) Variable temperature (298-393 K) ¹H NMR spectra (500 MHz, 1,1,2,2-tetrachloroethane-*d*₂) of unknot (0₁)-1 (left) and three-twist knot (+5₂)-1 (right). Key ¹H signals highlighted, for full assignments see Supplementary information.

Metal-free knot topoisomers

Once their role of chaperoning the folding and entanglement of the molecular strand is complete, the metal ions can be removed after covalent capture of the topology by RCM. Demetallated knots (-3₁)-1 and (+5₂)-1 were obtained from treatment of the metal-knot complexes with potassium cyanide (KCN, to remove Cu(I)) and/or tetraethylammonium fluoride (Et₄NF, to remove Lu(III)), and the corresponding unknot isomer, (0₁)-1, was produced by macrocyclization of **L1** (Fig. 4a). The three topoisomers were confirmed to have the same molecular mass by ESI-MS and matrix-assisted laser desorption/ionization-time of flight (MALDI-TOF) spectrometry, although (0₁)-1 and (-3₁)-1 formed ions preferentially with Na⁺ whereas (+5₂)-1 ionized with a H⁺ (Fig. 4a and Figs. S23-S25). Circular dichroism showed only minor differences between the three topoisomers (Fig. S83), suggesting that in the absence of metal ions none of the knots have a particularly preferred conformation. Rather, the effects of topological chirality are smeared out over the different environments each part of the chain experiences in numerous conformations.

The topoisomers have different diffusion constants in DOSY-NMR measurements (Table S2), with unknot macrocycle (0₁)-1 having the smallest effective radius (a result of solvent being able to pass through the cavity of the ring) and the looser knot (3₁)-1 the largest. The topoisomers have very different room temperature ¹H NMR spectra and temperature dependent behaviour (Figs. 4b and 4c). The ¹H NMR spectrum of unknot macrocycle (0₁)-1 in CDCl₃ is sharp at 298 K, with the minimum number of signals for each type of chemically distinct proton (e.g. H_k, H_i, H_h; Fig. 4b, top). The spectrum in 1,1,2,2-tetrachloroethane-*d*₂ is essentially invariant between 298 K and 393 K (Fig. 4c, left; Fig. S32). In contrast, the ¹H NMR spectra of knots (-3₁)-1 and (+5₂)-1 in CDCl₃ are broad at room temperature (Fig. S29) as a consequence of slow reptation⁴⁵ (snake-like motion of the entangled chain through the tight loops and crossings of the knotted backbone). At elevated temperatures sharpening of the resonances occurs for both knots, as reptation becomes faster on the NMR timescale and the signals become time-averaged. The ¹H NMR spectrum of the looser trefoil knot (-3₁)-1 is well-resolved at 325 K in CDCl₃ (Fig. 4b, middle), but heating to 393 K (in 1,1,2,2-tetrachloroethane-*d*₂) is necessary to obtain sharper features for the more entangled three-twist knot (+5₂)-1 (Fig. 4c, right; Fig. S31).

Conclusions

Metal ions can be used to direct the folding and entanglement of synthetic molecular strands along distinct pathways that result in knotted structures, in a manner reminiscent of the role played by chaperones during protein folding. Different metal ions, and combinations of metal ions, can be used to tie different knots using the same strand. The chirality of one tangle can be used to control the stereochemistry of another, enabling the tying of knots of low or high symmetry. Differently knotted isomers have different properties: for example, in terms of the number of metal ions a closed-loop strand can bind to. Metal ion complexation can also be used to change the position of an entanglement, and consequently the writhe, of the knot. The ability to tie nanoscale strands into different knots, and subsequently change the region and degree of entanglement, opens up new research directions for modifying the function and properties of synthetic molecular structures.

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Author contributions

F.S. and L.P. devised the original concept. D.P.A., L.P., F.S. and J.S. planned and carried out the synthetic work. J.H.S. performed the computational investigations. D.A.L. directed the research. All authors contributed to the analysis of the results and the writing of the manuscript.

Competing Interests statement

The authors declare no competing interests.

Additional information: Supplementary Information is available for this paper. Correspondence and requests for materials should be addressed to David A. Leigh.

Data availability

The data that support the findings of this study are available within the paper and its Supplementary Information, or are available from the Mendeley data repository (<https://data.mendeley.com/>) under doi xxxxxx.