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Numerical Investigation of Influences of Liquid Types on Flow Distribution and Temperature Distribution in Disc Type ON Cooled Transformers

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Abstract—In this paper, dimensional analysis is adopted to study fluid flow distribution and temperature distribution in disc-type ON (oil natural) cooled transformer windings. Theoretical analysis on the thermal driving force and the pressure drop in the liquid circulation loop is also performed to determine the total liquid flow rate in the transformer. The thermal performance of three different liquids, a hydrocarbon mineral oil, a hydrocarbon gas-to-liquid (GTL) oil and a synthetic ester are investigated using computational fluid dynamics (CFD) simulations, based on the understanding from dimensional analysis and the flow rates determined from the theoretical analysis. It is found in the investigated conditions that the hydrocarbon mineral and GTL oil share similar thermal performance; the synthetic ester has a lower total flow rate due to its higher viscosity and therefore requires additional effort to improve the thermal performance.

Keywords—CFD; dimensional analysis; disc-type winding; flow distribution; hot-spot temperature; hot-spot factor; ON transformer; ester; mineral oil; GTL oil

I. INTRODUCTION

Power transformers connect power systems of different voltage levels. The reliability of the transformer is of great importance to the reliability and safety of the power system. Apart from premature failure due to faults, transformer life expectancy is mainly dictated by the thermal ageing process of the insulation cellulose [1, 2]. The highest temperature in the winding, usually referred to as the hot-spot temperature, is of great interest to the transformer thermal designer and operator because it causes the severest thermal degradation.

Generally, the cooling of the windings of power transformers relies on the circulation of the dielectric coolant fluid between the radiator and the winding. The liquid flow distribution in conjunction with power loss distribution determines the temperature distribution. The liquid flow and the heat transfer processes in the winding, are mainly investigated by using thermal-hydraulic network models and models that incorporate computational fluid dynamics (CFD). For oil directed (OD) cooling modes, liquid flow and heat transfer are weakly coupled. Therefore, the hydraulic system and the thermal system can be investigated separately [3-5]. For oil forced/natural (OF/ON) cooling modes, liquid flow and heat transfer are strongly coupled and therefore buoyancy force and hot-streak dynamics play vital roles in determining the fluid flow and temperature distribution in the winding [6-8].

Other than traditional hydrocarbon mineral oil, alternative liquids like synthetic esters, natural esters and hydrocarbon gas-to-liquid (GTL) oils are increasingly being used as dielectric coolant for power transformers due to their

properties and performance, and potential for reduced fire and environmental risks. The influences of different liquids on OD transformer flow and temperature distributions are shown in [9]. In this paper, fluid flow and temperature distributions in disc-type ON transformer windings are investigated theoretically, followed by numerical investigation of the influences of different liquids upon the fluid flow distribution and the temperature distribution.

II. WINDING GEOMETRY UNDER INVESTIGATION

The winding under investigation is a LV winding of a 66 MVA 225/26.4 kV ONAN/ONAF transmission transformer [10]. This LV winding consists of 4 passes with pass 1 at the bottom being an anomaly, as shown in Fig. 1. There are 2 parts in pass 1. Part 1 is not representative of an ON transformer winding pass with 2 discs and three horizontal ducts. Part 2 is a typical ON winding pass and it is repeated to become the other 3 following passes with inlet alternating between the inner and outer vertical ducts to form a zigzag flow pattern. Since the geometry of the last 3 passes repeats part 2 of pass 1, the geometry of the whole winding is not illustrated in Fig. 1.

Fig. 1. Axisymmetric 2D geometry. (a) Winding geometry of pass 1 at the bottom of the LV winding. (b) Geometric details of one strand.

III. DIMENSIONAL ANALYSIS

Heat transfer in the winding involves conduction in the solid domain (copper and paper insulation) and convection in the fluid domain. The conduction is governed by Fourier's law of conduction. The convection, which is the challenging part, is governed by three conservation laws, i.e. the conservations of mass, momentum and energy.

A. Boussinesq Approximation

According to the Boussinesq approximation all fluid properties are assumed constant except for density in the buoyancy force term. In cylindrical coordinates, the conservation equations of mass, momentum and energy for axisymmetric 2D flow can be expressed by (1), (2) and (3), respectively.

$$\frac{1}{r} \frac{\partial(r u_r)}{\partial r} + \frac{\partial u_z}{\partial z} = 0 \quad (1)$$

$$\begin{cases} u_r \frac{\partial u_r}{\partial r} + u_z \frac{\partial u_r}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial r} + \nu \left(\frac{\partial}{\partial r} \left(\frac{1}{r} \frac{\partial(r u_r)}{\partial r} \right) + \frac{\partial^2 u_r}{\partial z^2} \right) \\ u_r \frac{\partial u_z}{\partial r} + u_z \frac{\partial u_z}{\partial z} = g\beta(T - T_{to}) + \nu \left(\frac{\partial}{\partial r} \left(r \frac{\partial u_z}{\partial r} \right) + \frac{\partial^2 u_z}{\partial z^2} \right) \end{cases} \quad (2)$$

$$u_r \frac{\partial T}{\partial r} + u_z \frac{\partial T}{\partial z} = \frac{k}{\rho c_p} \left(\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial T}{\partial r} \right) + \frac{\partial^2 T}{\partial z^2} \right) \quad (3)$$

where r (m) is denoted for the radial coordinate, u_r (m/s) for velocity radial component, z (m) for axial coordinate, u_z (m/s) for velocity axial component, ρ (kg/m³) for liquid density, p (Pa) for static pressure, ν (m²/s) for kinematic viscosity, g (m/s²) for gravitational acceleration, β (1/K) for volumetric thermal expansion coefficient, T (K) for liquid temperature, T_{to} (K) for liquid temperature at the top of the winding, k (W/(m·K)) for liquid thermal conductivity, c_p (J/(kg·K)) for liquid specific heat.

It is worth mentioning that the viscous dissipation term in the energy equation is neglected due to the small flow rate in transformer windings.

B. Dimensionless Forms

To transfer the governing equations to their dimensionless forms, the dimensionless independent variables are defined as:

$$r^* = \frac{r}{D_h} \quad \text{and} \quad z^* = \frac{z}{D_h} \quad (4)$$

$$u_r^* = \frac{u_r}{u_m} \quad \text{and} \quad u_z^* = \frac{u_z}{u_m} \quad (5)$$

$$p^* = \frac{p}{\rho u_m^2} \quad \text{and} \quad T^* = \frac{T - T_{to}}{T_{aw} - (T_{to} + T_{bo})/2} = \frac{T - T_{to}}{g_{ave}} \quad (6)$$

where D_h (m) is denoted for hydraulic diameter, defined as twice the inner vertical duct width (w_{inn}), u_m (m/s) for average liquid velocity at the inner vertical duct inlet, T_{aw} (K) for average winding temperature, T_{bo} (K) for winding bottom liquid temperature, g_{ave} (K) for the average temperature gradient between the winding and the average liquid temperature taken as the average of winding top and bottom liquid temperatures.

Substituting (4), (5) and (6) into the governing equations and noticing that the reference parameters (D_h , T_{aw} , T_{to} , T_{bo} , u_m) are not functions of the coordinates, we have the dimensionless governing equations:

$$\frac{1}{r^*} \frac{\partial(r^* u_r^*)}{\partial r^*} + \frac{\partial u_z^*}{\partial z^*} = 0 \quad (7)$$

$$\begin{cases} u_r^* \frac{\partial u_r^*}{\partial r^*} + u_z^* \frac{\partial u_r^*}{\partial z^*} = -\frac{\partial p^*}{\partial r^*} + \frac{1}{\text{Re}} \left(\frac{\partial}{\partial r^*} \left(\frac{1}{r^*} \frac{\partial(r^* u_r^*)}{\partial r^*} \right) + \frac{\partial^2 u_r^*}{\partial z^{*2}} \right) \\ u_r^* \frac{\partial u_z^*}{\partial r^*} + u_z^* \frac{\partial u_z^*}{\partial z^*} = \frac{\text{Gr}}{\text{Re}^2} T^* + \frac{1}{\text{Re}} \left(\frac{\partial}{\partial r^*} \left(r^* \frac{\partial u_z^*}{\partial r^*} \right) + \frac{\partial^2 u_z^*}{\partial z^{*2}} \right) \end{cases} \quad (8)$$

$$u_r^* \frac{\partial T^*}{\partial r^*} + u_z^* \frac{\partial T^*}{\partial z^*} = \frac{1}{\text{Re} \cdot \text{Pr}} \left(\frac{\partial}{\partial r^*} \left(r^* \frac{\partial T^*}{\partial r^*} \right) + \frac{\partial^2 T^*}{\partial z^{*2}} \right) \quad (9)$$

where the definitions of Re, Pr and Gr/Re² are shown below:

$$\text{Re} = \frac{u_m D_h}{\nu} \quad (10)$$

$$\text{Pr} = \frac{\mu c_p}{k} \quad (11)$$

$$\frac{\text{Gr}}{\text{Re}^2} = \frac{g\beta(T_{aw} - (T_{to} + T_{bo})/2)D_h}{u_m^2} \quad (12)$$

where μ (Pa·s) stands for liquid dynamic viscosity.

C. Flow and temperature distribution in the fluid domain

For a fixed winding geometry with a fixed power loss distribution in dimensionless senses, both liquid flow distribution and temperature distribution are determined by the coefficients, Re, Gr/Re² and Pr as shown in the dimensionless governing equations (7)-(9). Pr plays the same role as Re in (9). Re in conjunction with Gr/Re² determines liquid flow distribution in (8). For ON cooling modes, flow and temperature are strongly coupled. Therefore, Re is more influential than Pr in determining flow and temperature distribution. Gr/Re² is related to buoyancy force which is the main driving force of the flow. In conclusion, liquid flow distribution and temperature distribution are mainly controlled by Re, Pr and Gr/Re². Following the same argument as presented in [11], we can conclude that the hot-spot factor for ON cooling modes are mainly controlled by Re, Pr and Gr/Re².

IV. DETERMINATION OF TOTAL LIQUID FLOW RATE

For ON cooling modes, total liquid flow rate in the winding has a significant influence on the liquid flow distribution, and the temperature distribution. The total liquid flow rate is determined by the thermal driving force (p_T) and the pressure drop (p_D) over the whole circulation loop. A schematic illustration of the loop is shown in Fig. 2.

A. Thermal Driving Force

The thermal driving force can be expressed as:

$$p_T = \oint \rho \cdot \vec{g} d\vec{l} \quad (13)$$

Under the assumptions that heat transfer occurs only in the winding and the radiator, and temperatures rise linearly with elevation in the winding and the radiator, the thermal driving force in (13) can be approximated to be:

$$p_T = \rho_0 \cdot g \cdot \beta \cdot \Delta T \cdot \Delta H \quad (14)$$

where ρ_0 (kg/m³) is a reference density at 20 °C, ΔT (K) is the liquid temperature gradient between the top and bottom

of the winding, ΔH (m) is height difference of the central points of the radiator and the winding.

Fig. 2. Schematic illustration of the liquid circulation loop.

B. Pressure Drop in the Loop

The pressure drop in the loop is determined by the geometry, liquid properties and liquid flow rate. It is verified experimentally that for ON cooling modes, the so called minor pressure drops related to the change of flow direction is negligible, compared to the major pressure drop due to friction [7]. Therefore, the pressure drop over the loop can be expressed as:

$$p_D = \frac{C}{\text{Re}} \frac{L'}{H'} \frac{\rho u_m^2}{2} \quad (15)$$

where C is a constant, L' (m) and H' (m) are the equivalent length and the equivalent diameter of the circulation loop.

C. Determination of Total Flow Rate

Applying energy conservation to the total liquid flow through the winding or the radiator, in steady state we have:

$$\Delta T = \frac{P}{\dot{m} c_p} = \frac{P}{A u_m \rho c_p} \quad (16)$$

where P (W) is the total power loss in the winding or radiator, A is the cross sectional area of the winding inlet.

Combining (14), (15) and (16), we have:

$$u_m^2 = \frac{2 \rho_0 g \beta H'^2}{\mu C L' A \rho c_p} \Delta H \cdot P \quad (17)$$

Notice that for a given liquid and a given winding geometry ρ_0 , g , β , H' , L' , μ , C , A , ρ , c_p can all be treated as constant. Therefore the total liquid flow rate characterized by the winding inlet velocity u_m is proportional to the square root of the total power loss in the winding, and the square root of the central point height difference between the radiator and the winding. These square root relationships between u_m and P and ΔH are obtained experimentally in [7].

V. INFLUENCES OF LIQUID TYPES

For a fixed winding geometry (fixed geometrical boundary conditions and fixed ΔH) with a fixed power loss distribution (fixed P), the total liquid flow rate is determined by the properties of the liquid as shown in (17). In (17), liquid-type related properties are ρ_0 , μ , ρ and c_p . Three types of liquid are investigated in this paper. They are a traditional hydrocarbon mineral oil, a hydrocarbon gas-to-liquid (GTL)

oil and a synthetic ester. The properties of these three liquids are obtained from least-square curve fittings of the results provided by the manufacturers.

$$\begin{cases} \rho_1 = -0.6568 \times T + 1064 \text{ [kg/m}^3\text{]} \\ \rho_2 = -0.6455 \times T + 995.5 \text{ [kg/m}^3\text{]} \\ \rho_3 = -0.7327 \times T + 1185 \text{ [kg/m}^3\text{]} \\ \mu_1 = 7.863 \times 10^{-5} \times \exp(632.0/(T - 176.0)) \text{ [Pa} \cdot \text{s]} \\ \mu_2 = 6.133 \times 10^{-5} \times \exp(749.8/(T - 157.4)) \text{ [Pa} \cdot \text{s]} \\ \mu_3 = 6.239 \times 10^{-5} \times \exp(914.1/(T - 162.4)) \text{ [Pa} \cdot \text{s]} \\ c_{p1} = 3.950 \times T + 560 \text{ [J/(kg} \cdot \text{K)}] \\ c_{p2} = 4.449 \times T + 871.7 \text{ [J/(kg} \cdot \text{K)}] \\ c_{p3} = 2.069 \times T + 1287 \text{ [J/(kg} \cdot \text{K)}] \\ \beta_1 = 7.778 \times 10^{-4} \text{ [1/K]} \\ \beta_2 = 8.273 \times 10^{-4} \text{ [1/K]} \\ \beta_3 = 7.790 \times 10^{-4} \text{ [1/K]} \end{cases}$$

where the subscript 1 is for the mineral oil, 2 for the GTL, 3 for the synthetic ester, T for temperature in Kelvin.

When we choose the flow rate of mineral oil as a unit, and liquid temperature as 70 °C to determine the properties (ρ_0 is determined at 20 °C), according to (17), the volumetric flow rate for the mineral oil, the GTL oil and the synthetic ester is 1: 0.919: 0.581.

Computations have been performed by using commercial finite element method based software COMSOL Multiphysics in laminar model. To compare the thermal performance of the three liquids, the winding inlet temperature is fixed to be 46.7 °C and the power loss of each disc is set to be 420 W, corresponding to a current density of 4 A/mm² at 85 °C copper resistance. The flow rate of the mineral oil is the benchmark which corresponds to a winding inlet velocity of 0.053 m/s. The inlet velocity of the GTL oil and the synthetic ester is therefore 0.049 m/s and 0.031 m/s, respectively.

The average liquid velocity in the middle of each horizontal cooling duct and the maximum temperature of each disc are shown in Fig. 3 and Fig. 4 respectively. Since part 1 of pass 1 is not representative of an ON transformer winding pass, the flow and temperature results in this part is not included in this paper. The comparisons of some lumped parameters and hot-spot temperature for these three liquids are shown in Table 1.

It can be seen from Fig. 3 and Fig. 4 that both hydrocarbons, the mineral oil and the GTL oil, share similar flow and temperature distribution because they have similar Re , Pr and Gr/Re^2 as shown in Table 1. Although the mineral oil has a slightly higher total flow rate than the GTL oil, the temperature of the GTL oil is slightly lower than the mineral oil due to its higher thermal conductivity and higher specific heat (which arise from its lower density). The synthetic ester has a much lower flow rate than the other two liquids and therefore has lower velocities in most of the horizontal ducts and higher disc temperatures. The flow distribution and temperature distribution of the synthetic ester are very different from those of the mineral oil and the

GTL oil because they have quite different Re , Pr and Gr/Re^2 as shown in Table 1. For the synthetic ester, the liquid at the top part of pass 4 is almost in stagnation, causing overheating at the top of the winding. The distorted temperature distribution of the synthetic ester results in a larger hot-spot factor than the other two liquids. To improve the thermal performance of the synthetic ester, a higher total liquid flow rate is needed. According to (17), a feasible way to do this would be to increase the height difference between the centre line of the radiator and the centre line of the winding, ΔH .

Fig. 3. Average liquid velocity in each horizontal cooling duct. Flow from outer vertical duct to inner vertical duct is set to be negative and vice versa.

Fig. 4. Maximum temperature of each disc.

Table 1. Comparisons of lumped parameters

	T_{aw} (°C)	T_{to} (°C)	T_{hs} (°C)	Re	Pr	Gr/Re^2	H
Mineral oil	70.4	67.4	83.0	169	68	0.65	1.17
GTL oil	69.1	66.1	81.4	143	80	0.72	1.20
Synthetic ester	76.9	78.6	109.6	42	172	2.06	2.17

where T_{aw} refers to average winding temperature, T_{to} to top oil temperature, T_{hs} to hot-spot temperature, H to hot-spot factor. Re , Pr and Gr/Re^2 are calculated based on oil properties at the average of winding top oil and winding bottom oil temperatures.

VI. CONCLUSION

Dimensional analysis on fluid flow and heat transfer in the winding has been performed for ON transformers. It is found that for a fixed winding geometry and a fixed power loss distribution in dimensionless senses the flow distribution and temperature distribution is governed by Re , Pr and Gr/Re^2 .

Theoretical analysis of the thermal driving force and the pressure drop in the liquid circulation loop, shows that the total volumetric flow rate is proportional to the square root of the power loss in the winding, and the square root of the height difference between the centre line of the radiator and the centre line of the winding, ΔH .

For different liquids, the ratios of total liquid flow rate are determined. CFD simulations of typical cases are performed. It is found that the hydrocarbon mineral oil gives similar thermal performance to the GTL oil in this evaluation. The synthetic ester on the other hand has quite different flow and temperature distribution due to the significant differences in Re , Pr and Gr/Re^2 . The low liquid flow rate of the synthetic ester can cause local overheating in the winding. A feasible way to improve the thermal performance of the synthetic ester would be to increase ΔH .

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